

Systems Biology and Networks

**MMG 835, SPRING 2016
Eukaryotic Molecular Genetics**

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What is Systems Biology

- **Wikipedia: “*Systems biology Systems biology is the computational and mathematical modeling of complex biological systems. An emerging engineering approach applied to biological scientific research, systems biology is a **biology-based** inter-disciplinary field of study that focuses on complex interactions within biological systems, using a holistic approach (holism instead of the more traditional reductionism) to biological research.*”**

What is Systems Biology

- **nature.com : “*Systems biology is the study of biological systems whose behaviour cannot be reduced to the linear sum of their parts’ functions. Systems biology does not necessarily involve large numbers of components or vast datasets, as in genomics or connectomics, but often requires quantitative modelling methods borrowed from physics.”***

What is Systems Biology

- Encyclopedia of Systems Biology (Springer New York, 2013).
- ***“Systems biology refers to the quantitative analysis of the dynamic interactions among several components of a biological system and aims to understand the behavior of the system as a whole. Systems biology involves the development and application of systems theory concepts for the study of complex biological systems through iteration over mathematical modeling, computational simulation and biological experimentation. Systems biology could be viewed as a tool to increase our understanding of biological systems, to develop more directed experiments, and to allow accurate predictions.”***

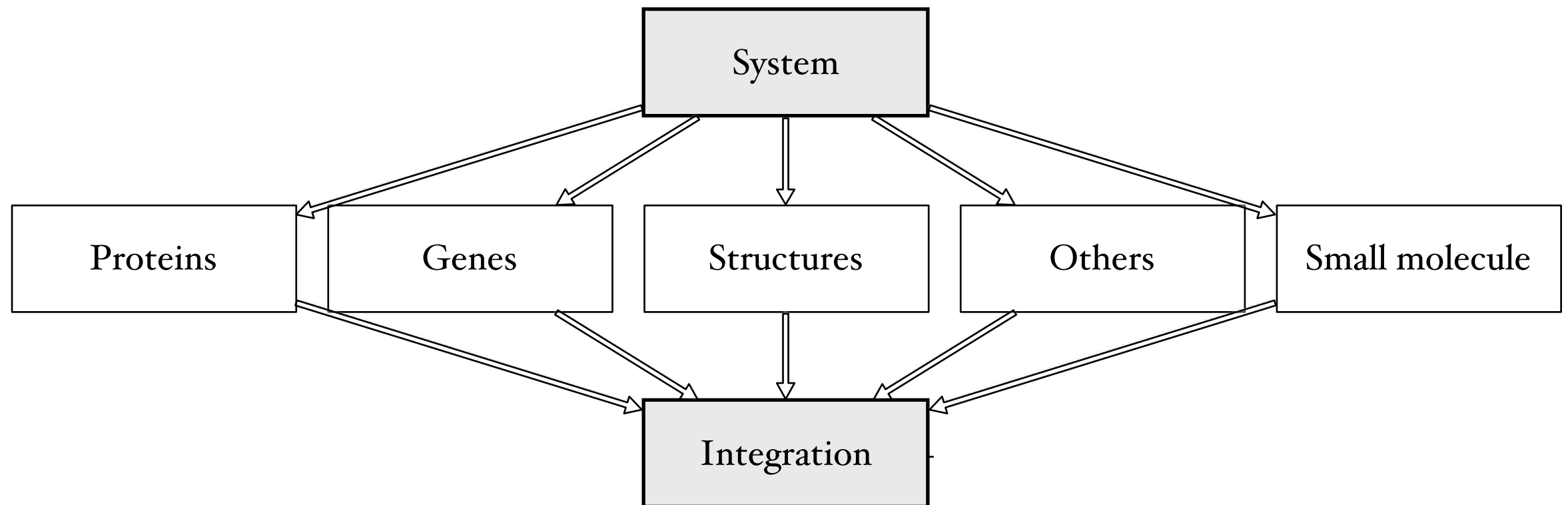
Systems Biology

- Systematic
- Novel approach (in biology at least)
- interdisciplinary
- Non-reductionist
 - Reductionist: Study the subcomponents for a system in detail, each one
 - Whole is greater the sum of its parts

Systems Biology

- Multiple inputs of information in a complex system
- More mathematical than traditional biology

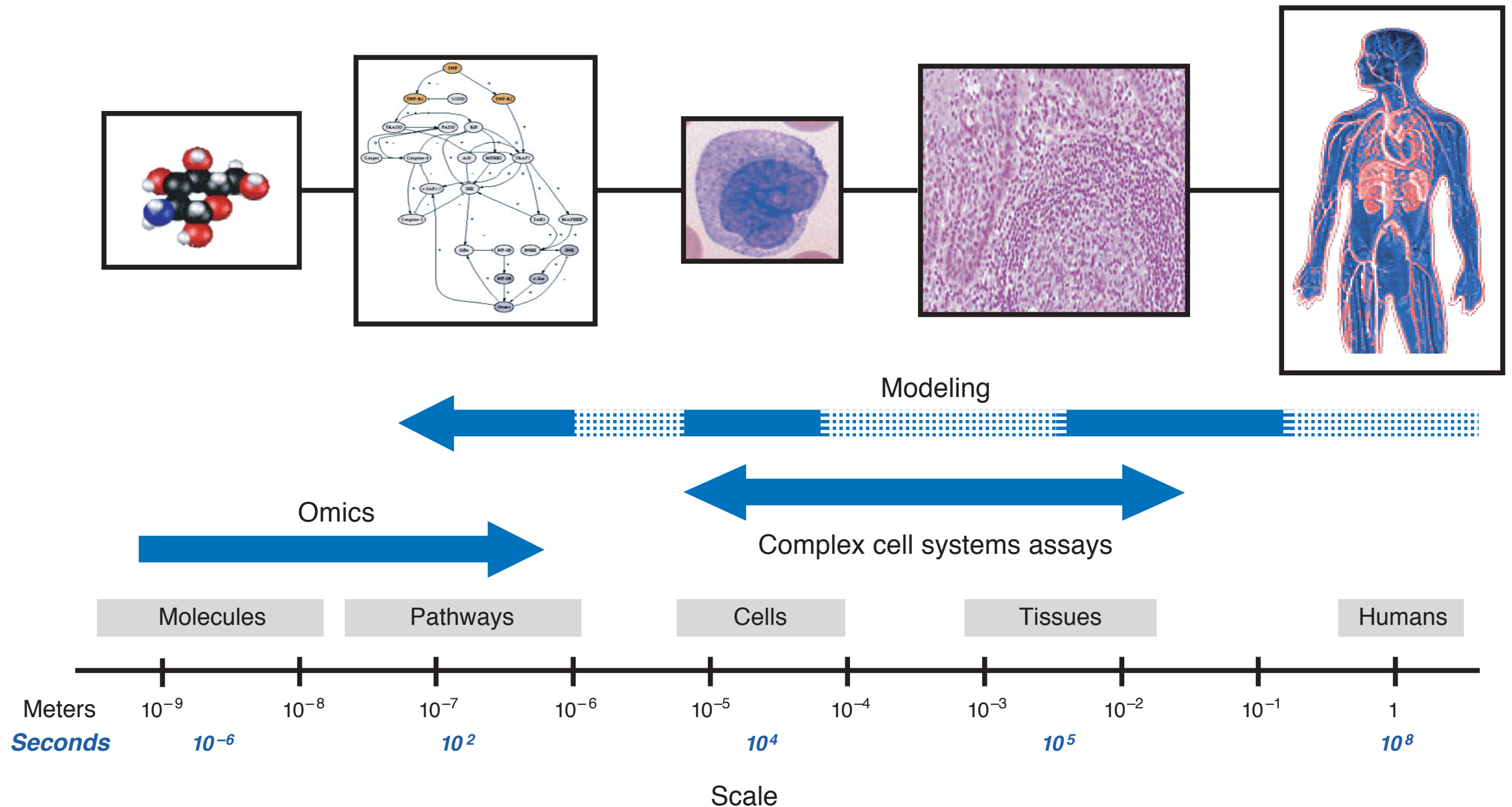
Systems Biology



Systems Biology

- Molecular components
 - Cell subsystems
 - parts of an organism
 - the organism
 - the environment
 - set of environments
- **Study of**
 - Function
 - Networks
 - Signals
 - Interactions of components

Systems Biology

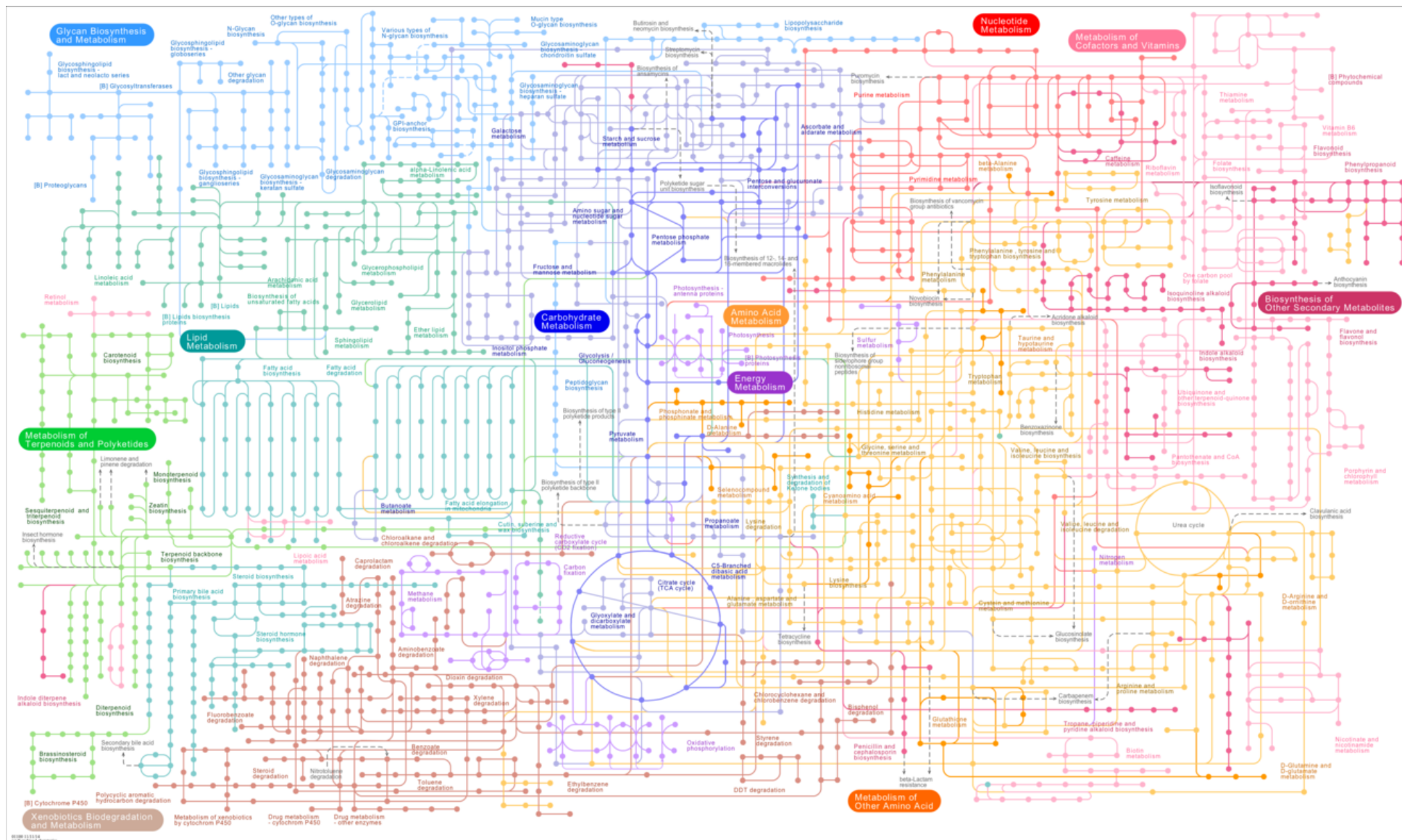


Systems Biology

- Examples
 - Omics approaches
 - Human Genome Project
 - Mass spectrometry
 - Proteomics
 - Metabolomics
 - name-it-omics

Systems Biology

- Example: Metabolism



<http://www.genome.jp/kegg/pathway/map/map01100.html> (11/18/2014)

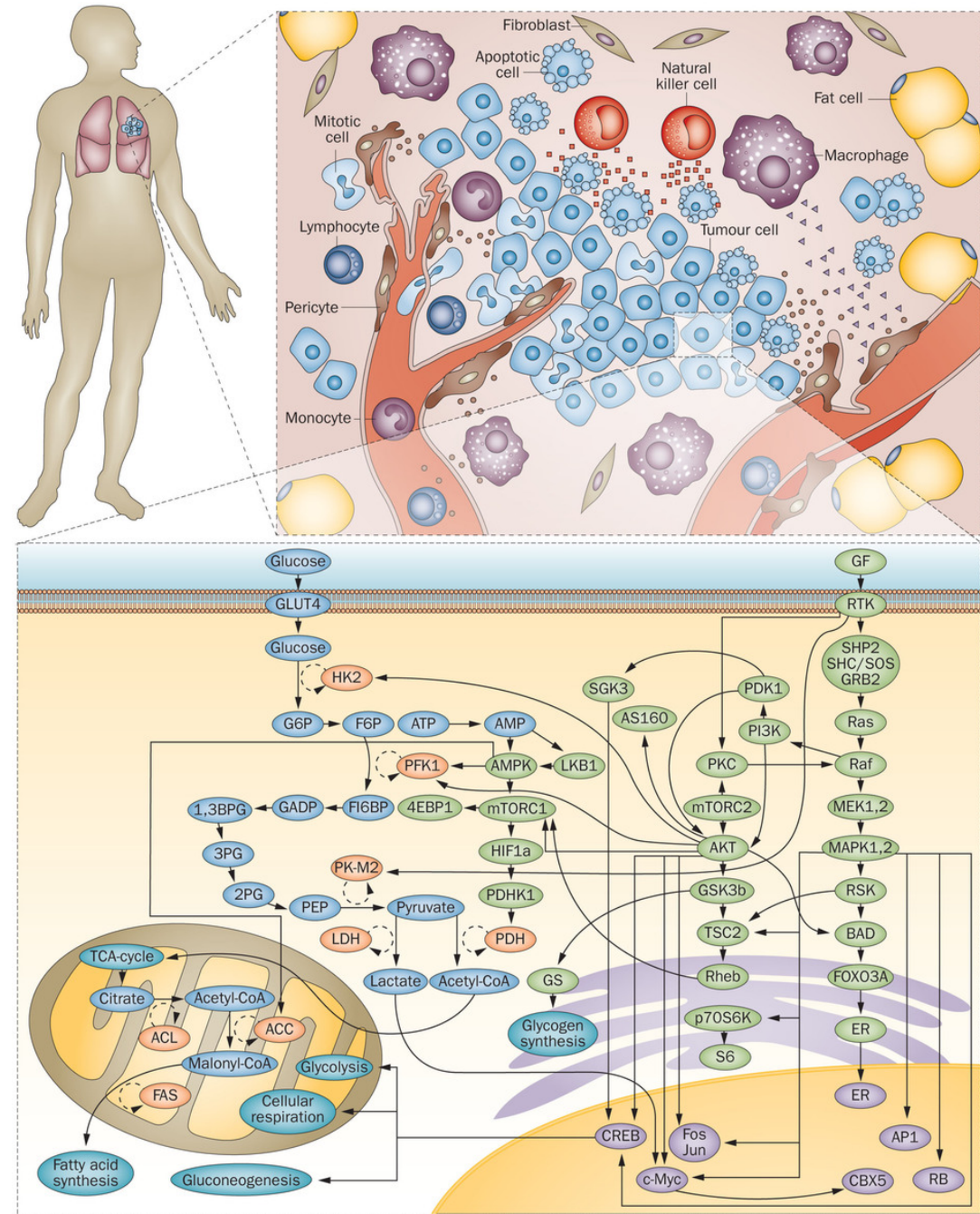
KEGG: Kyoto Encyclopedia of Genes and Genomes

- Example: Metabolism: Galactose Metabolism (degradation)



Systems Biology

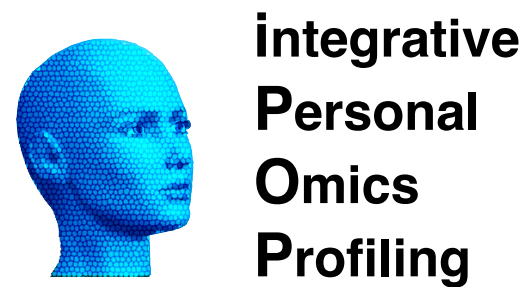
- Example: Cancer
- Different Networks
- Homeostasis
- Molecular components



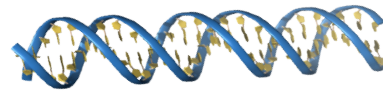
Werner, H. M. J. *et al.* (2014) *Nat. Rev. Clin. Oncol.* doi:10.1038/nrclinonc.2014.6

Systems Medicine

- Personalized
- Determine risks
- Monitor
- Integrate



I.



Whole Genome Sequencing

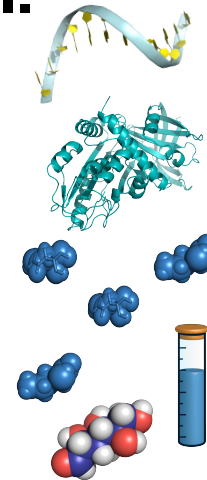
Disease Risk Evaluation

Medical History & Environment

Pharmacogenomic Evaluation

RISK EVALUATION

II.



Transcriptomics

Proteomics

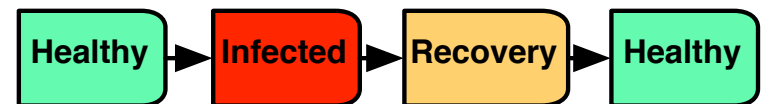
Metabolomics

Clinical Tests

Autoantibodyomics

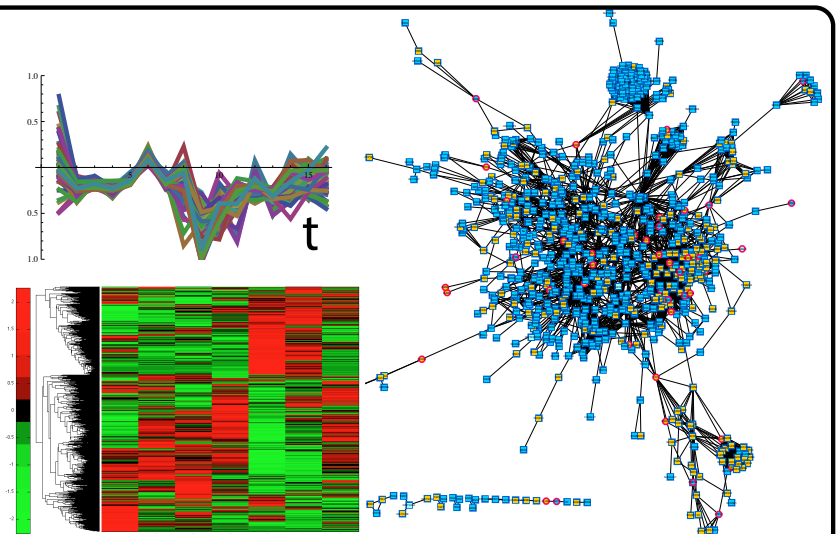
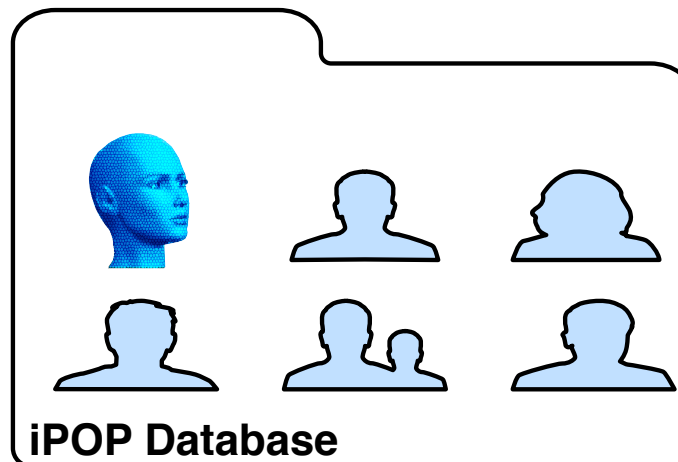
Microbiomics

New omics



LONGITUDINAL OMICS PROFILING
OF MULTIPLE PHYSIOLOGICAL
STATES

III.



INTEGRATION OF MULTIPLE OMICS AND TEMPORAL RESPONSES
MATCHED AGAINST iPOP DATABASES

Mias and Snyder, Quantitative
Biology 1(1) p. 71 (2013)

Chen*, Mias*, Li-Pook-Than*,
Jiang* et al Cell 148,1293 (2012)

<http://goo.gl/iamZth>

Systems Biology

- Experiments
- Models
 - data
 - theory
 - computation
- **Nobert Wiener (1894-1964)**
 - **cybernetics and systems controls)**
- **20th century biochemistry**
- **21st century Leroy Hood and others**

Systems Biology

- Experiments

• **BIG**
DATA!

Reformulate biological problems in terms of mathematical models.

Models need computational approaches

Big data handling in storing, retrieving useful information and relaying/displaying this information

Data - Omics

Molecular Components

Nucleic acids

Proteins

Lipids

Carbohydrates

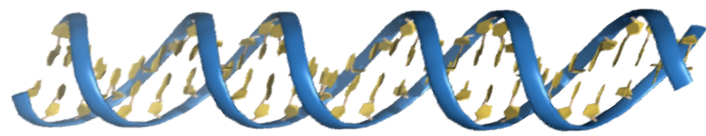
Genomics



Illumina

DNA VARIANTS

A



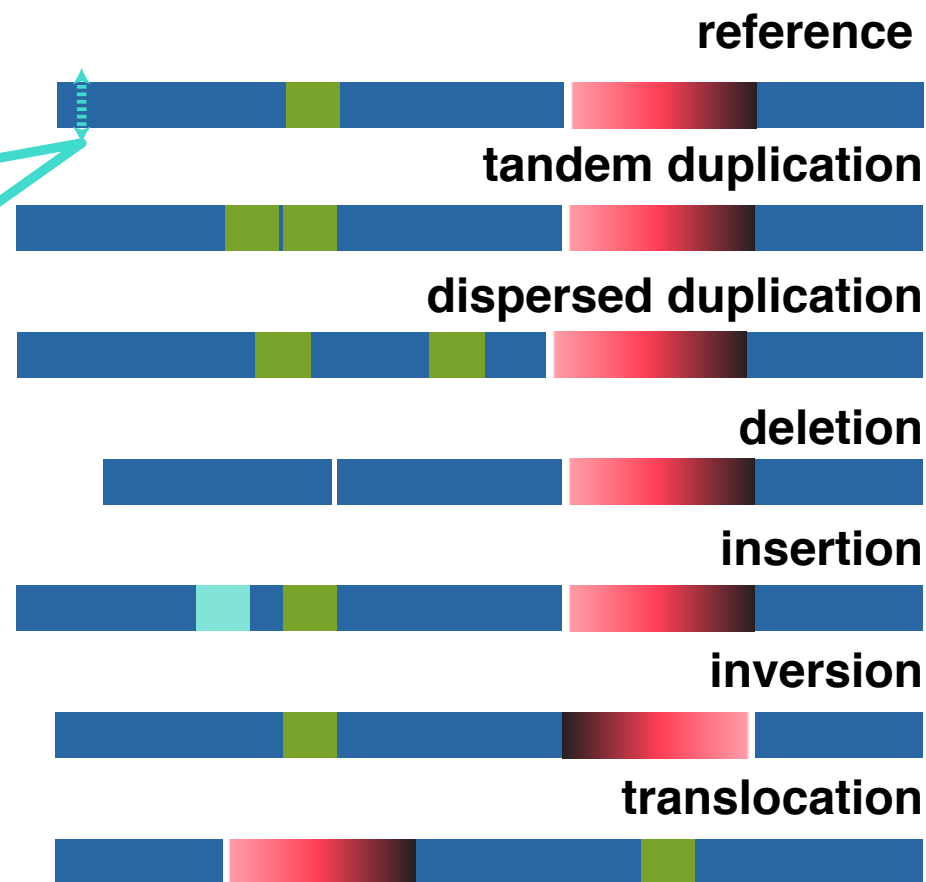
bp Level
Variation

reference *ggcttccaggaactc*
 point mutation *ggcttccag***a***aactc*
ggcttccaggaactc
 insertion *ggcttccagg***g***aactc*
*ggcttccagg***a***aactc*
 deletion *ggcttccagg***a***actc*
*ggcttccagg***X***aactc*



MinION

Structural Variation [>1000 bp]



SOLiD



PacBio

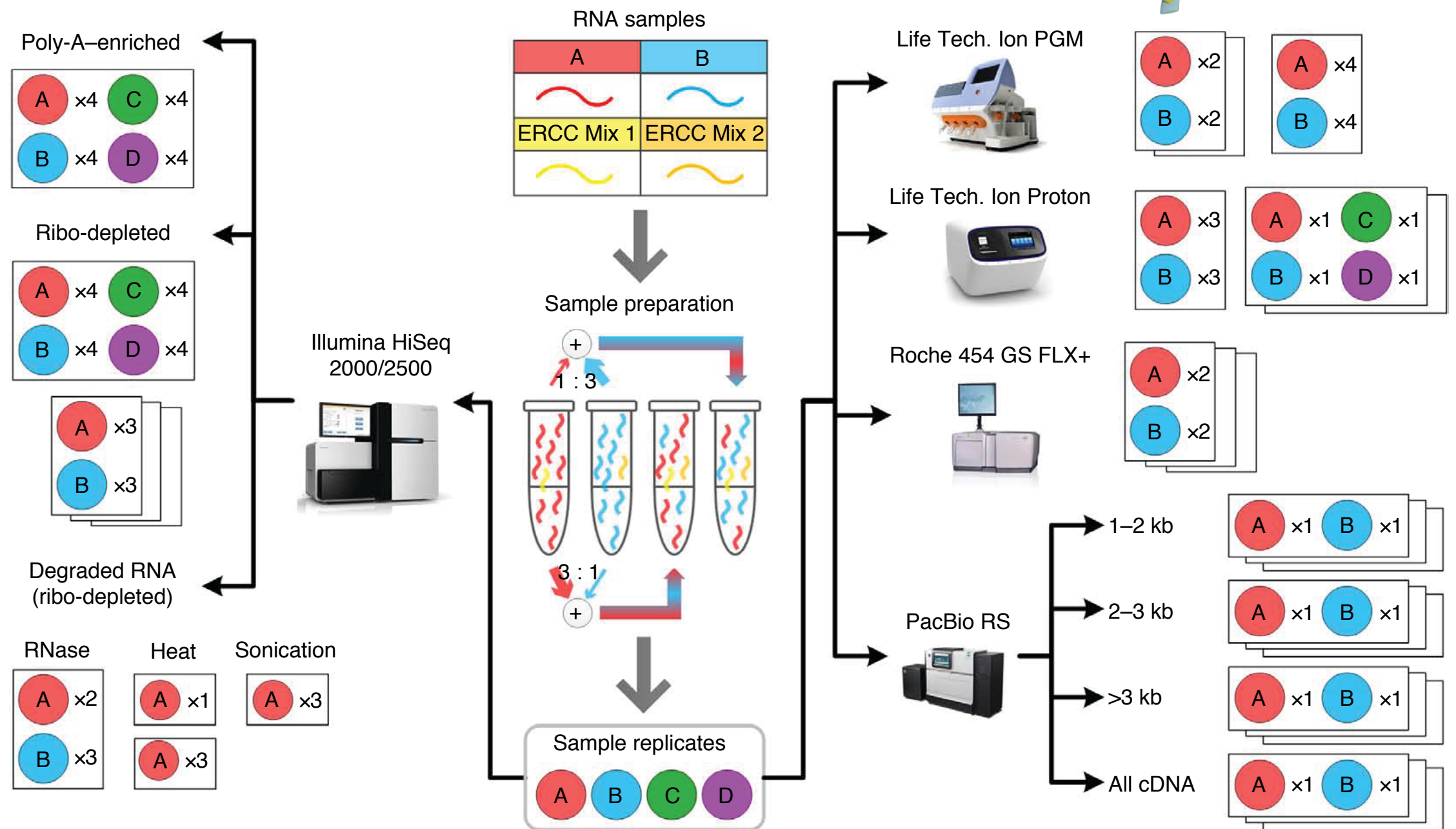
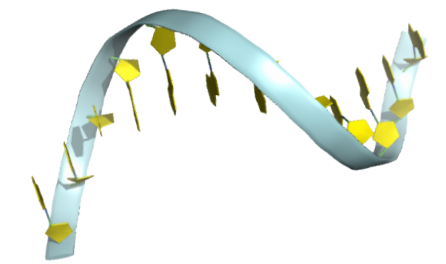


454

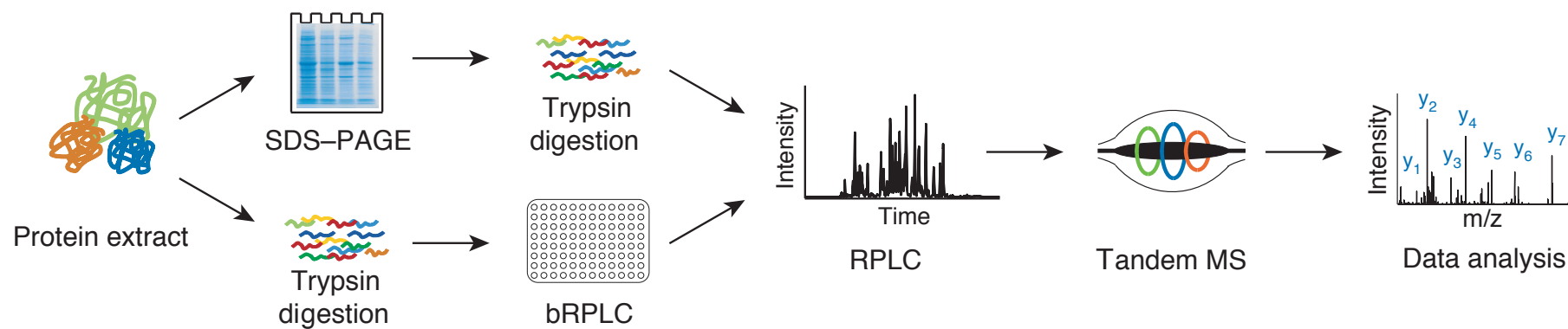
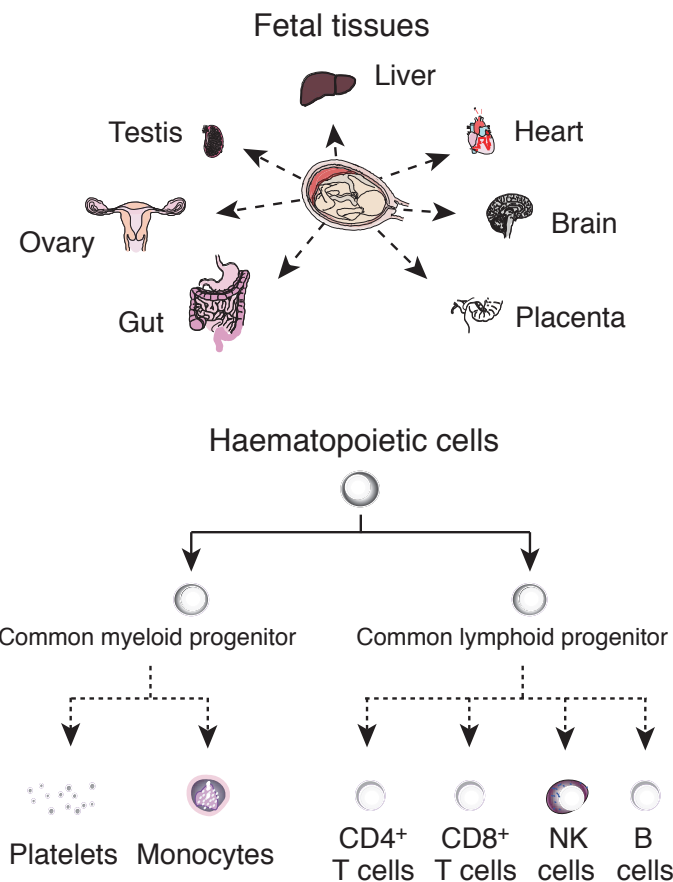
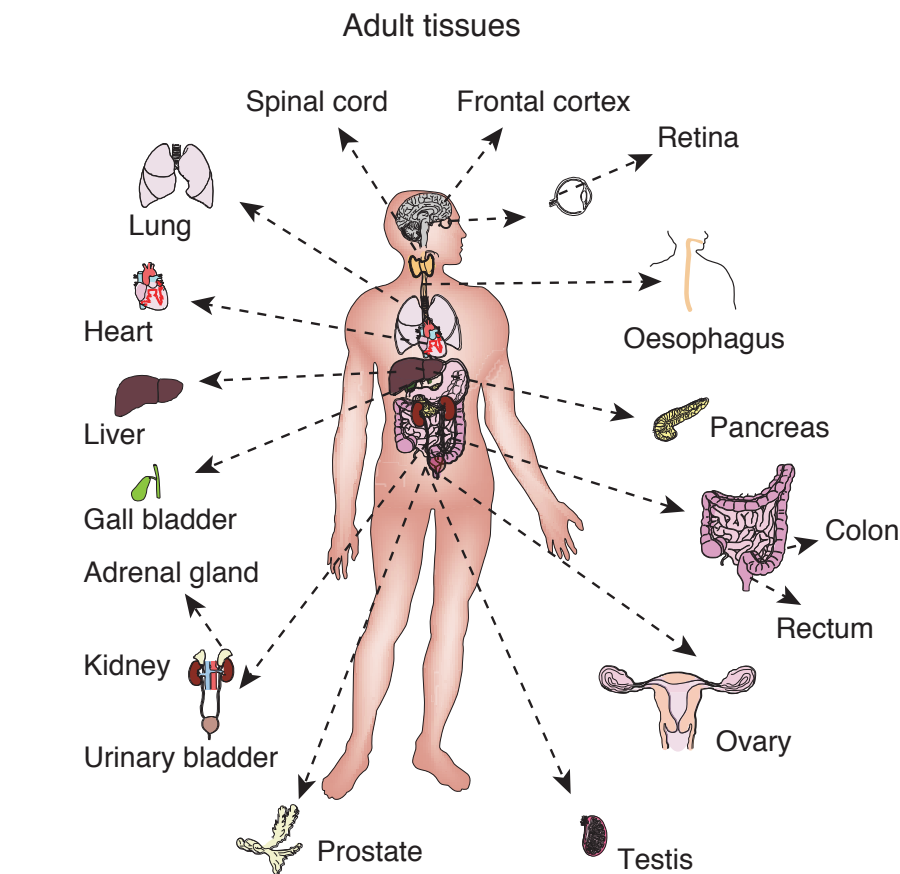
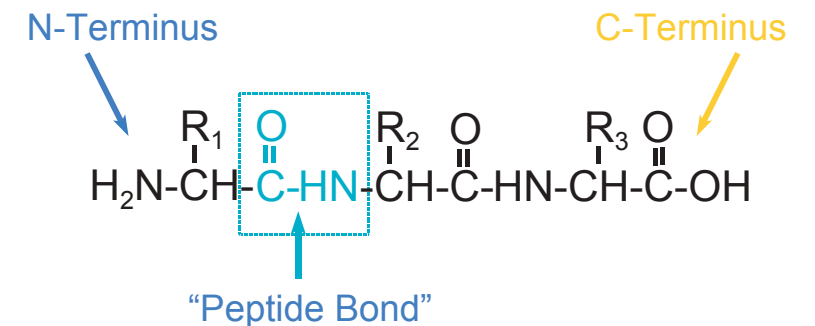
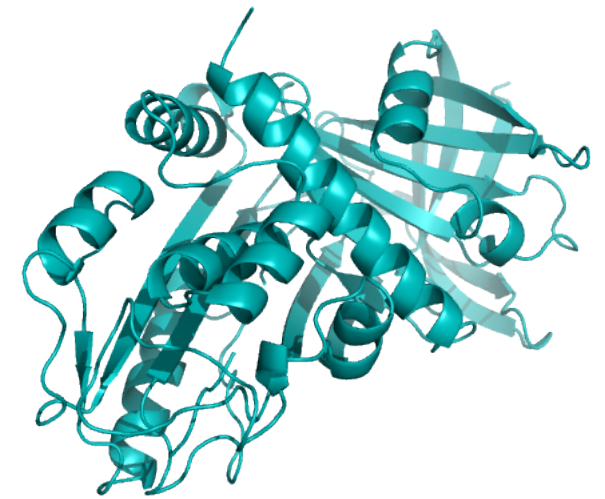


Ion Torrent

Transcriptomics



Proteomics



A draft map
of the human
proteome

Kim et al., Nature 509, p. 575 2014

Metabolomics



thermofisher.com

NMR

Other varieties



agilent.com

all metabolites in cells

- small molecules
- lipids
- peptides
- amino acids
- nucleic acids
- organic acids

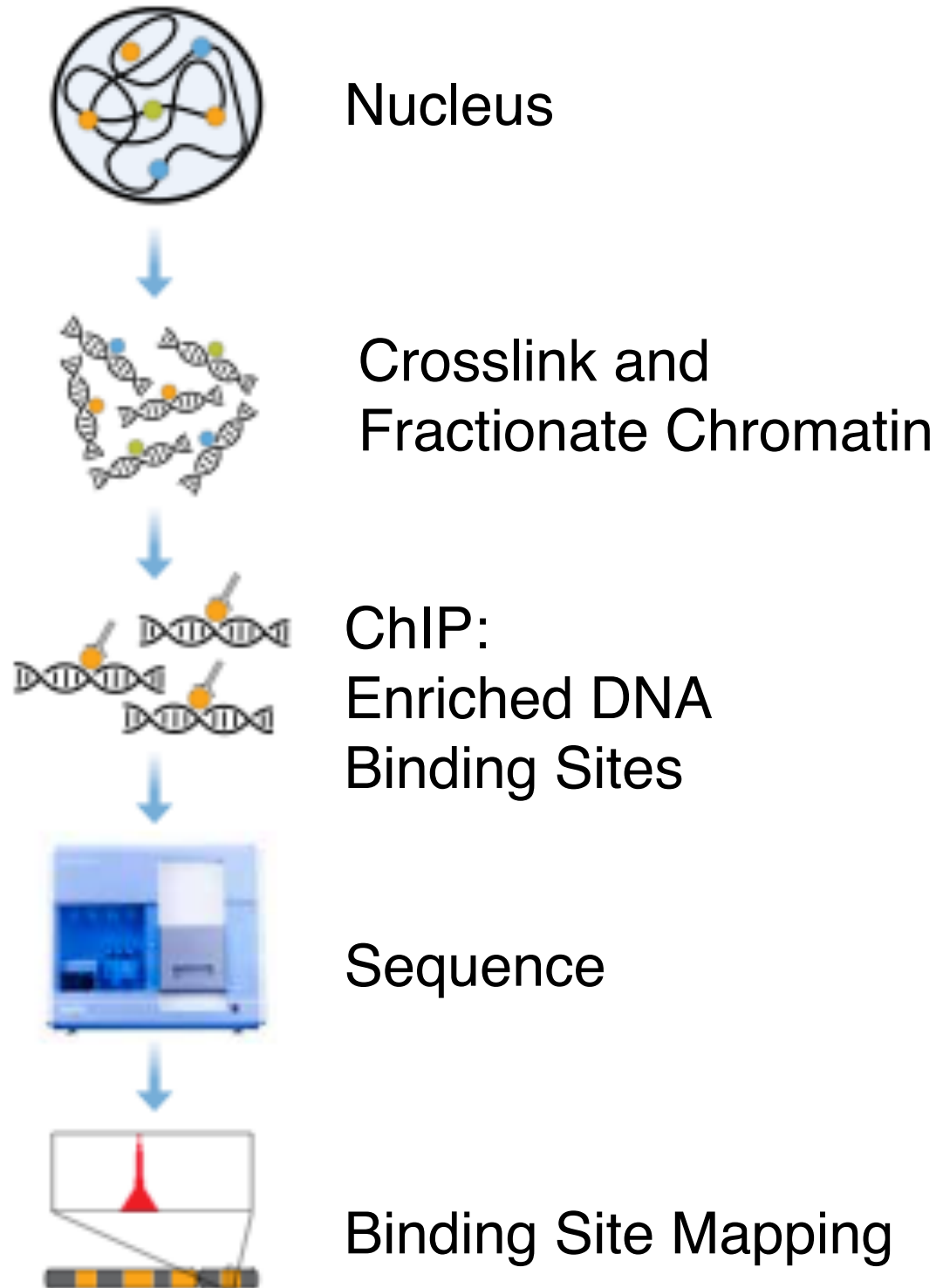
Lipidomics

- lipids
- metabolic signaling
- energy storage
- cell proliferation
- cell migration
- apoptosis
- cellular membrane

Interactions

Whole-Genome Chromatin IP Sequencing (ChIP-Seq)

identify binding
sites of DNA-
associated proteins



Interactions

Protein Arrays

Peptide Array

Bead Methods

Two Hybrid Methods

Many more!

Practical Issues

Not quantitative enough

Expensive enough

Inconclusive

Not exhaustive

Not dynamic

Systems Biology

- **Applications**
 - Genotype to Phenotype
 - In-silico Cell
 - Physiological Models
 - Personalized Precise and Predictive Medicine

Modeling

What's new?

- Technological Advancements (e.g. mass spectrometry/sequencing/imaging).
- High Performance Computing
- Information Storage abilities
- Information sharing abilities

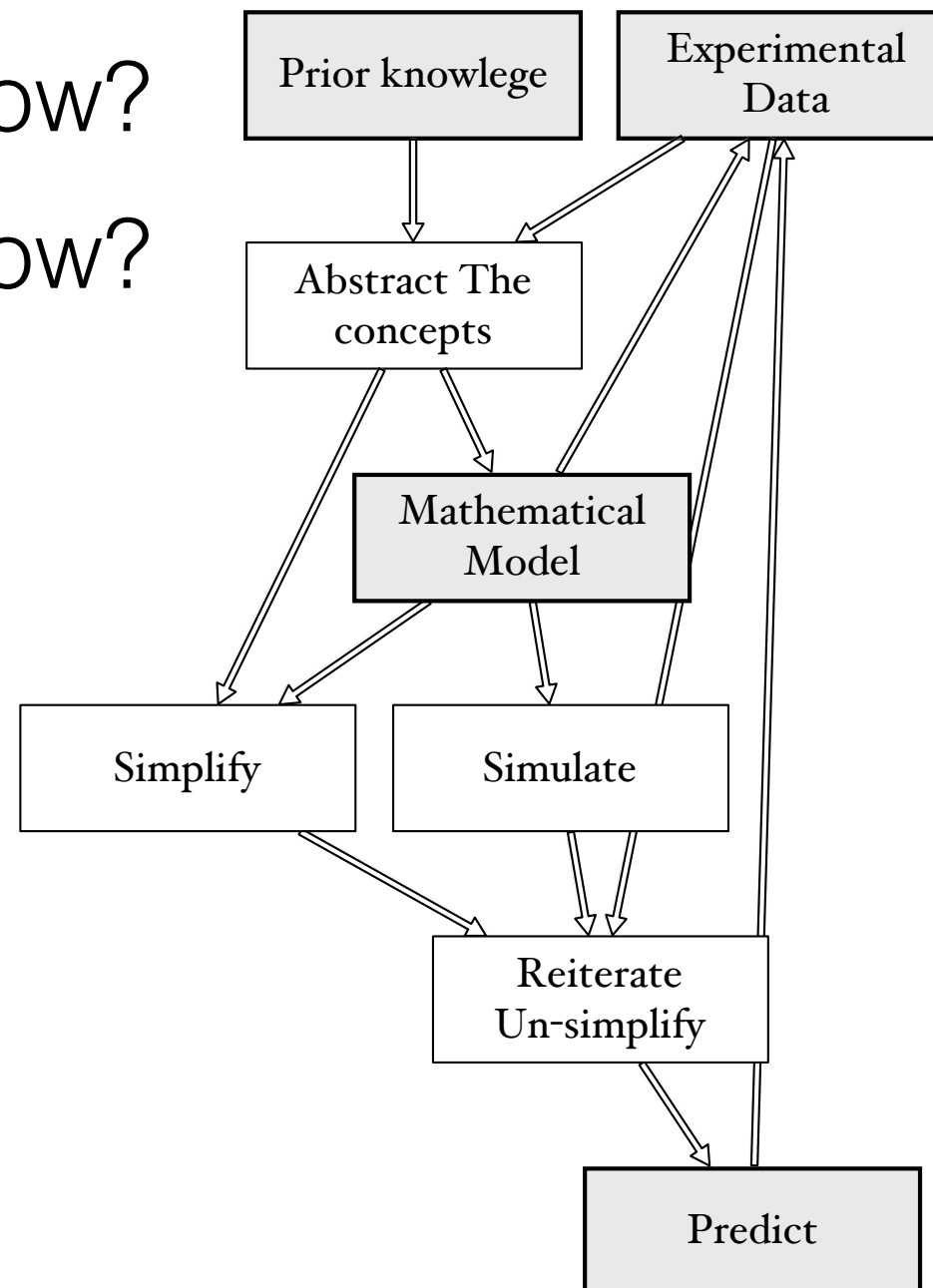
How to approach it

What is the question?

42

What do we know?

What can we know?

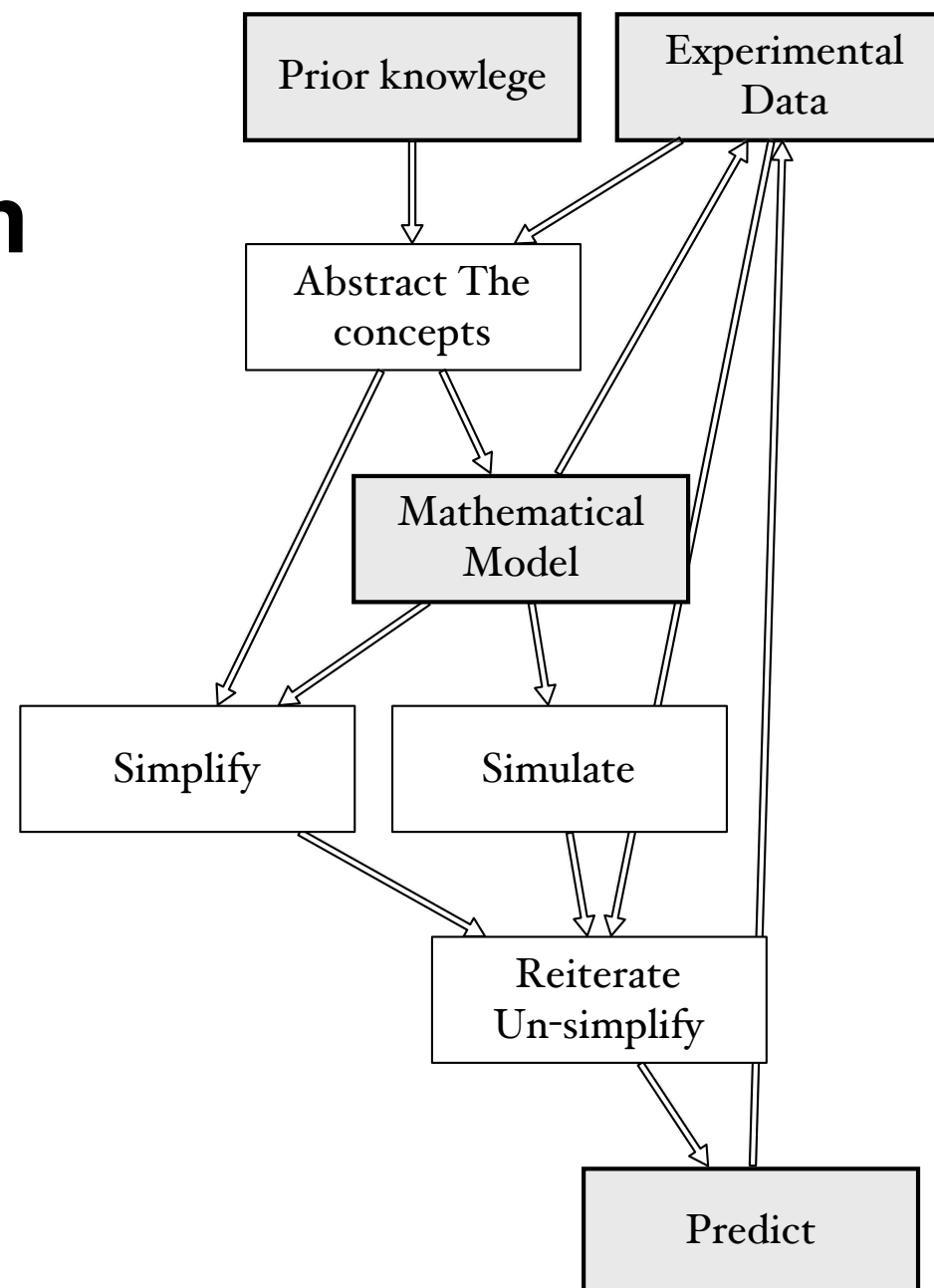


How to approach it

42

Underlying system

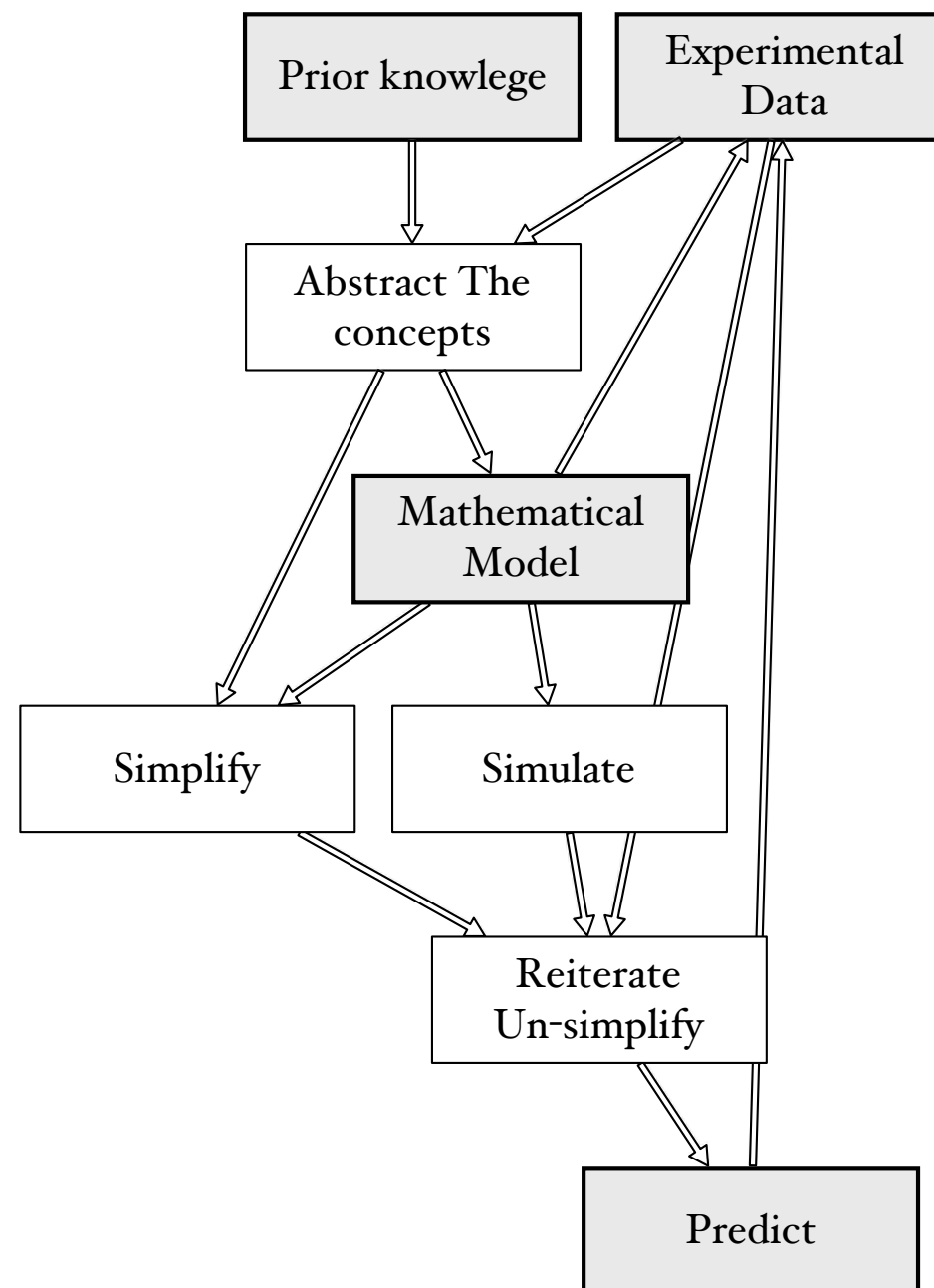
- characteristics
- responses
- interactions



How to approach it

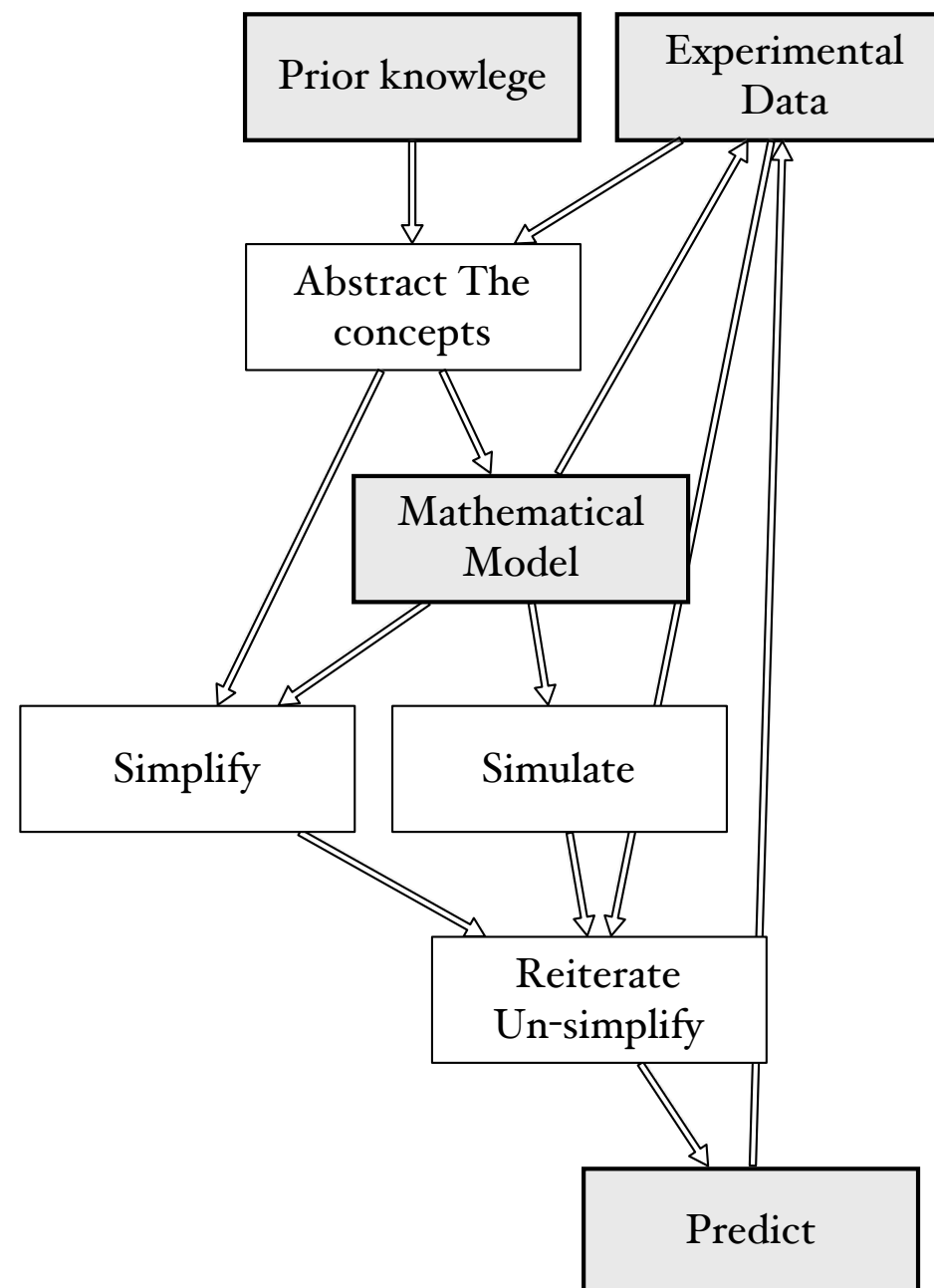
Pick your model (Based on system)

- atomic level
- cells
- molecular components
- dynamic Vs. Static
- How much to coarse grain?
- How many parameters?



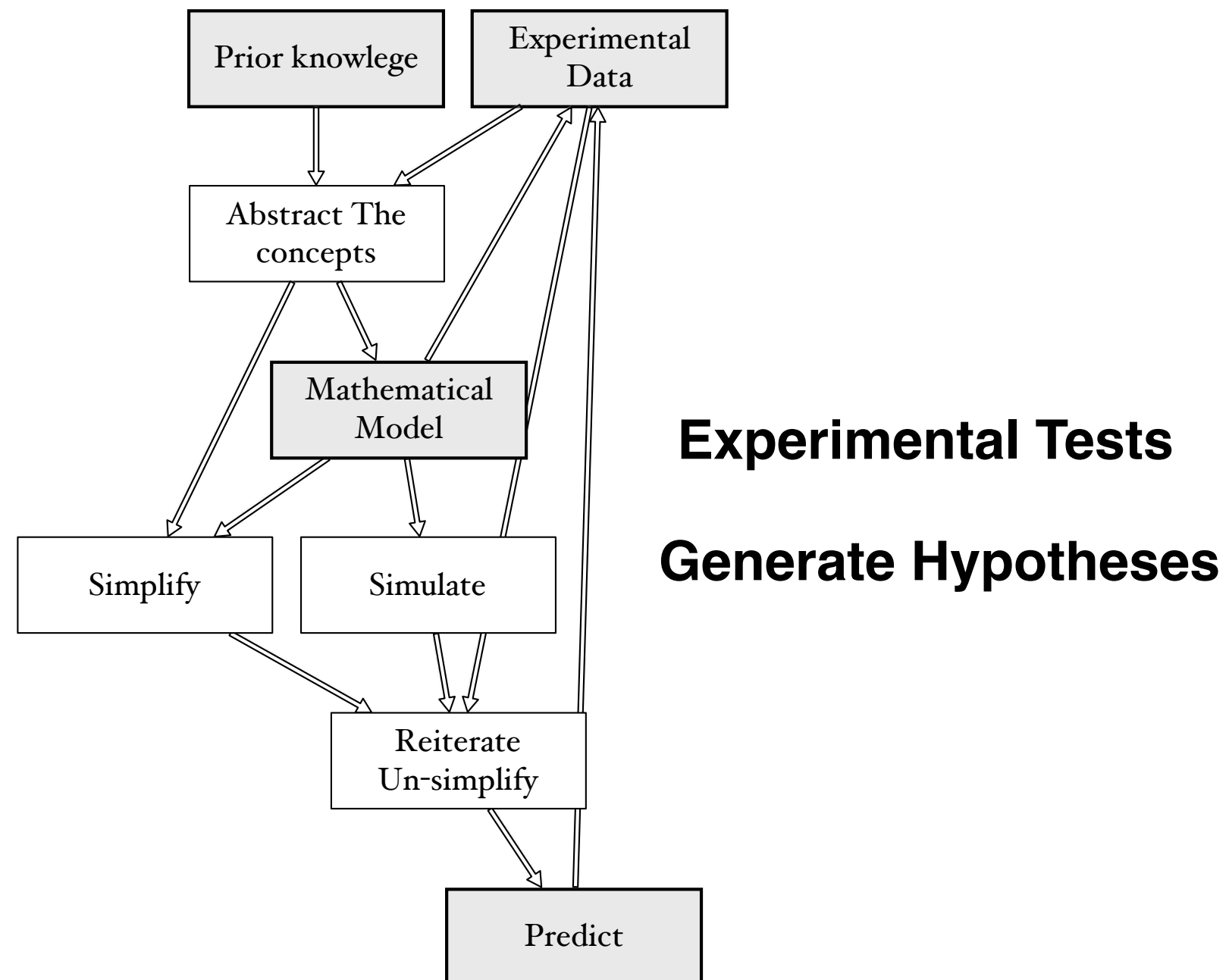
How to approach it

- Interactions and Networks
- Assumptions
- New knowledge required
- Storage of information



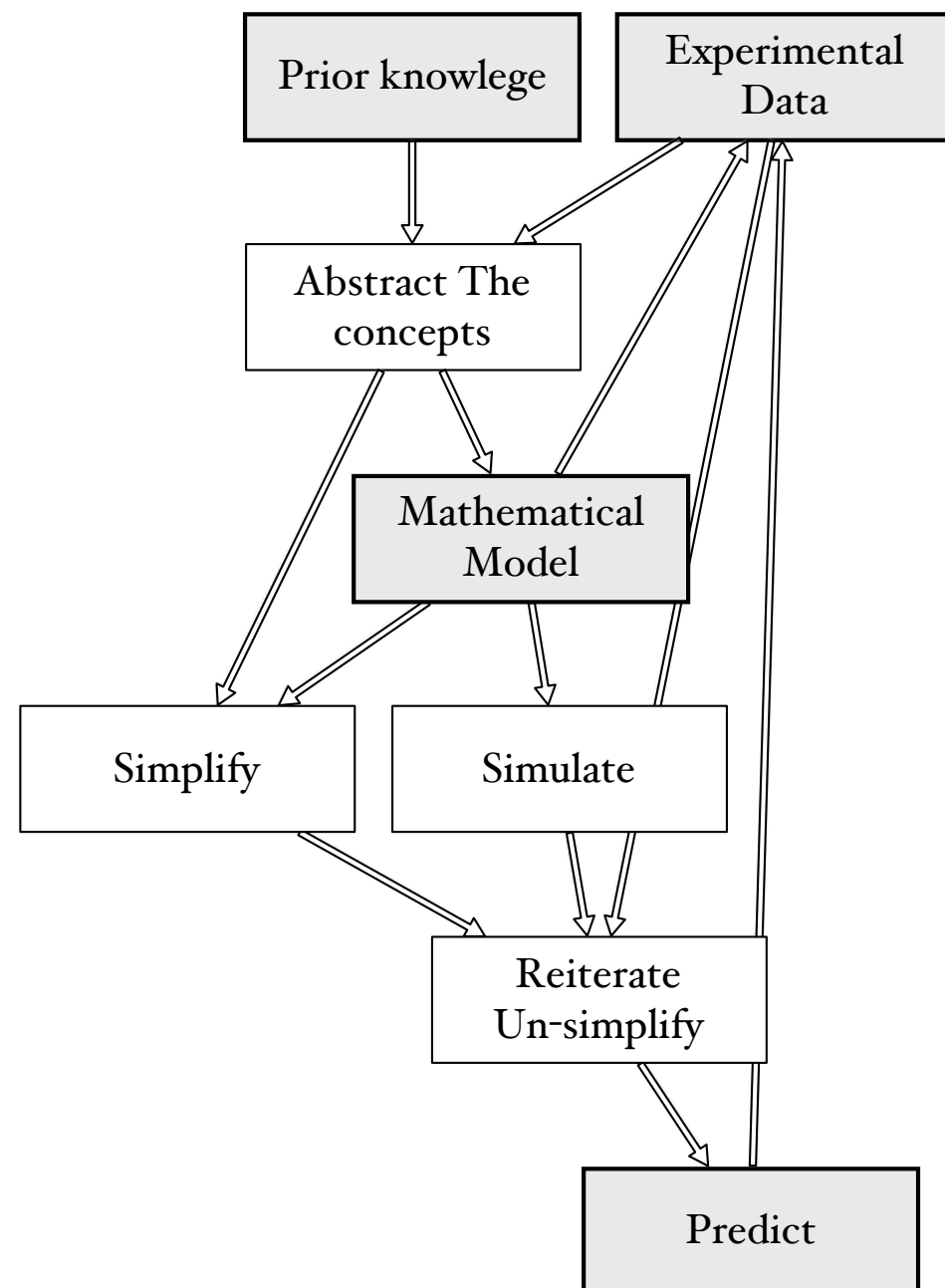
How to approach it

- Interactions and Networks
- Assumptions
- New knowledge required
- Storage of information



How to approach it

- Interactions and Networks
- Assumptions
- New knowledge required
- Storage of information



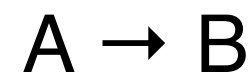
Validation
may invalidate
cannot confirm

Biochemical Models

Biochemical Models

Chemical Reactions

A transforms to B



- conversion
- modification
- dimerization

A associates with B to form C



- association
- synthesis

C dissociates to A and B

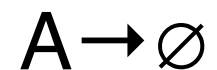


- dissociation
- decomposition

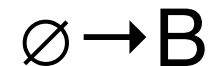
Biochemical Models

Chemical Reactions

null species (e.g. constant abundance)



- degradation



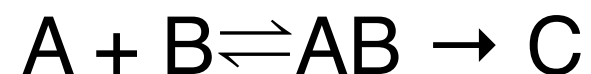
- production
- discarded reactants

Elementary Irreversible Reactions

- Single step
- one direction

Chemical Reactions

Can put it all together: e.g.

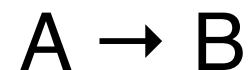


- $\rightleftharpoons$ • 2 elementary reactions
- C covalent modification of AB

Biochemical Models

Chemical Reactions

A transforms to B



$$\text{Reaction Rate} = k [A]$$

mass action

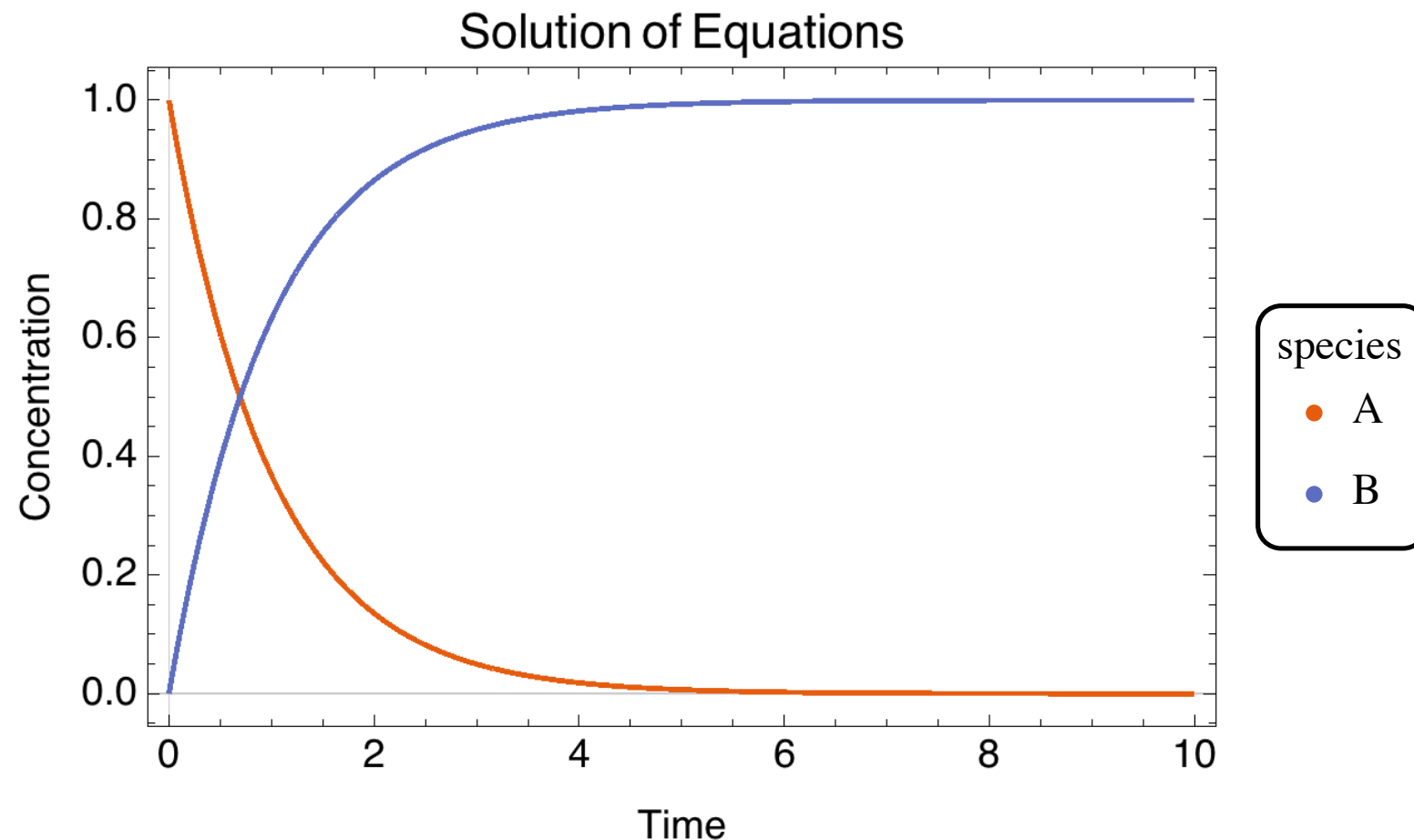
Rate of changes proportional to concentration

$$\frac{d[A]}{dt} = -k(A); \frac{d[B]}{dt} = k(A)$$

Biochemical Models

Chemical Reactions

A transforms to B $\frac{d[A]}{dt} = -k(A); \frac{d[B]}{dt} = k(A)$



Rate of changes proportional to concentration

Biochemical Models

Chemical Reactions

Chemical Reaction	Rate Equation for One Species
$A + B \rightarrow C$	$\frac{dc}{dt} = k_f ab = k_f (a_0 - c)(b_0 - c)$
$2A \rightleftharpoons B$	$\frac{db}{dt} = k_f (a_0 - 2b)^2 - k_r b$
$A \rightleftharpoons 2B$	$\frac{db}{dt} = k_f (a_0 - \frac{b}{2}) - k_r b^2$
$A \rightleftharpoons B + C$	$\frac{dc}{dt} = k_f (a_0 - c) - k_r (b_0 + c)(c_0 + c)$
$A + B \rightleftharpoons C$	$\frac{dc}{dt} = k_f (a_0 - c)(b_0 - c) - k_r c$
$A + B \rightleftharpoons C + D$	$\frac{db}{dt} = k_f (a_0 - c)(b_0 - c) - k_r (c_0 + c)(d_0 + c)$

x_0 : initial concentration for x

Biochemical Models

Chemical Reactions

$$X_i(t) = \frac{N_i(t)}{\Omega}$$

X_i : ith species concentration

Ω : system size = $N_A \times \text{Volume}$

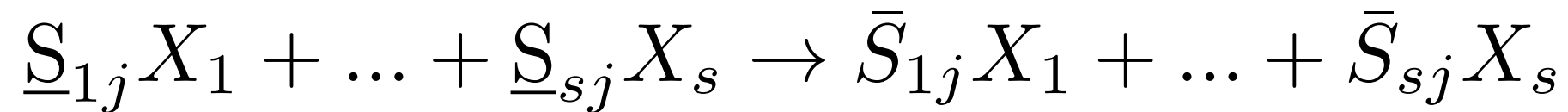
N_i : copy number

N_A : Avogadro's constant

Biochemical Models

Chemical Reactions

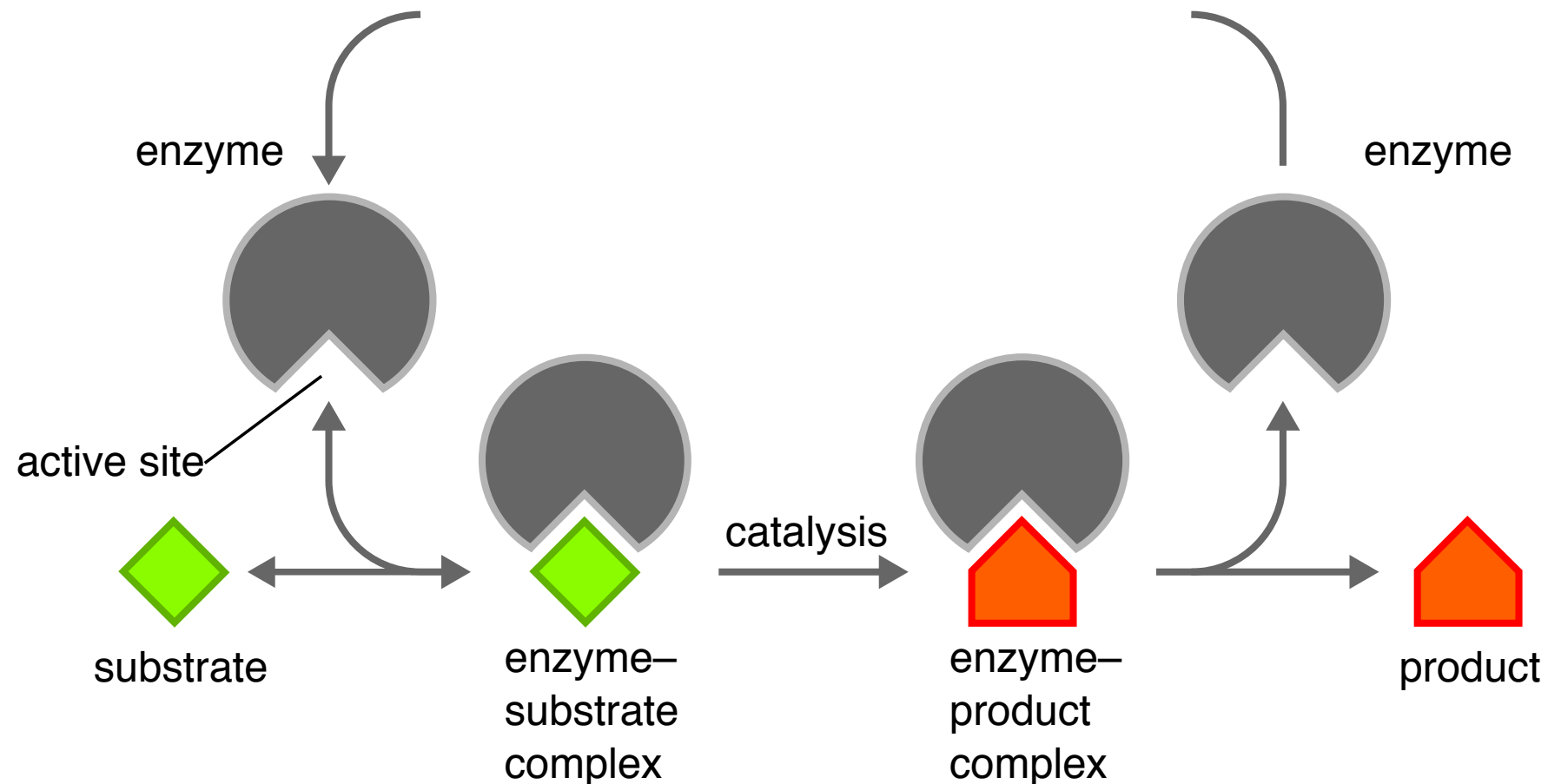
Reaction scheme R_j



S_{ij} stoichiometric coefficient indicates participation of X_i as a reactant

Biochemical Models

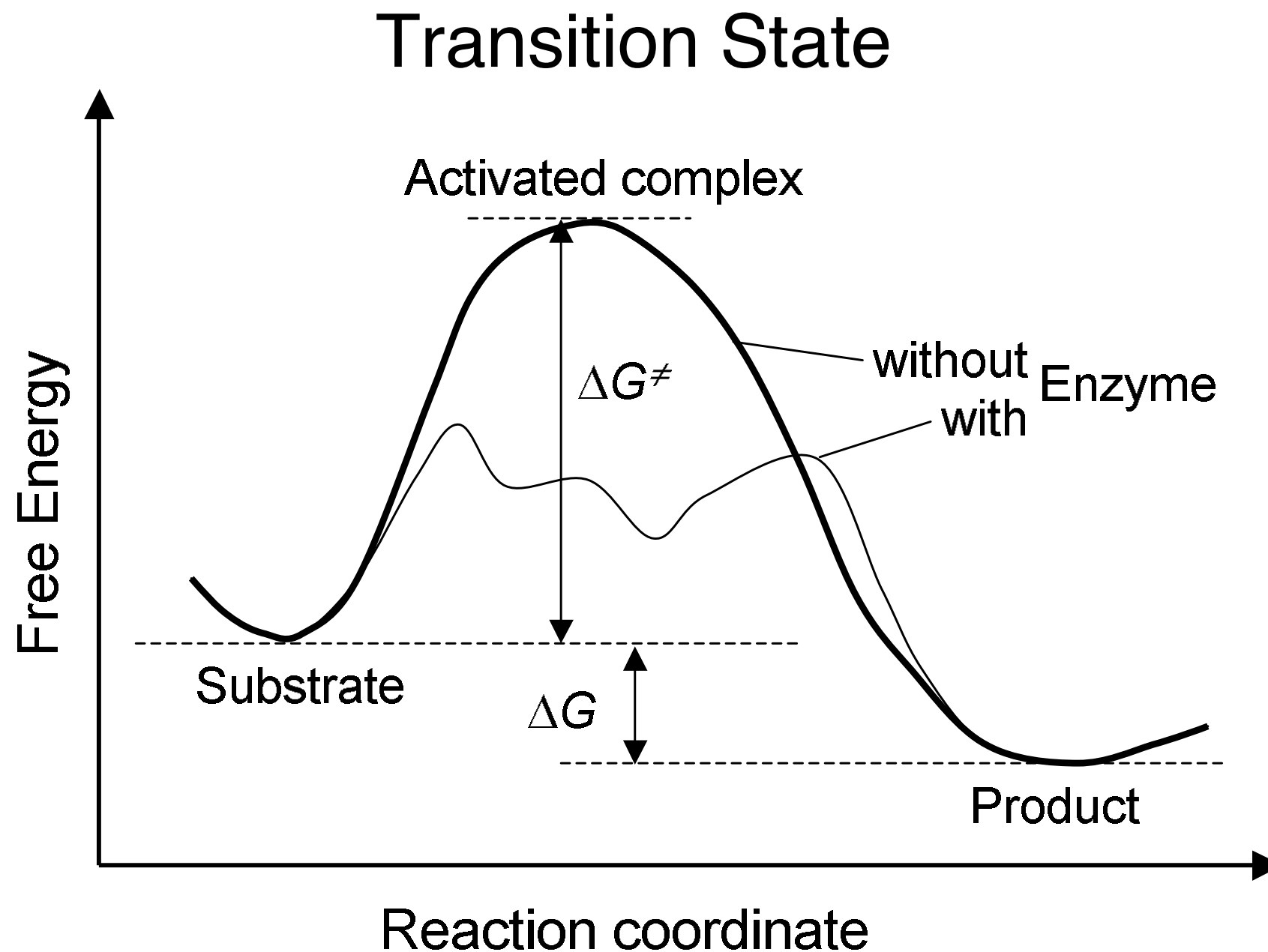
Chemical Reactions



energy

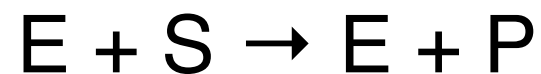
Enzyme Catalyzed Conversion of Substrate to Product

Biochemical Models



Biochemical Models

Chemical Reactions

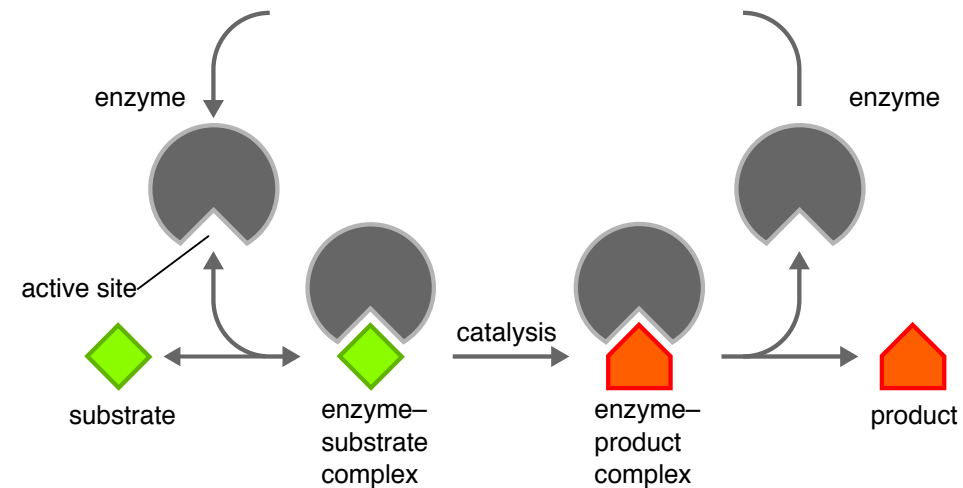


k_1



k_2

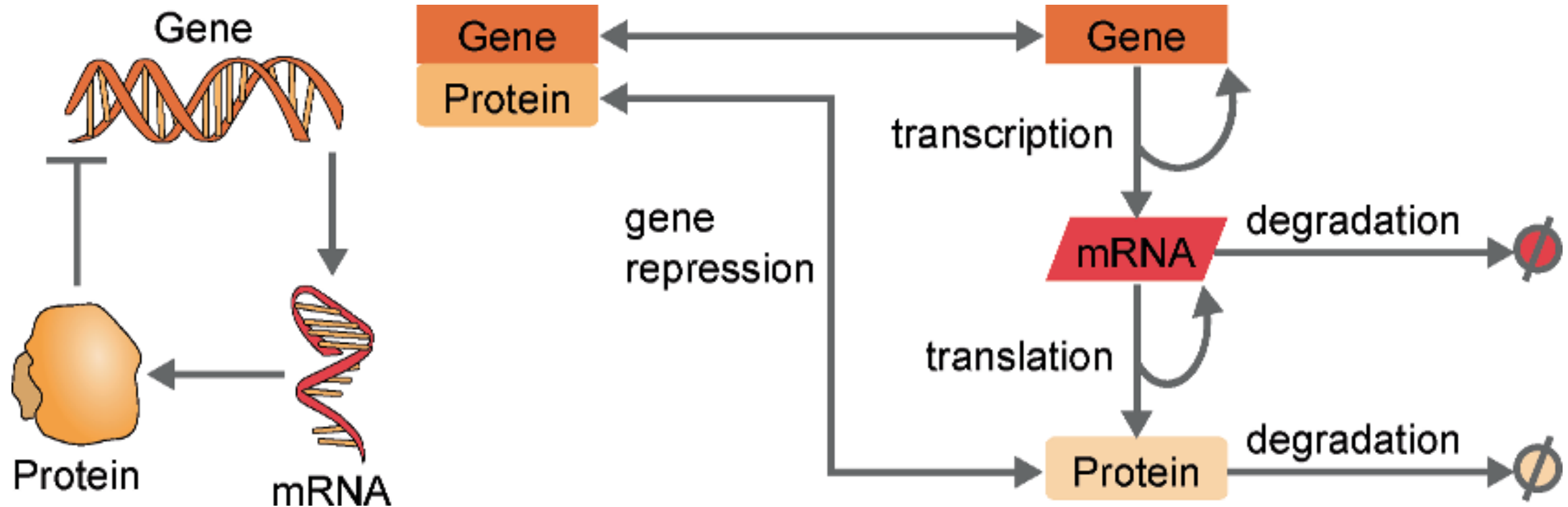
- 3 elementary reactions



- Can approximate to single step

Biochemical Models

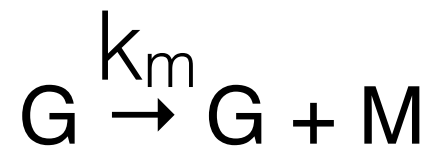
Simplified Gene Regulation



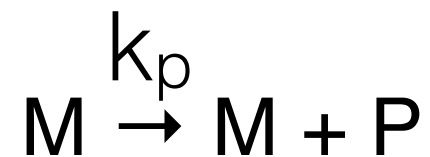
Biochemical Models

Simplified Gene Regulation

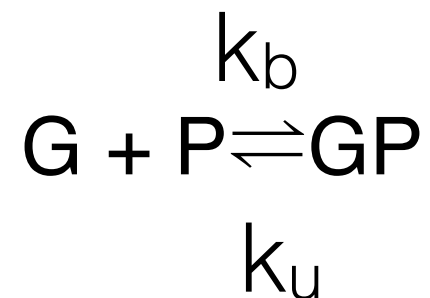
- Transcription



- Translation



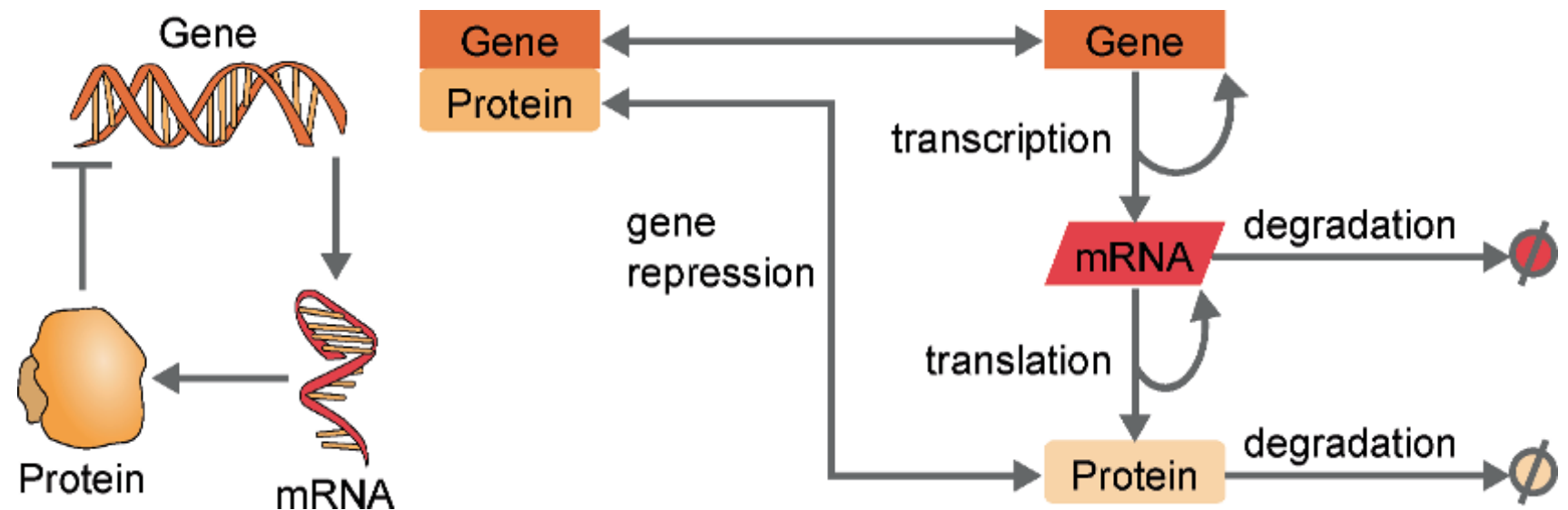
- Binding/unbinding



- Degradation



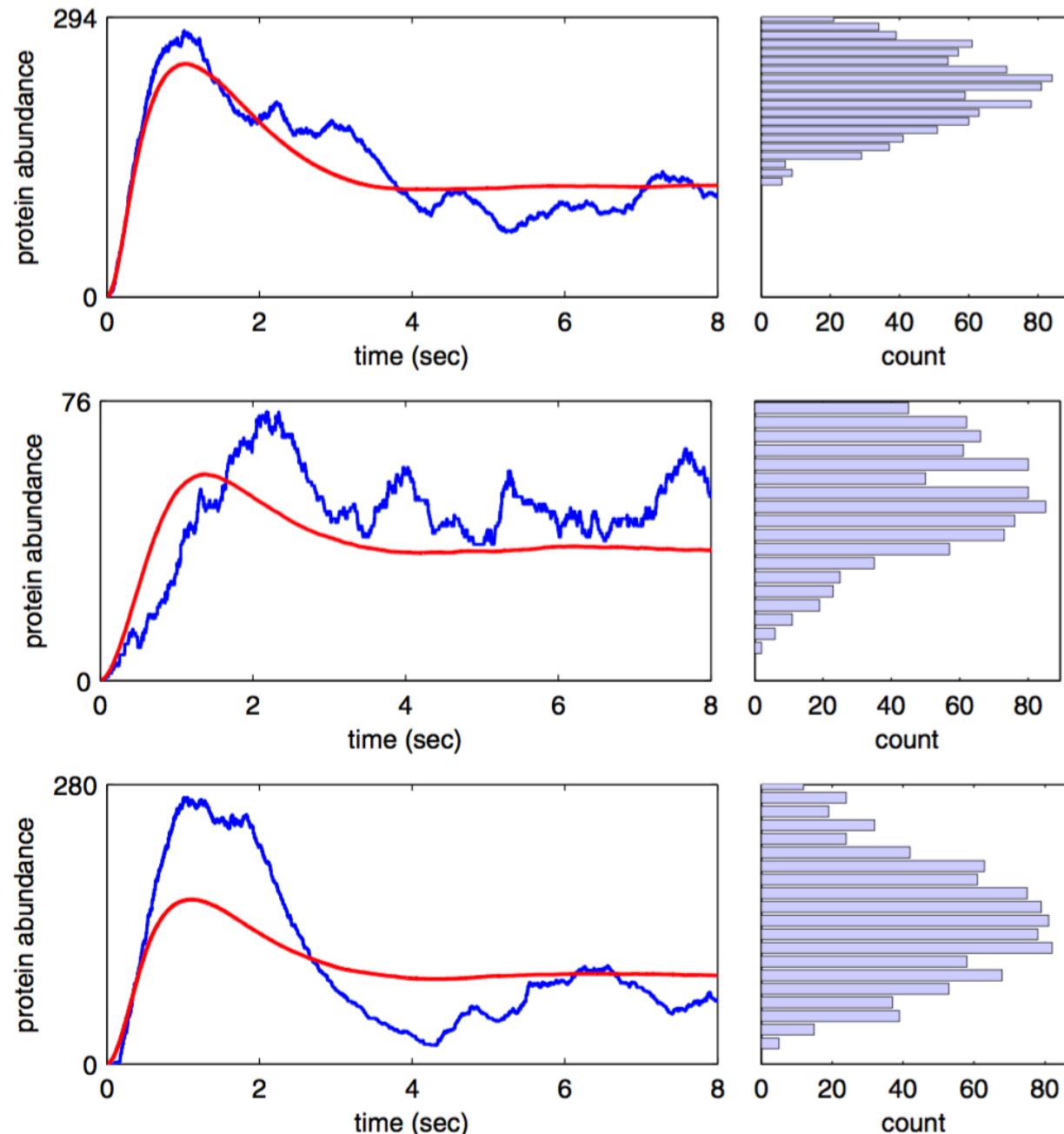
G: gene
M: mRNA
P: protein



Biochemical Models

Simplified Gene Regulation

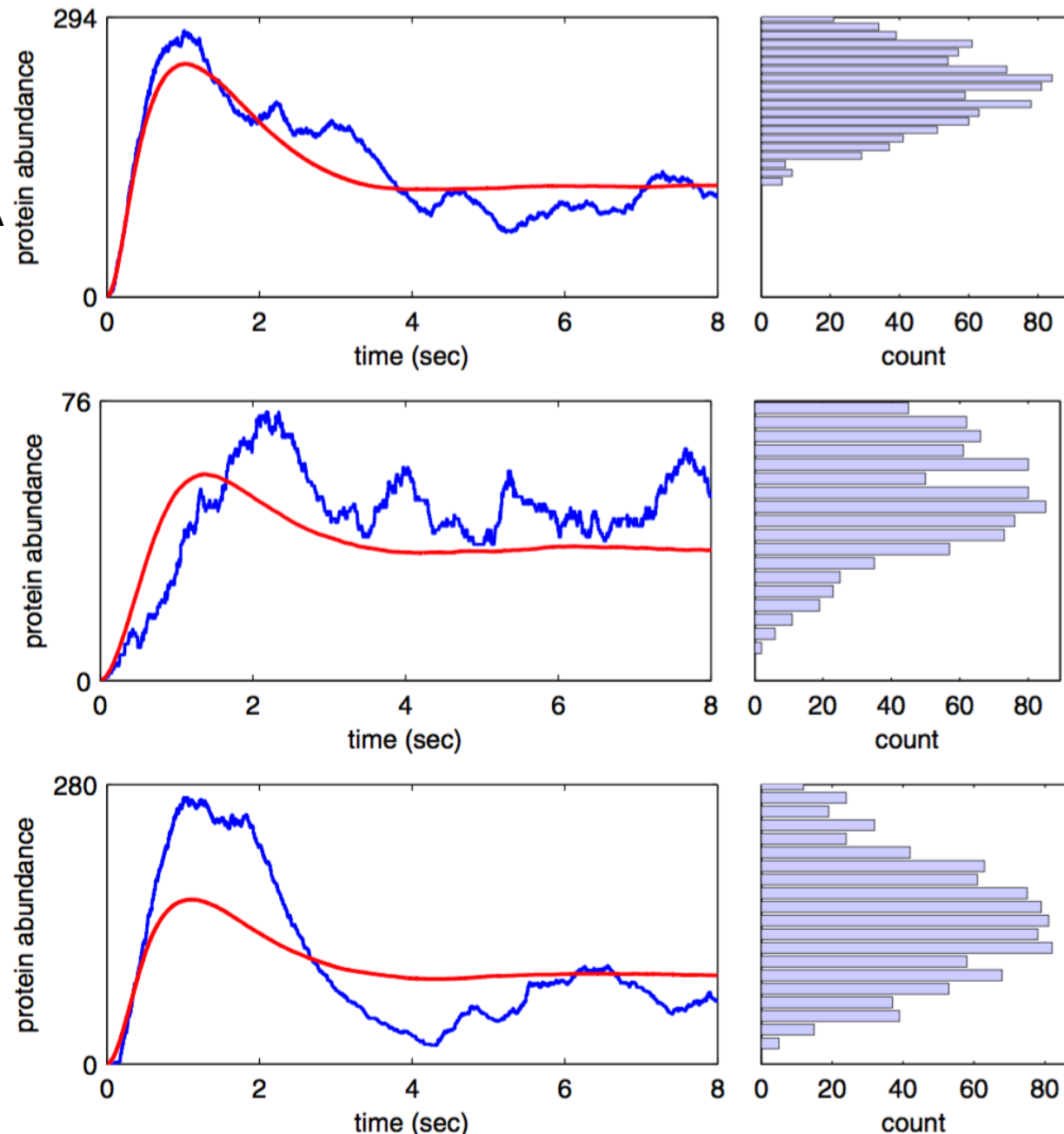
- Add stochasticity
- Time courses of a single stochastic simulation algorithm run (blue)
- Mean over 1000 runs (red curve).
- Initial conditions
 - ▶ 10 copies gene G
 - ▶ 0 copies of other species
- Endpoint histogram shows empirical probability that a cell will have a given protein abundance.



Biochemical Models

Simplified Gene Regulation

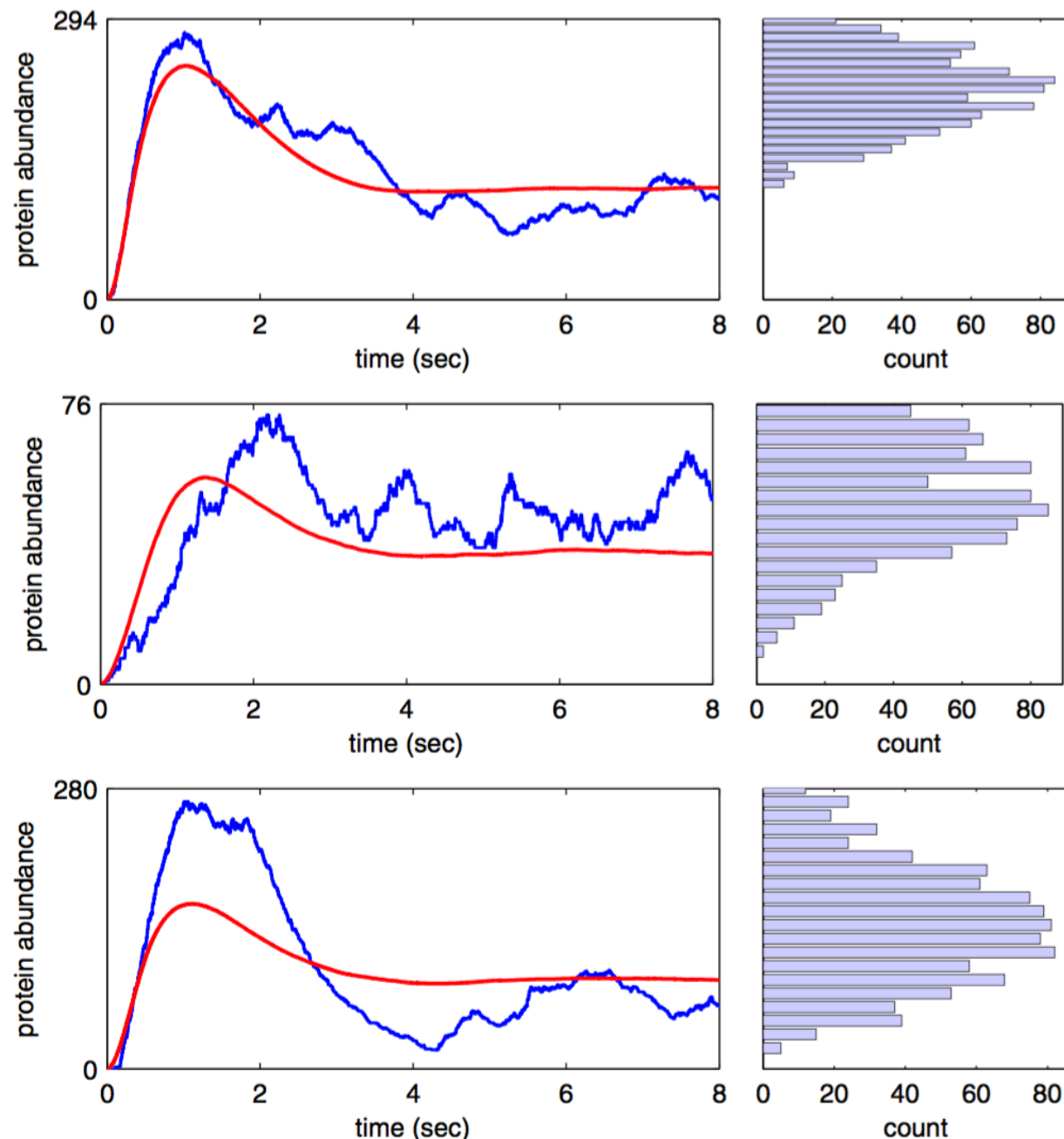
- Top: Small fluctuations with high copy numbers of expressed mRNA and protein.



Biochemical Models

Simplified Gene Regulation

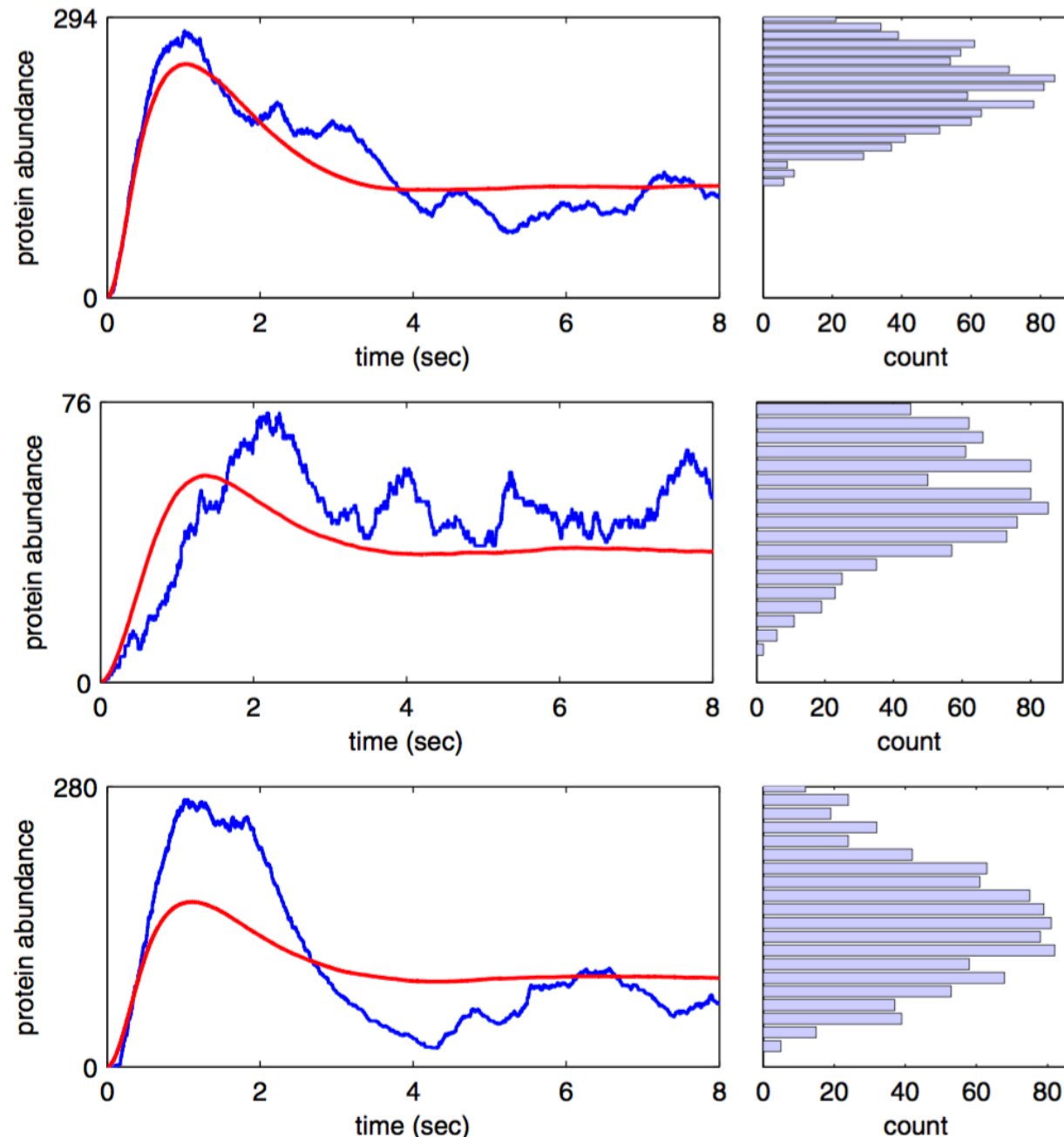
- Middle: A tenfold decrease in the transcription rate k_m leads to
 - ▶ Decrease in the expressed mRNA abundance
 - ▶ An associated decrease in protein abundance
 - ▶ Large fluctuations in the protein abundance.



Biochemical Models

Simplified Gene Regulation

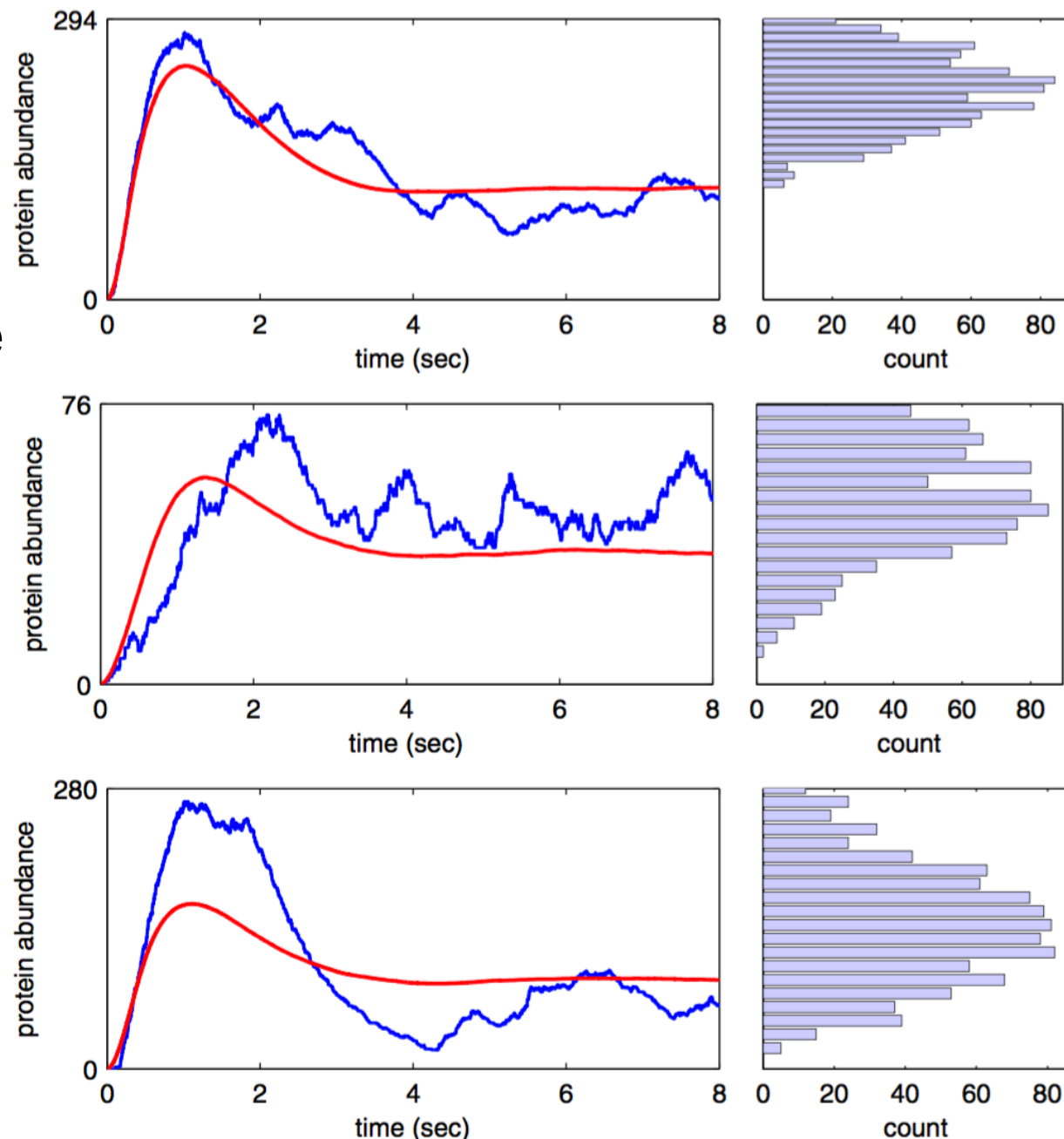
- Bottom: Fluctuations in mRNA abundance at the transcription level are a second important factor contributing to gene-expression noise.
 - ▶ Tenfold decrease rate of transcription
 - ▶ Rate of translation is increased fivefold to keep the protein abundance more or less the same as in the first case



Biochemical Models

Simplified Gene Regulation

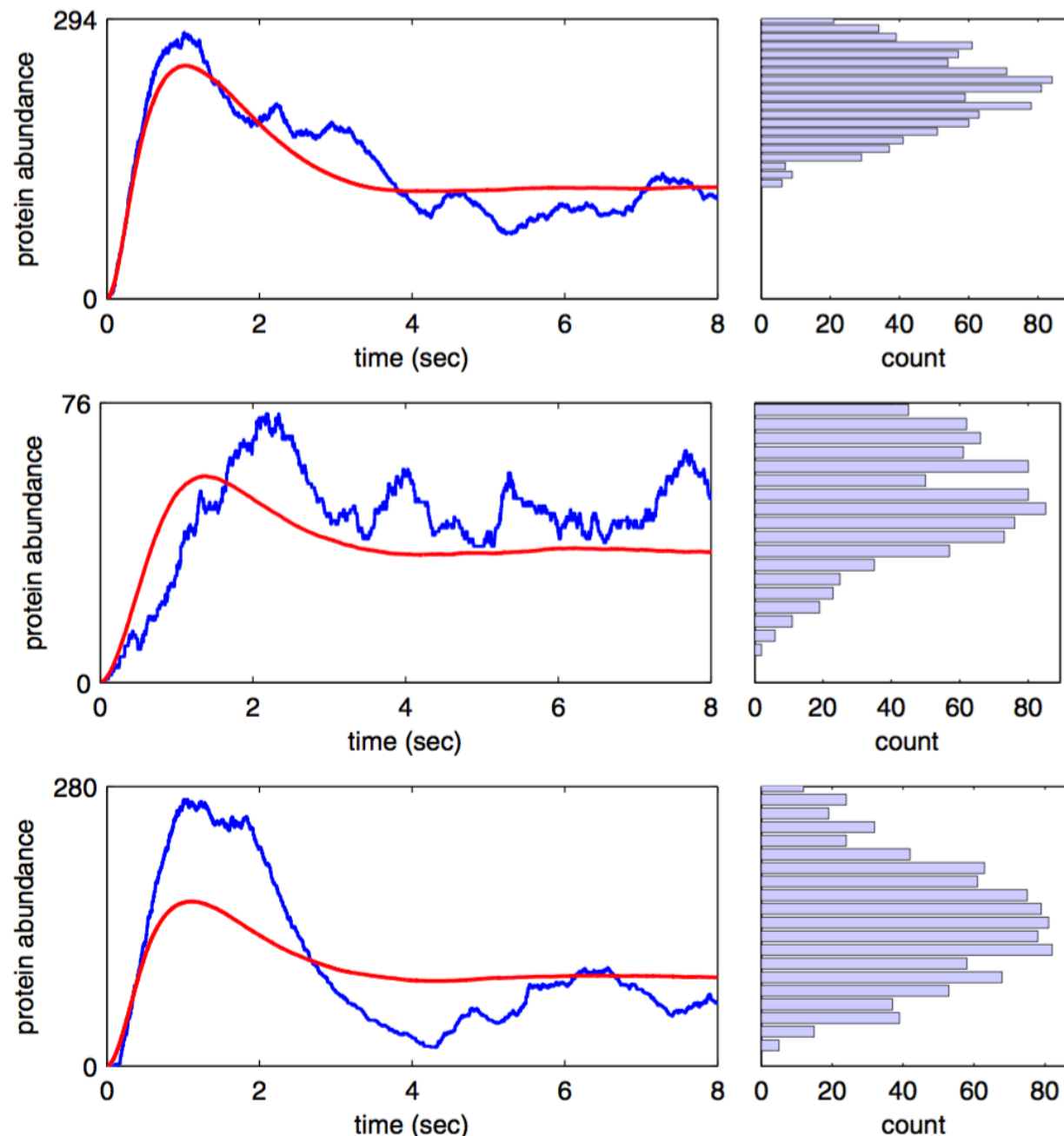
- Bottom:
 - ▶ increased gene-expression noise in spite of large protein abundance
 - ▶ Noise attributable to increased fluctuations in mRNA abundance
 - Causing increased fluctuations in the rate of protein synthesis.



Biochemical Models

Simplified Gene Regulation

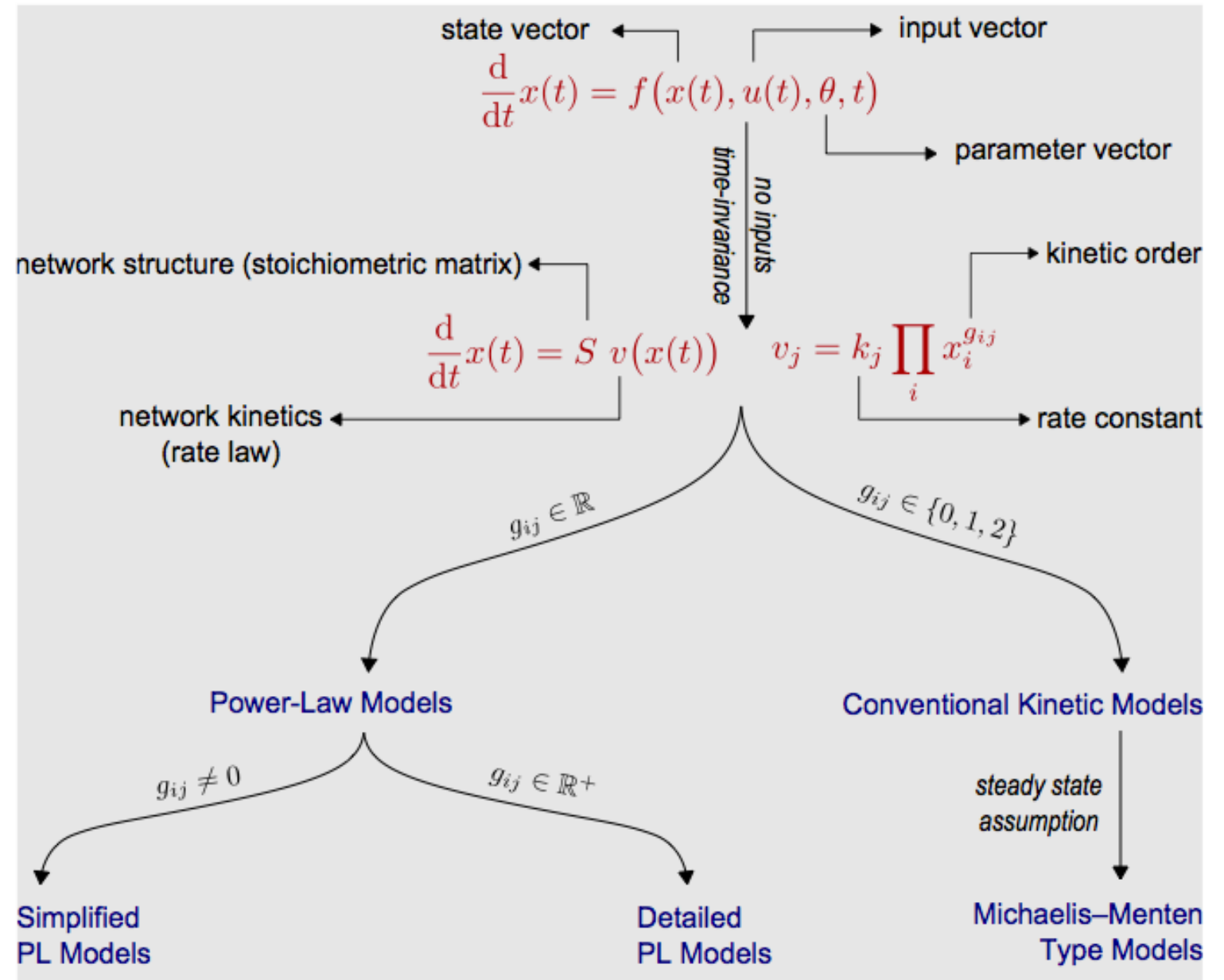
- **Noise is propagated from transcription to translation.**



Deterministic Models

Chemical Reaction Networks

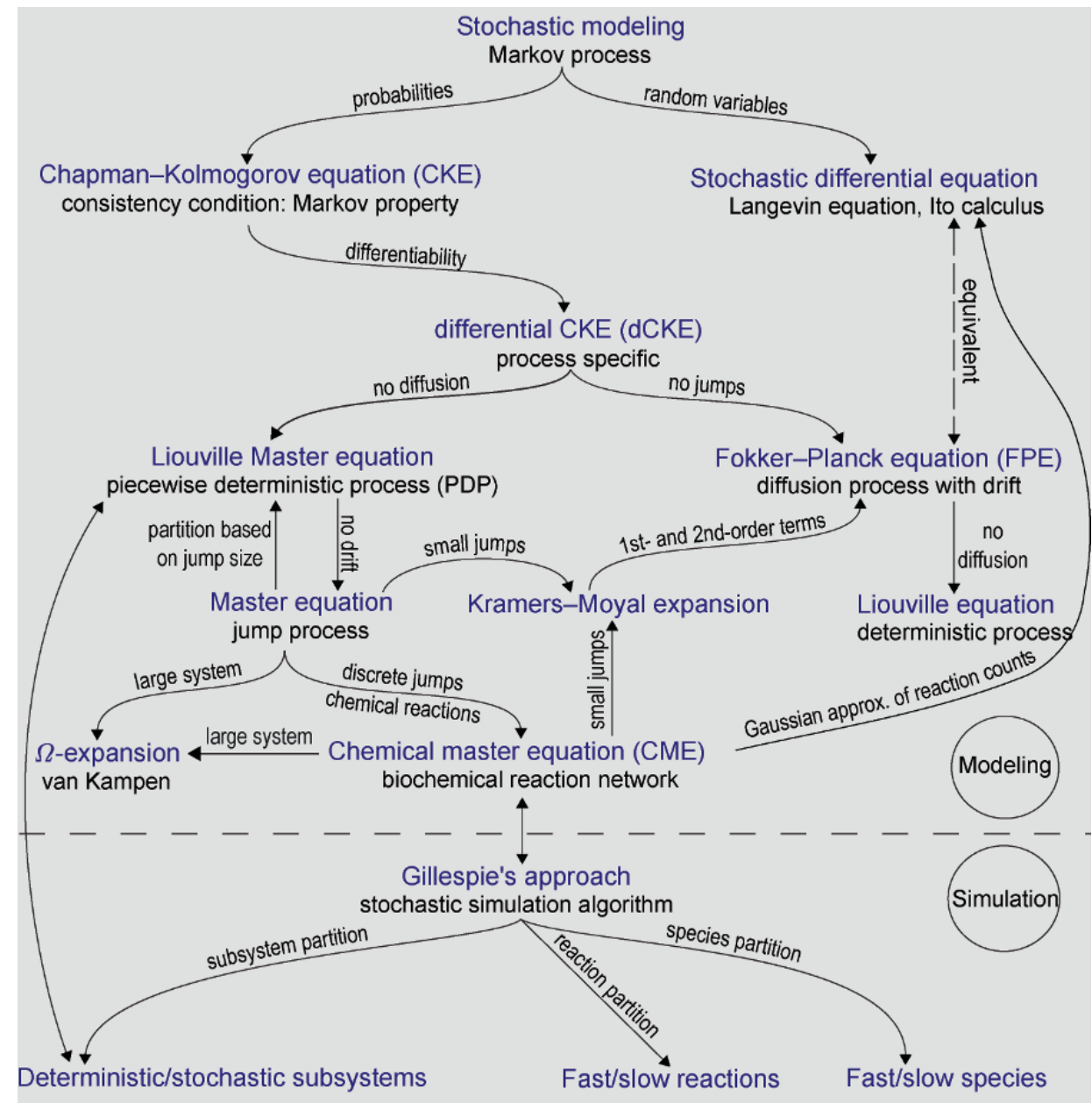
- Differential Equations
 - Stoichiometry matrix
 - (network structure)
- rate law
 - kinetics
 - collision theory
 - transition state theory



Stochastic Models

Chemical Reaction Networks

- Stochastic
 - statistical
 - fluctuations
 - noise



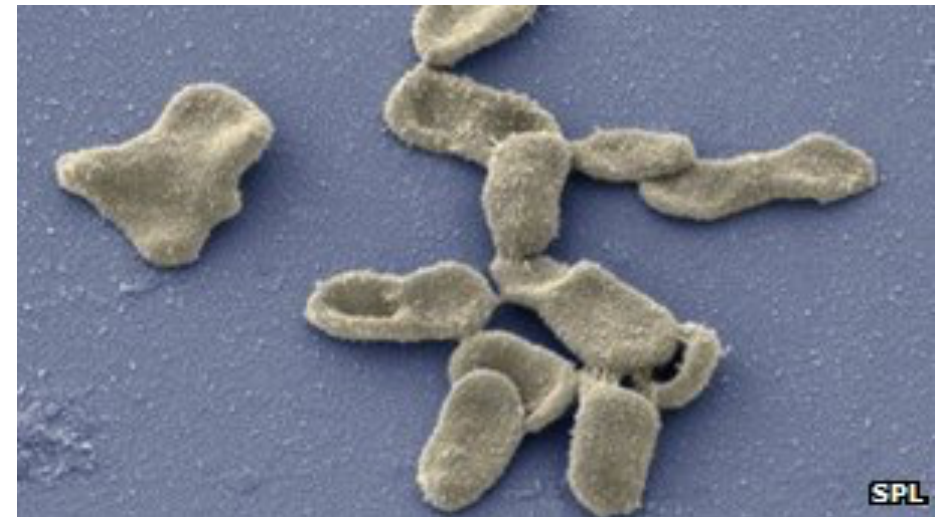
Example: Whole Cell Model

- *Mycoplasma genitalium*

parasitic bacterium

synthetic genome 2008 (J. Craig Venter Institute)

- 525 Genes
- 580.07 kb pairs
- 2nd smallest

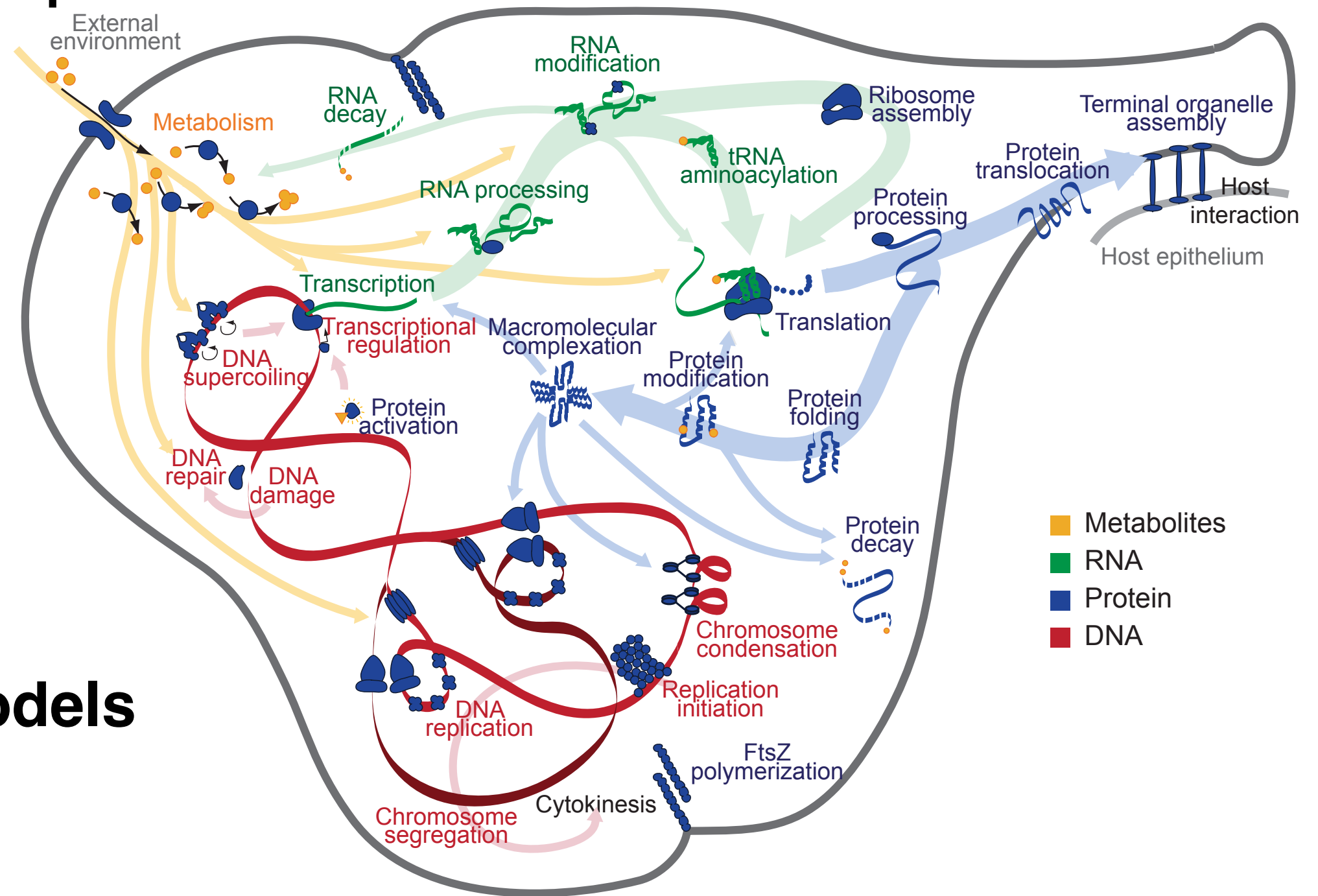


(left) Tully et al, International Journal of Systematic Bacteriology 33 (2): 387 (1983).

(right) <http://www.bbc.com/news/science-environment-19016772>

The virtual cell that simulates life

Example: Whole Cell Model

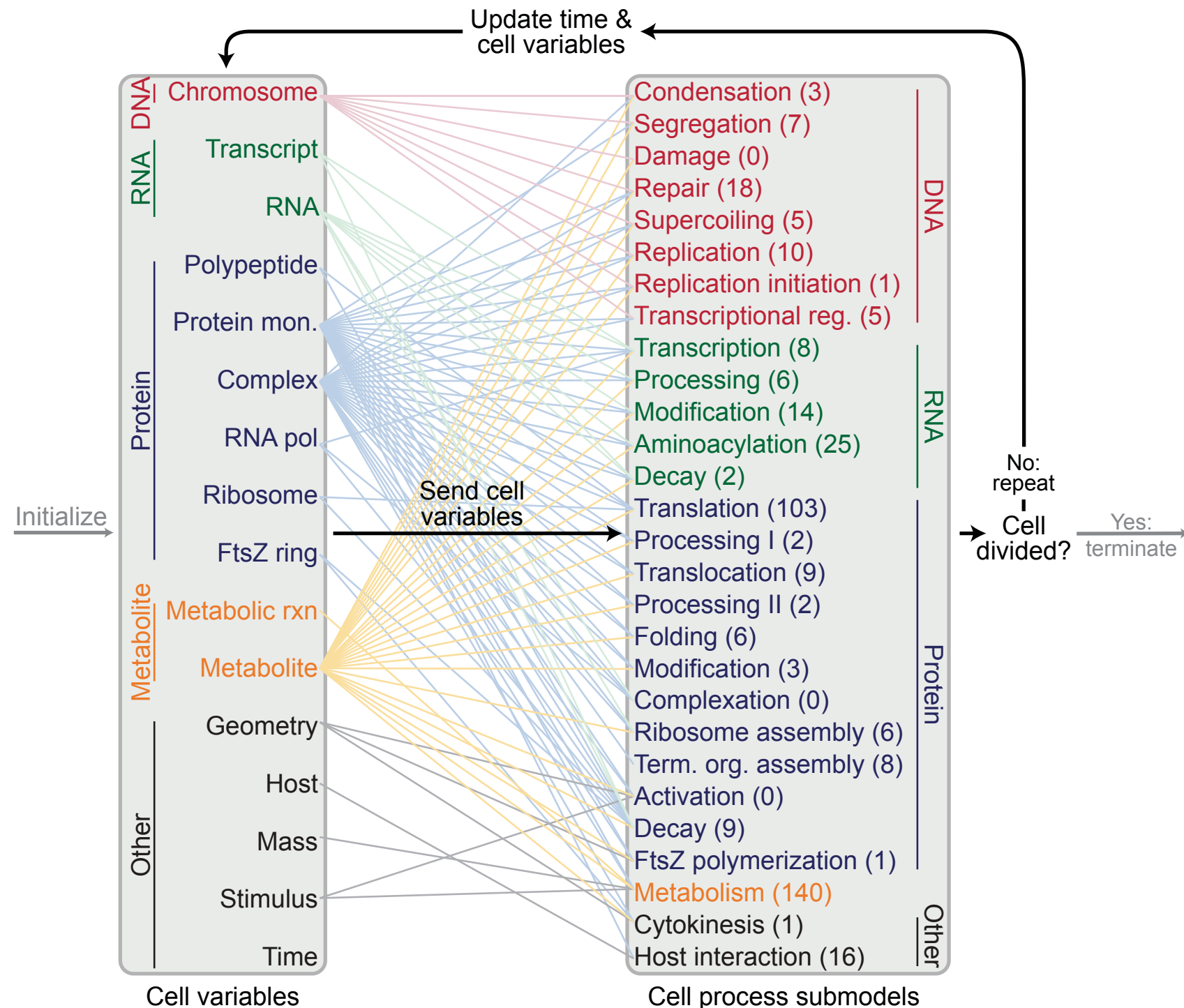


28 Submodels

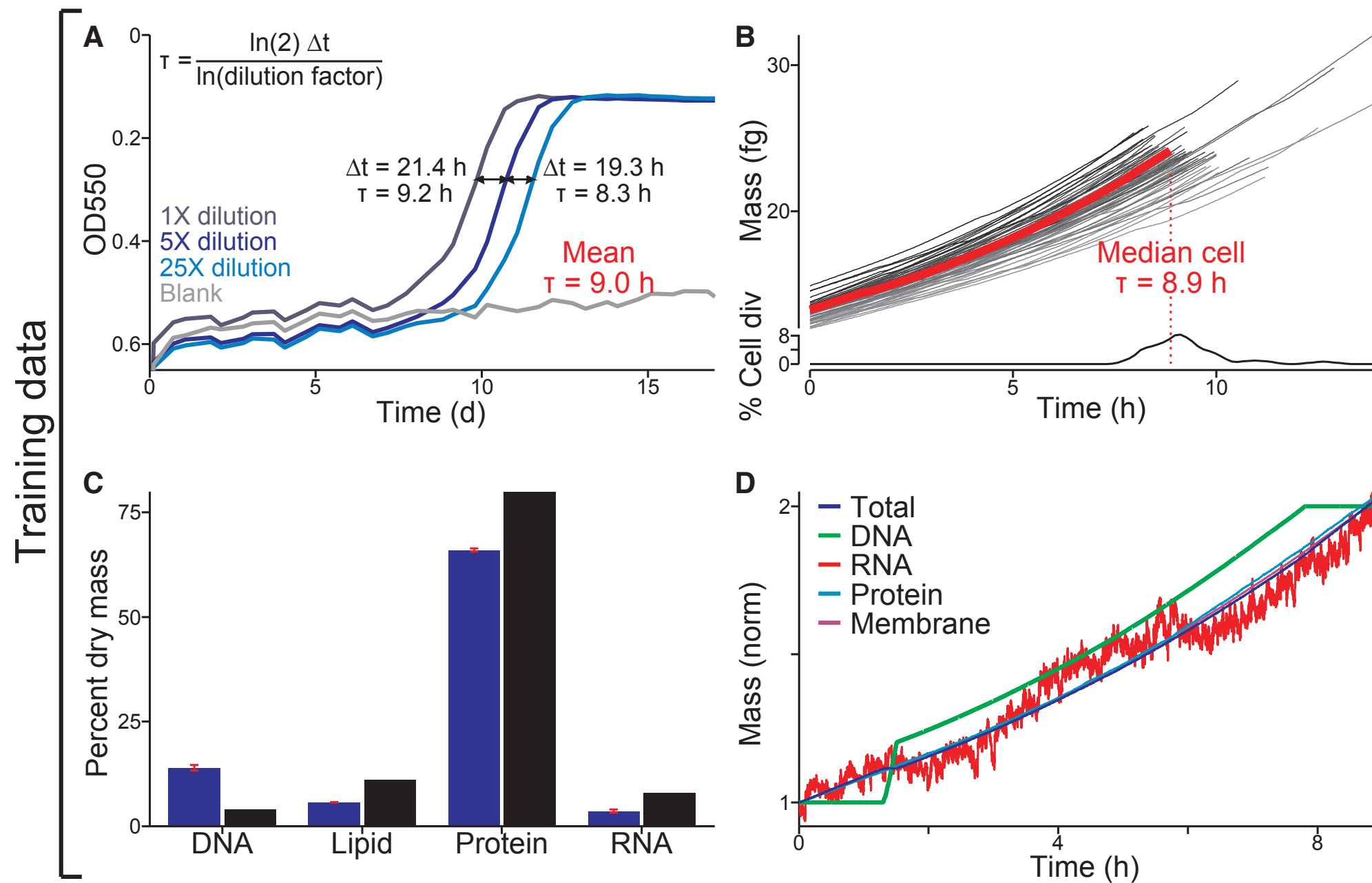
Example: Whole Cell Model

16 Variables

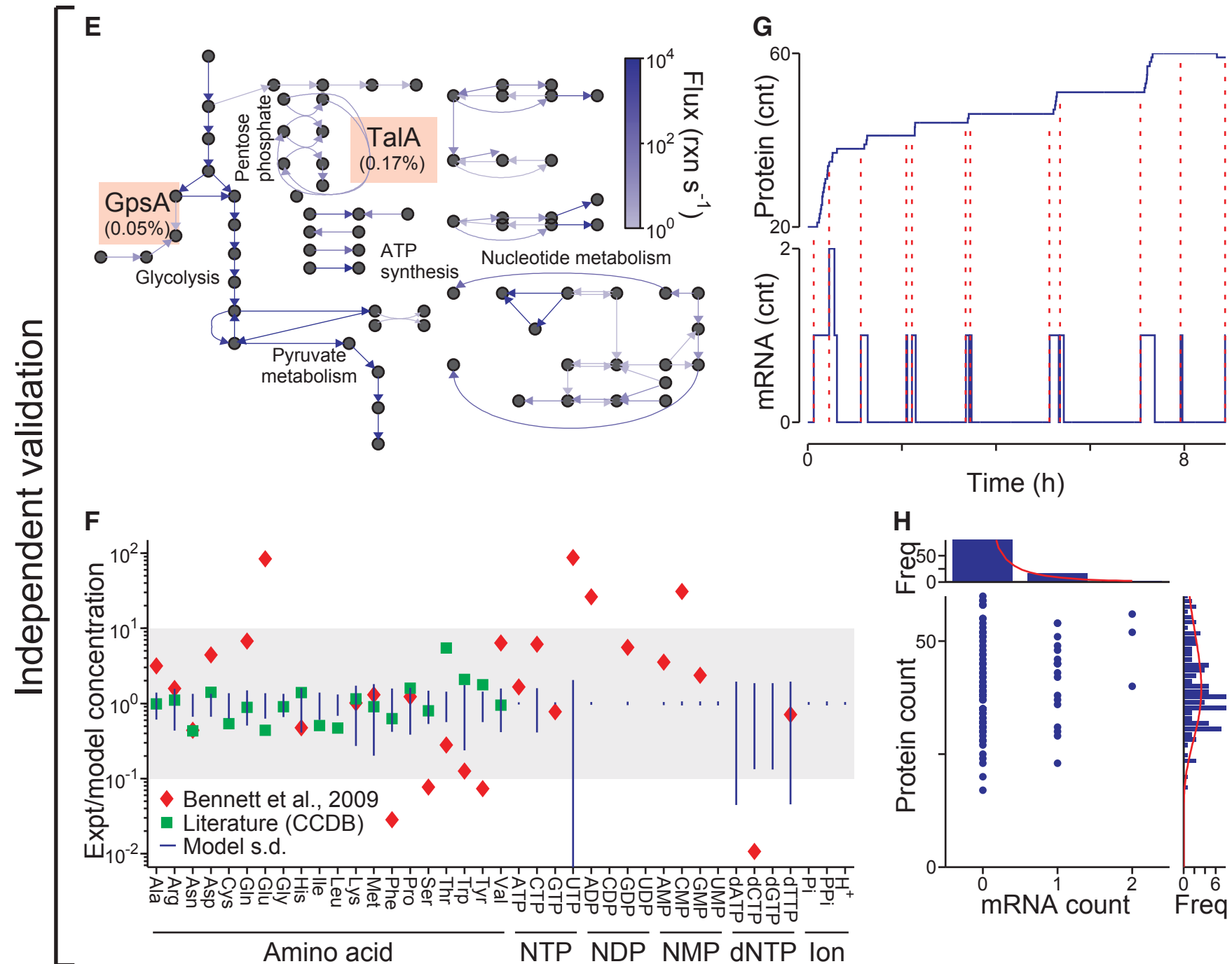
- Random initialize
- 1s time step
- Repeat
- Terminate on cell division



Example: Whole Cell Model



Example: Whole Cell Model



Math tools

- Exploratory data analysis and Data Mining
 - Statistics
 - Distributions
 - Correlations
 - Clustering/Visualization
 - Dimensional Reductions
 - Principal Components Analysis
 - Neural Networks
 - Mathematics
 - Systems of differential Equations
- different parts require different models

Math tools



<http://www.r-project.org>



<http://www.mathworks.com/products/matlab/>



<https://www.gnu.org/software/octave/>



<http://www.wolfram.com/mathematica/>



<http://www.sagemath.org>

home made varieties

(not an exhaustive list)

Representation

- **Common languages**

- XML (extensible markup language)
 - `<tag attribute="value"> content </tag>`
 - SBML (Systems Biology Markup Language)
 - CellML
 - SED-ML (Simulation Experiment Description Markup Language)
- BioPAX (Biological Pathway Exchange - Resource Description Framework [RDF])

- **Databases**

- KEGG, Gene Ontology (GEO), WikiPathways, IPA, Reactome

- **Networks** (next)

- **Multi-model systems**

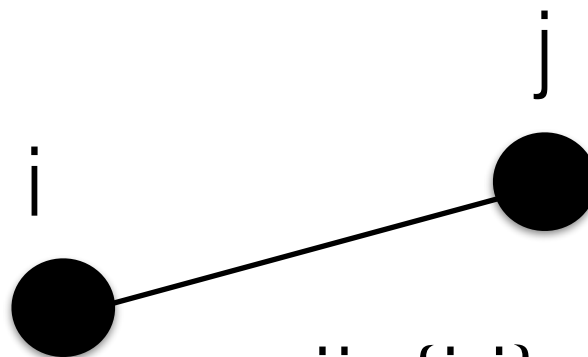
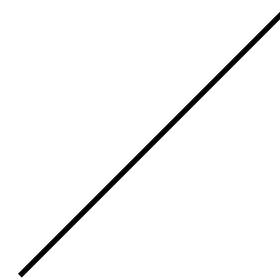
Networks & Pathways

Graphs

Vertices (nodes) $\{V\}$



Edges (links) $\{E\}$



$ij, \{i,j\}, \langle i,j \rangle, e_{ij},$

graph $G = (V, E)$

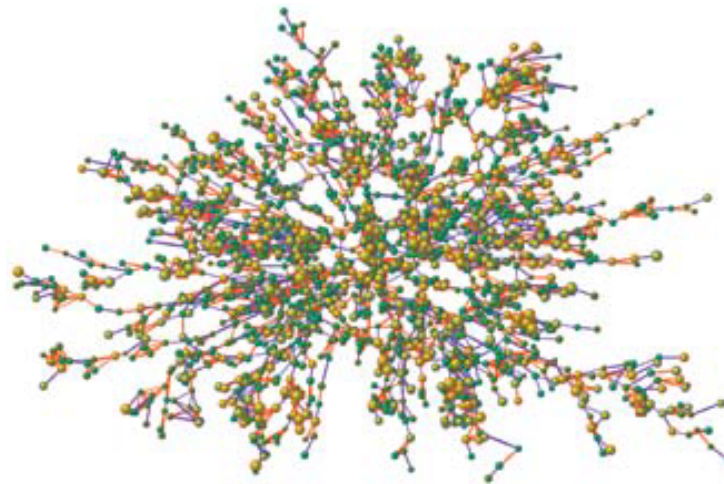
$V(G) = \{\text{set of vertices}\}$

$E(G) = \{\text{set of edges}\}$

Examples



Adult Human
Brain

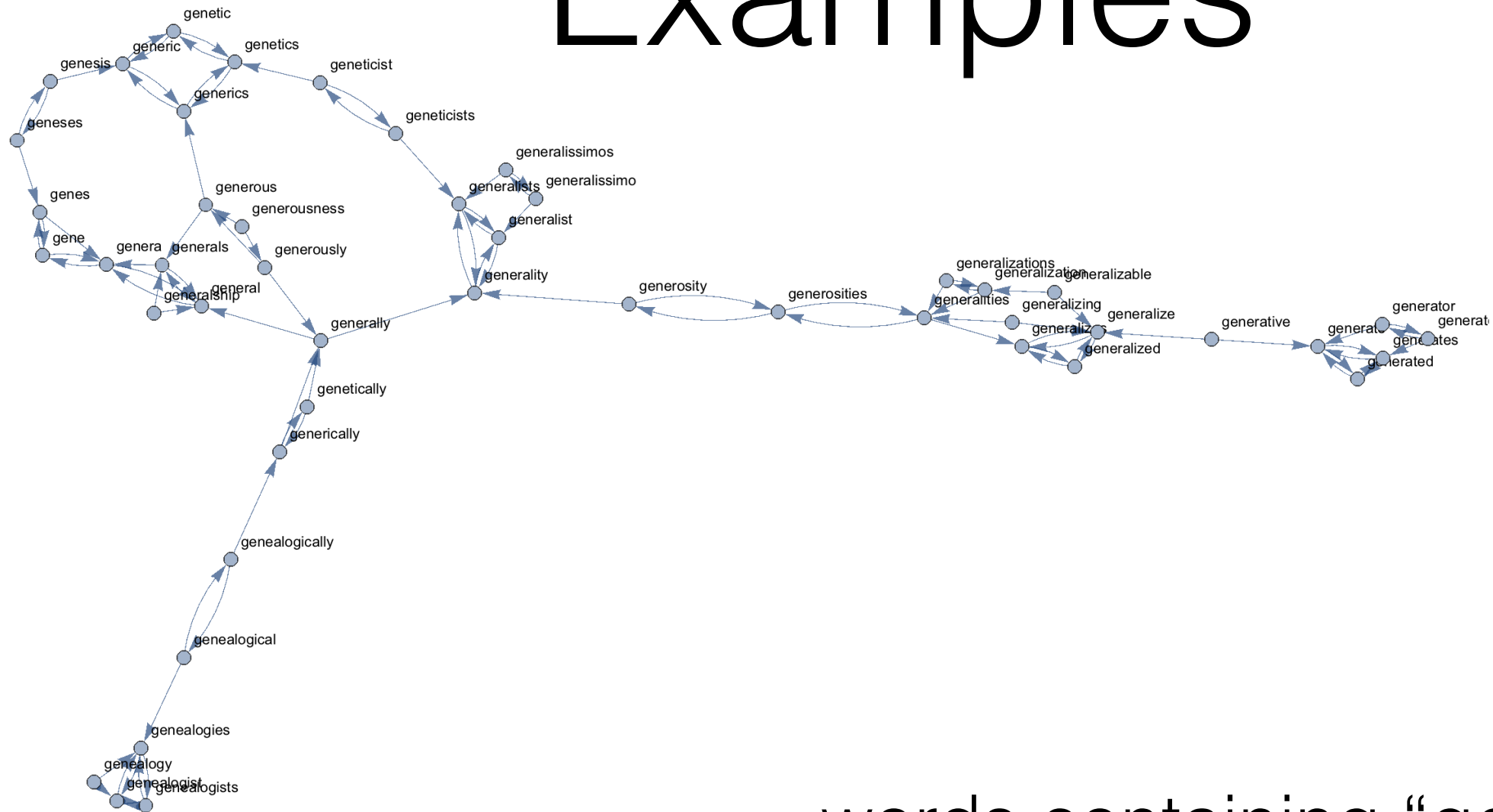


Social Network
Influence of Body
Weight

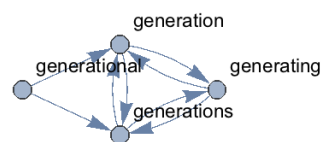


Internet Service
Providers

Examples



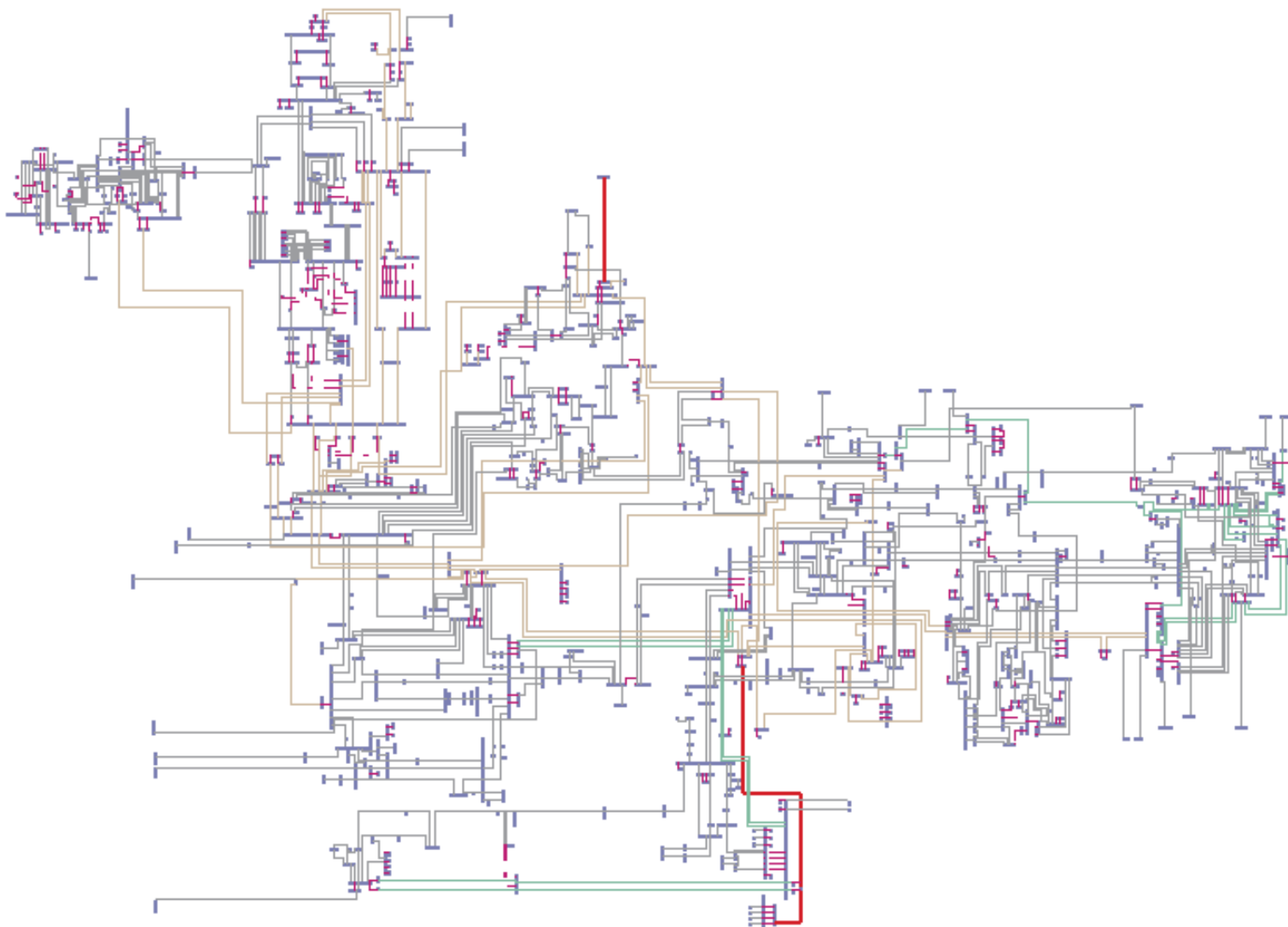
words containing “gene”



Examples

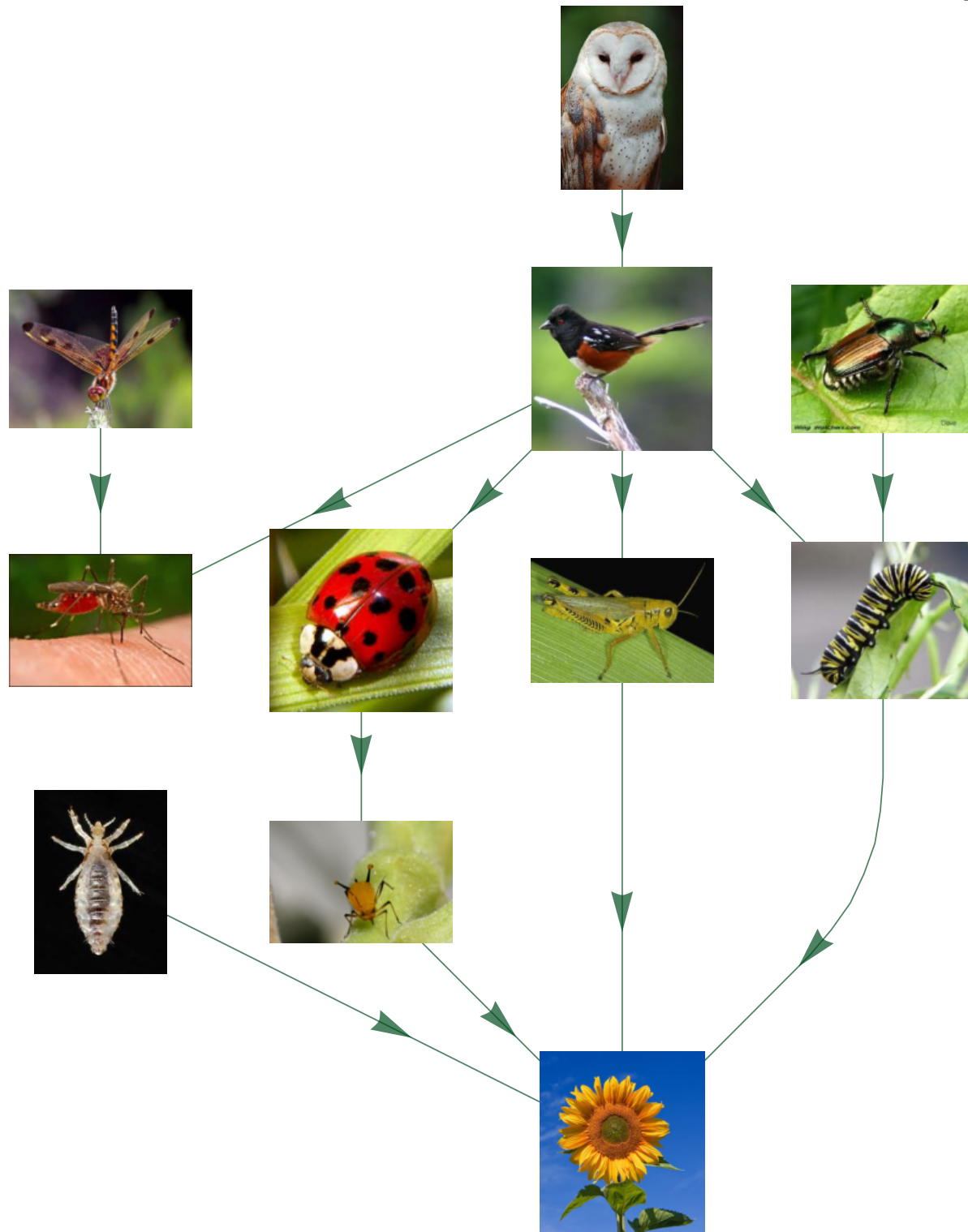
Nodes: Generators and substations

Edges: Transmission lines and transformers. (Line thickness and color indicate the voltage level)



NY Power Grid

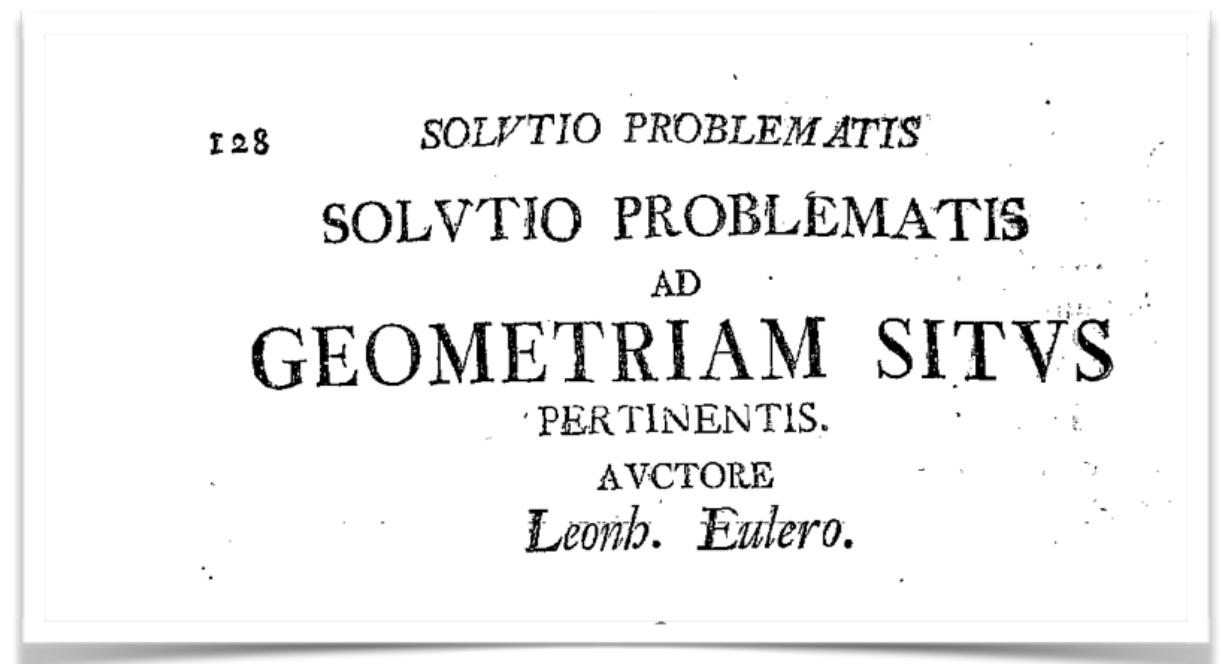
Examples



Food Web Network

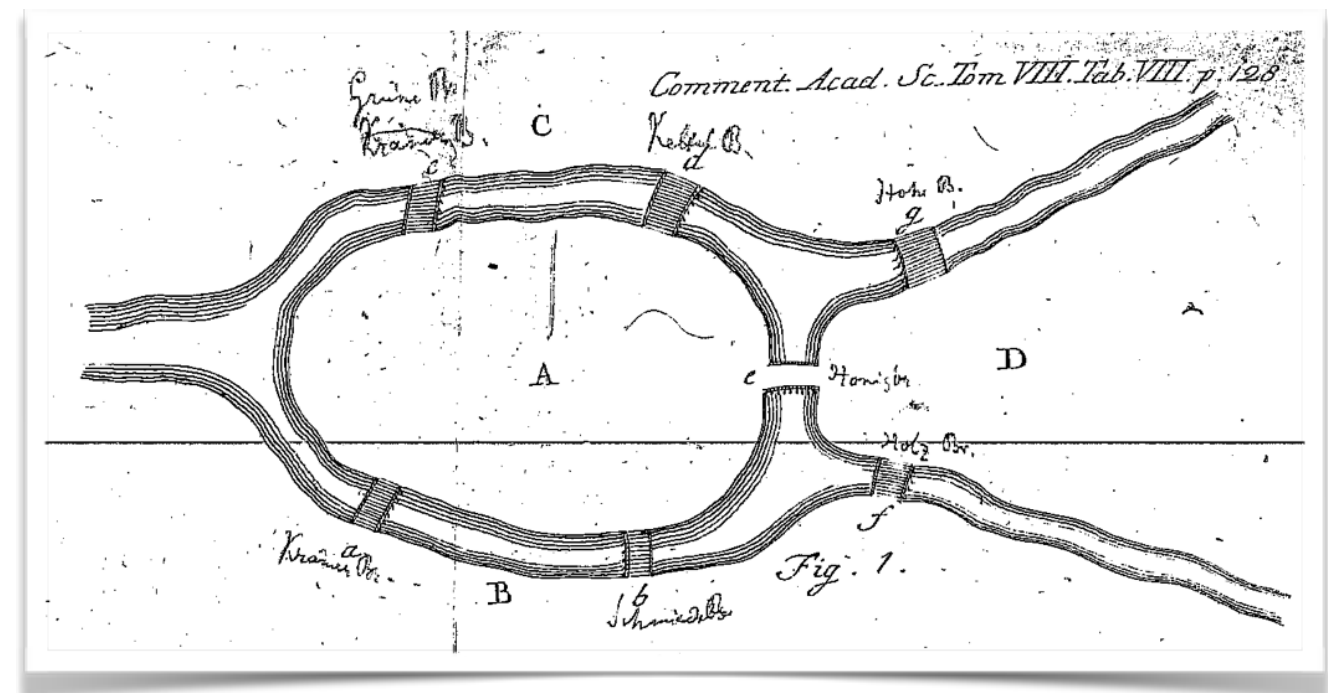
Bridges of Königsberg

- Leonhard Euler
 - 1736
 - 7 bridges across Pregolya River
 - Prussian Königsberg (now Kaliningrad, Russia)
 - Is there a route to cross each bridge exactly once?



Bridges of Königsberg

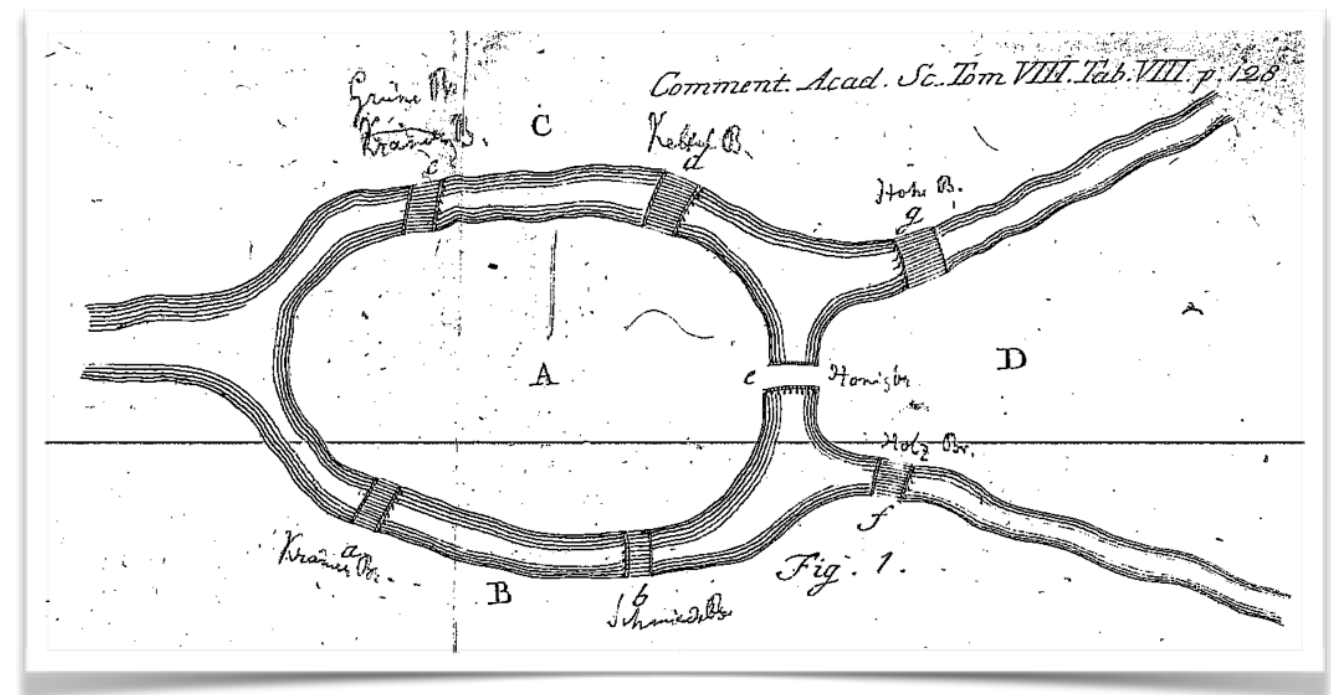
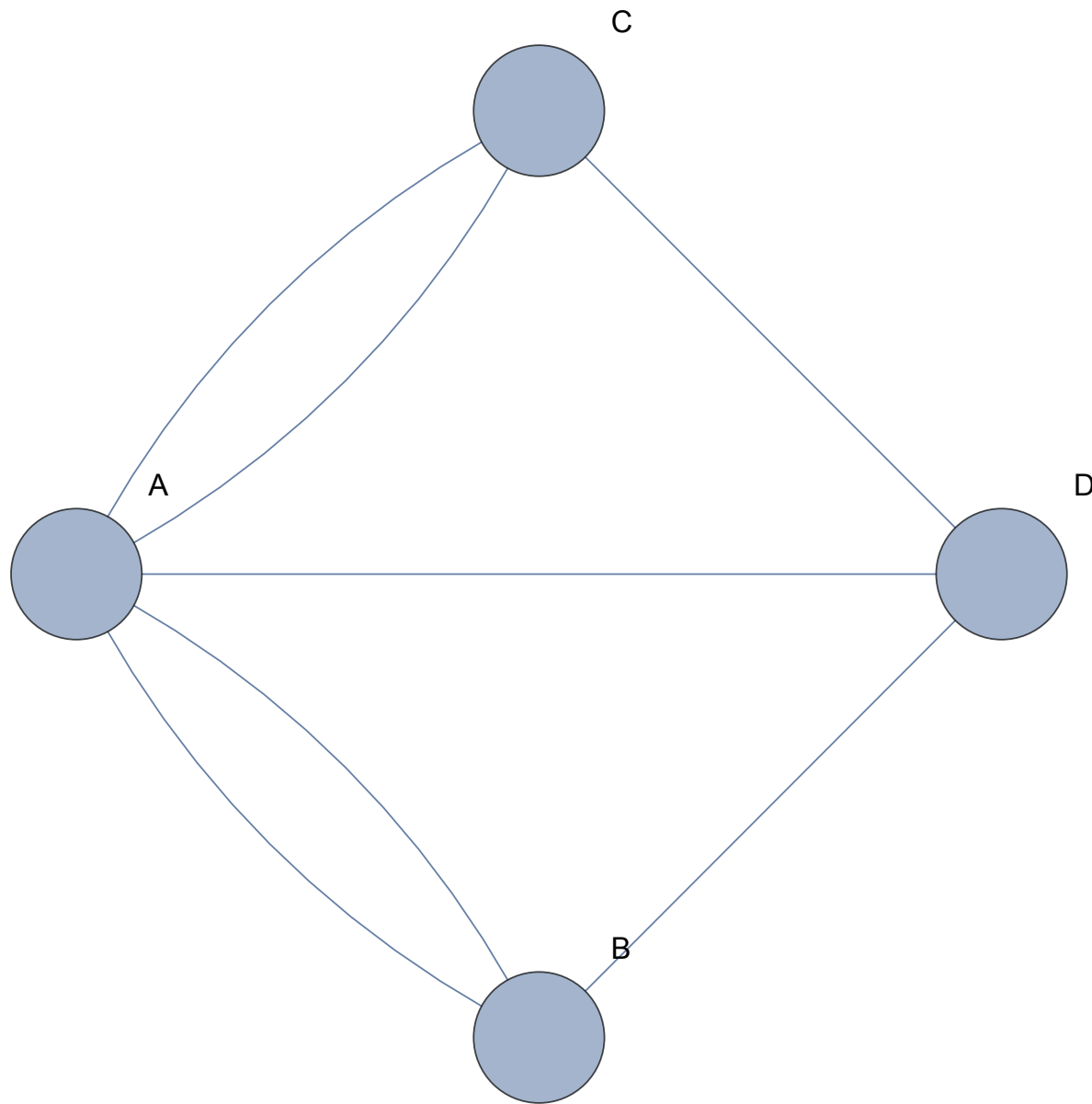
- Leonhard Euler
- 1736
- 7 bridges across Pregolya River
- Prussian Königsberg (now Kaliningrad, Russia)
- Is there a route to cross each bridge exactly once?



e.g. AB, BA, AC, CA, AD, ..., ?

The Euler Archive <http://eulerarchive.maa.org>

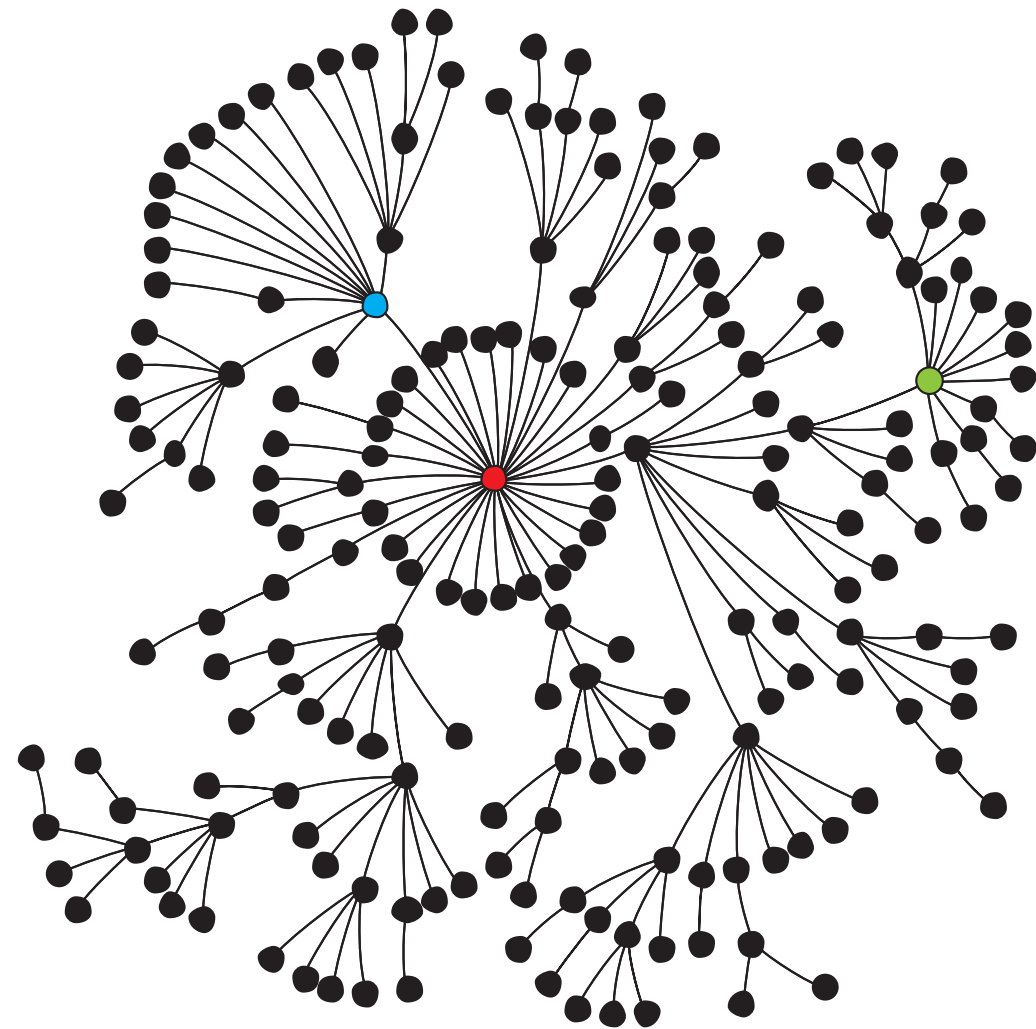
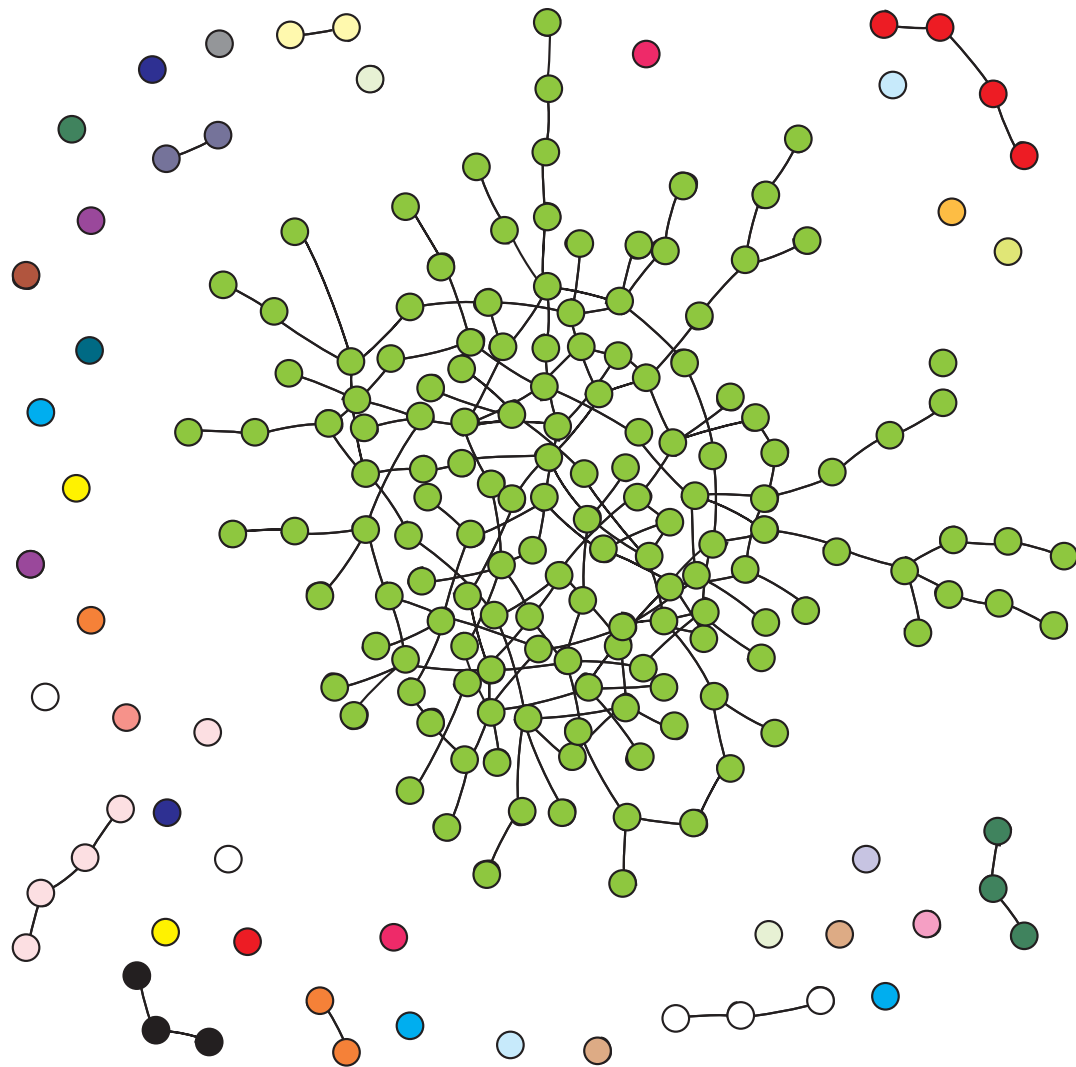
Bridges of Königsberg



e.g. AB, BA, AC, CA, AD, ..., ?

The Euler Archive <http://eulerarchive.maa.org>

Random Networks



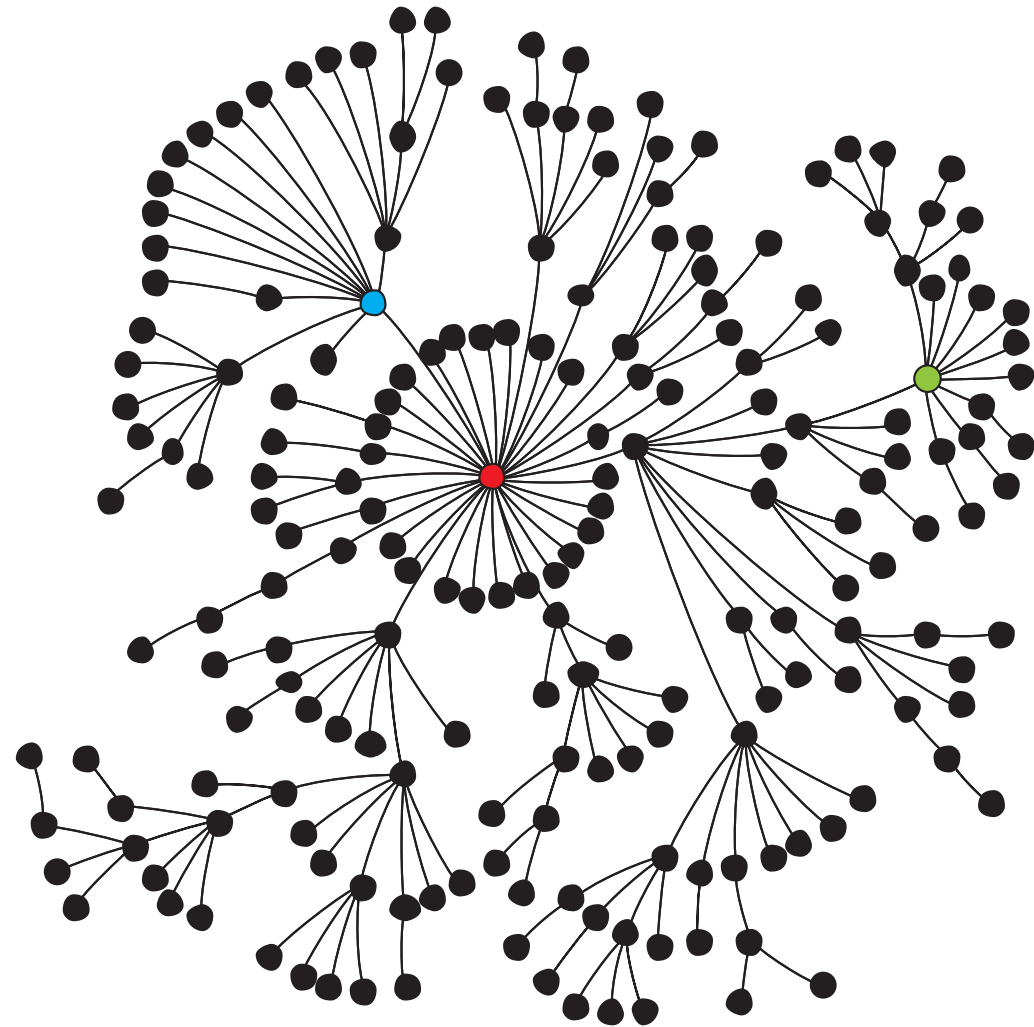
Scale Free Graph

Strogatz, Nature 410, p268 (2001)

Properties

Scale Free Networks

- Robust
 - if vertices removed network still connected
- Vulnerable
 - can target hubs



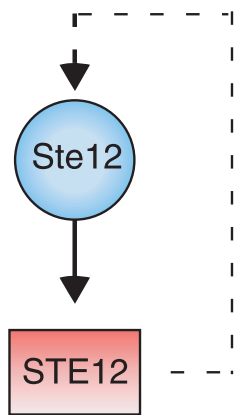
Strogatz, Nature 410, p268 (2001)
Albert et al., Nature 406 p.378 (2000)

Community Structure

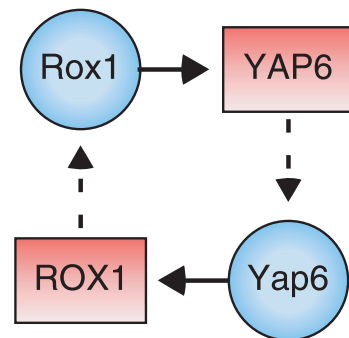
- **Social Networks**
 - groups of different people
- **internet pages**
 - various topics
- **Metabolites**
 - various functions
- **genes**
 - various processes

Gene Regulation

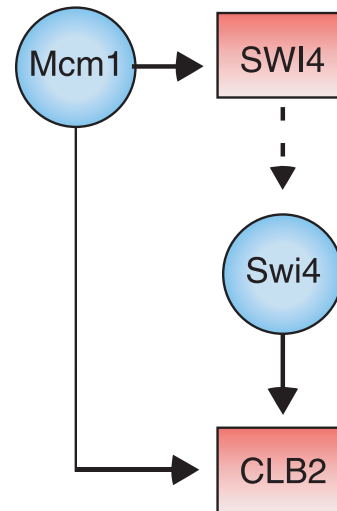
Autoregulation



Multi-Component Loop

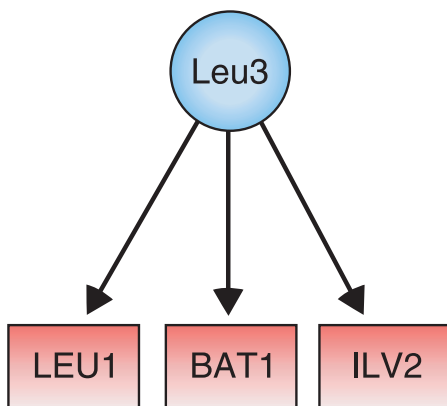


Feedforward Loop

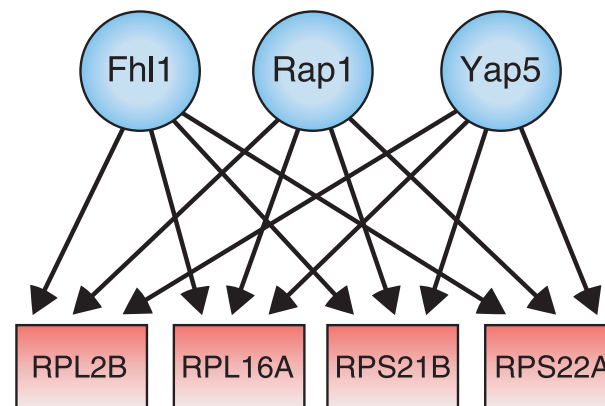


- *Saccharomyces cerevisiae*
- Activators (increase)
- Repressor (decrease)
- Feedback loops
- Motifs

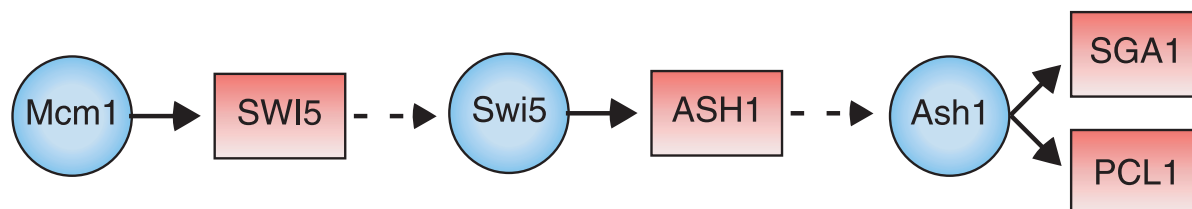
Single Input Motif



Multi-Input Motif

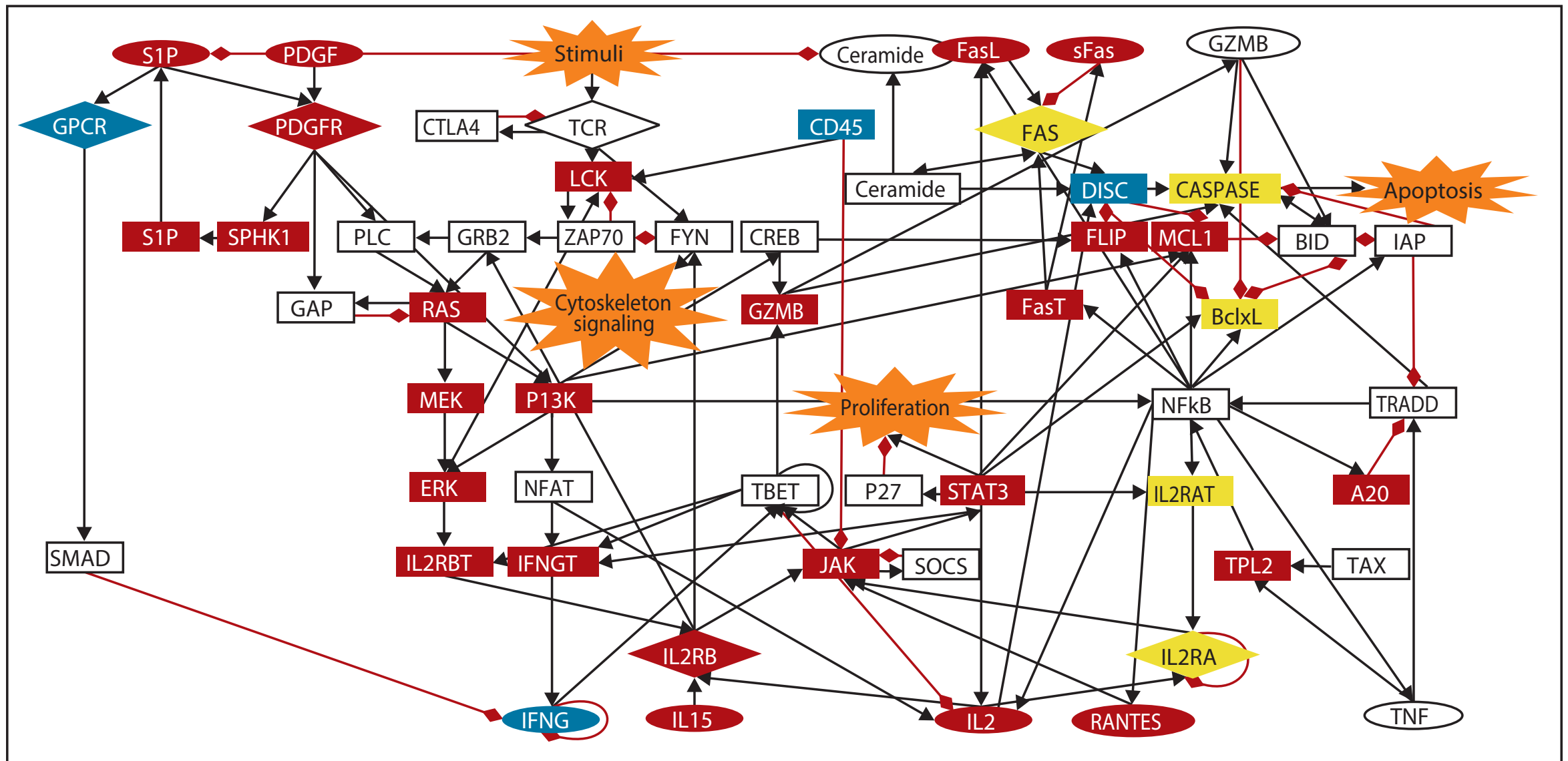


Regulator Chain



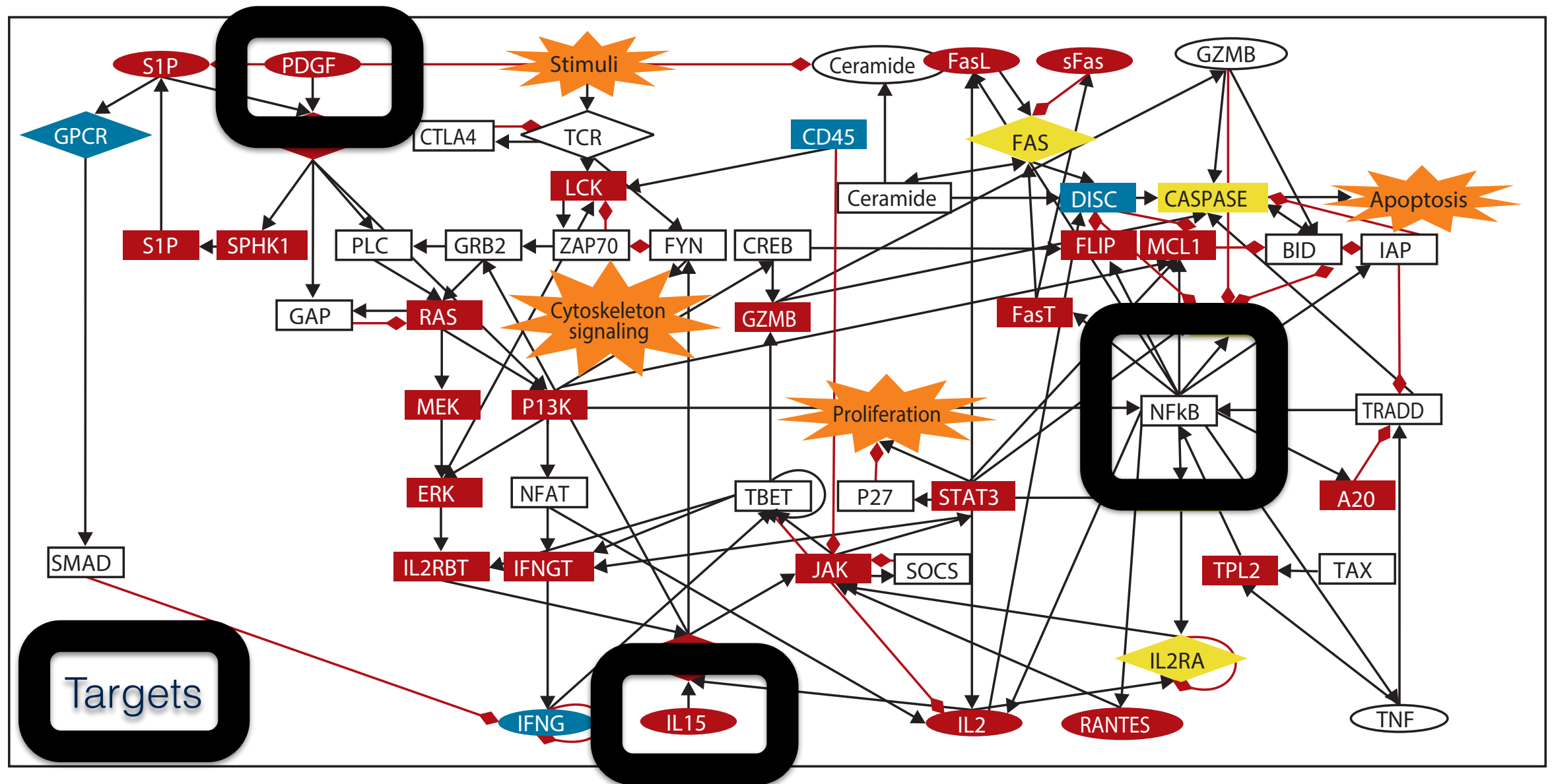
Lee et al., Science 298, p.799 (2002)

Examples



T cell signaling (Apoptosis) Protein Network

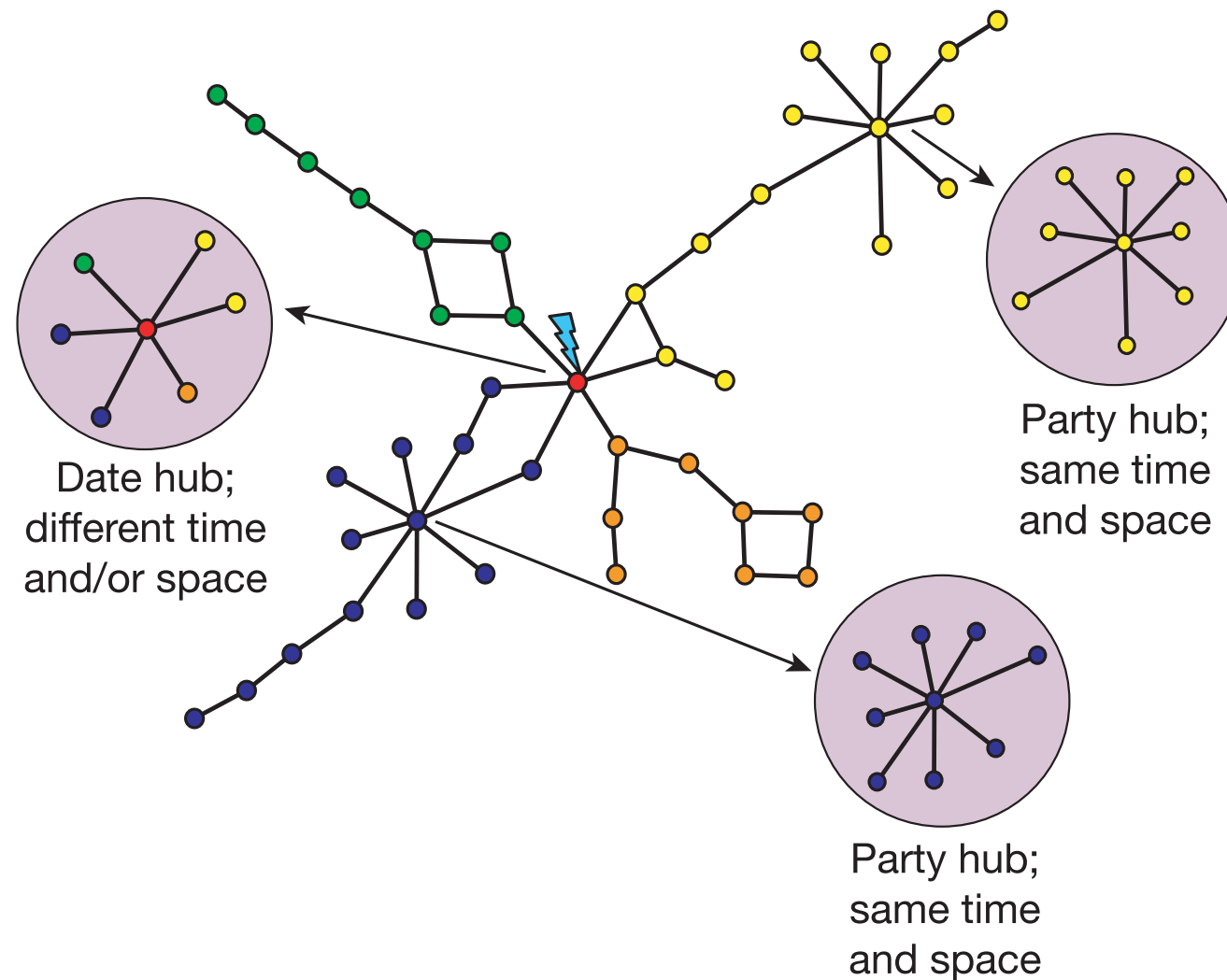
Examples



T cell signaling (Apoptosis) Protein Network

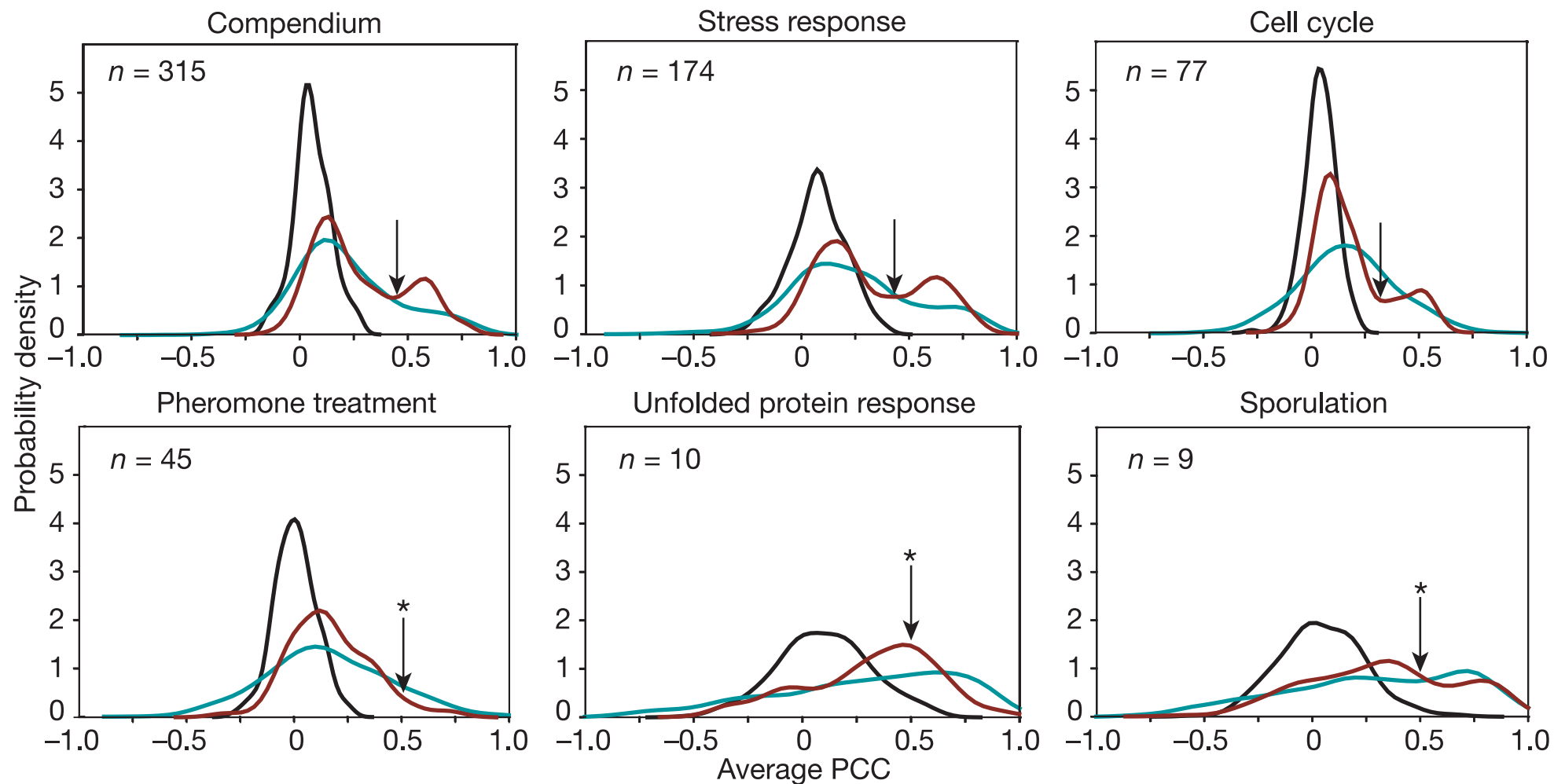
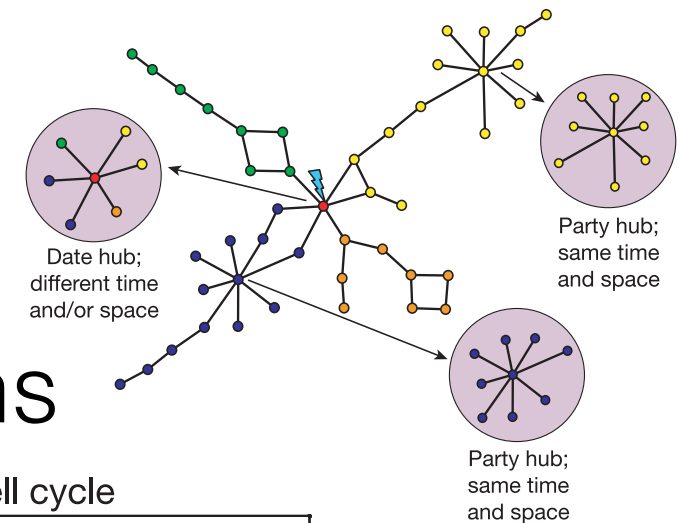
Examples

modularity in Yeast Protein-Protein Interactions



Examples

modularity in Yeast Protein-Protein Interactions

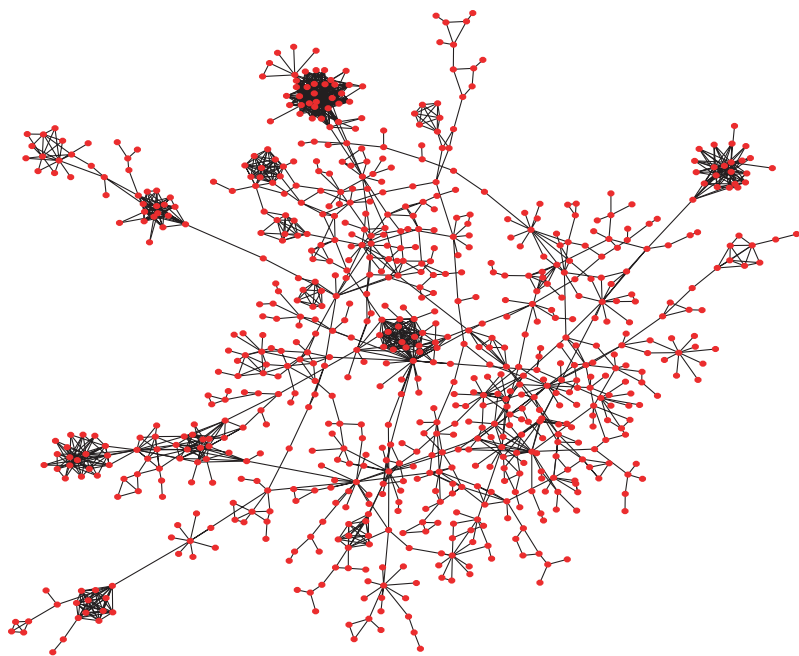


PCC: average Pearson Correlation Coefficient between the hub and each of its respective partners for mRNA expression

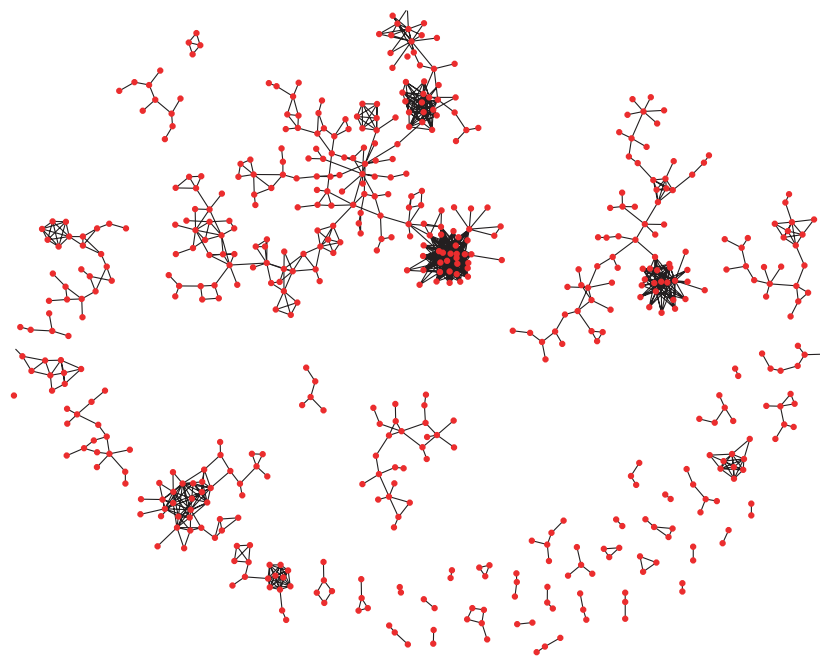
Han et al., Nature 430, p. 88 (2004)

Examples

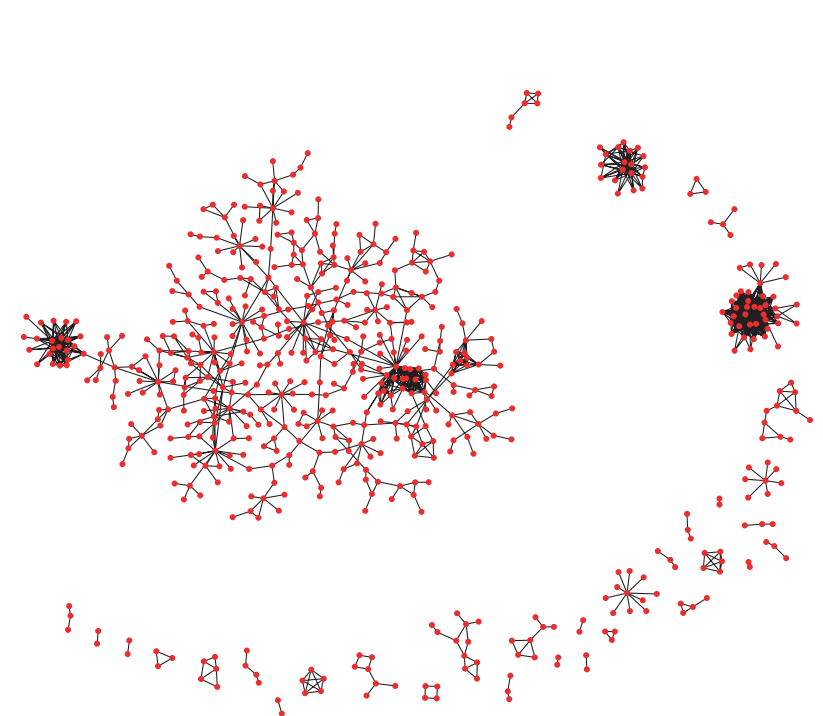
modularity in Yeast Protein-Protein Interactions



main component



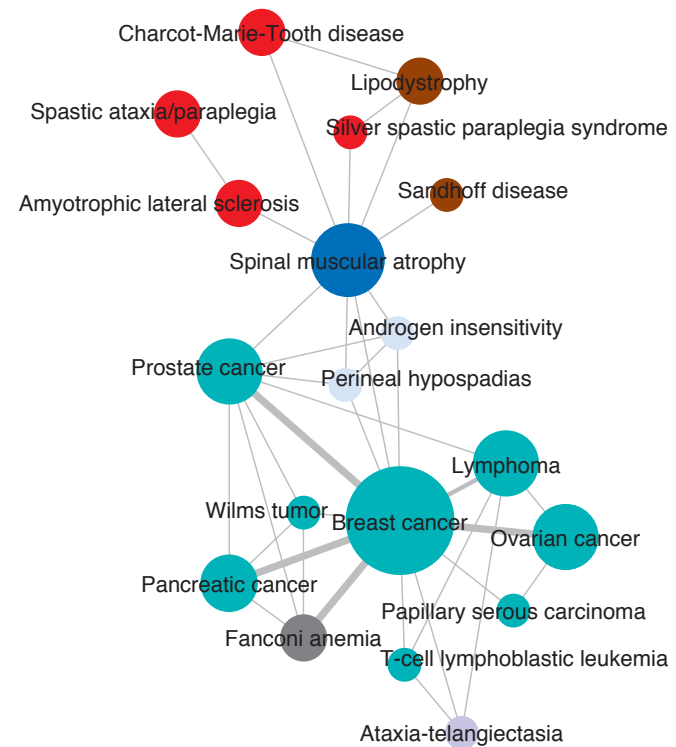
removal of date hubs
(small subnetworks)



removal of party hubs
(intact)

Examples

*Human Disease Network
(HDN)*

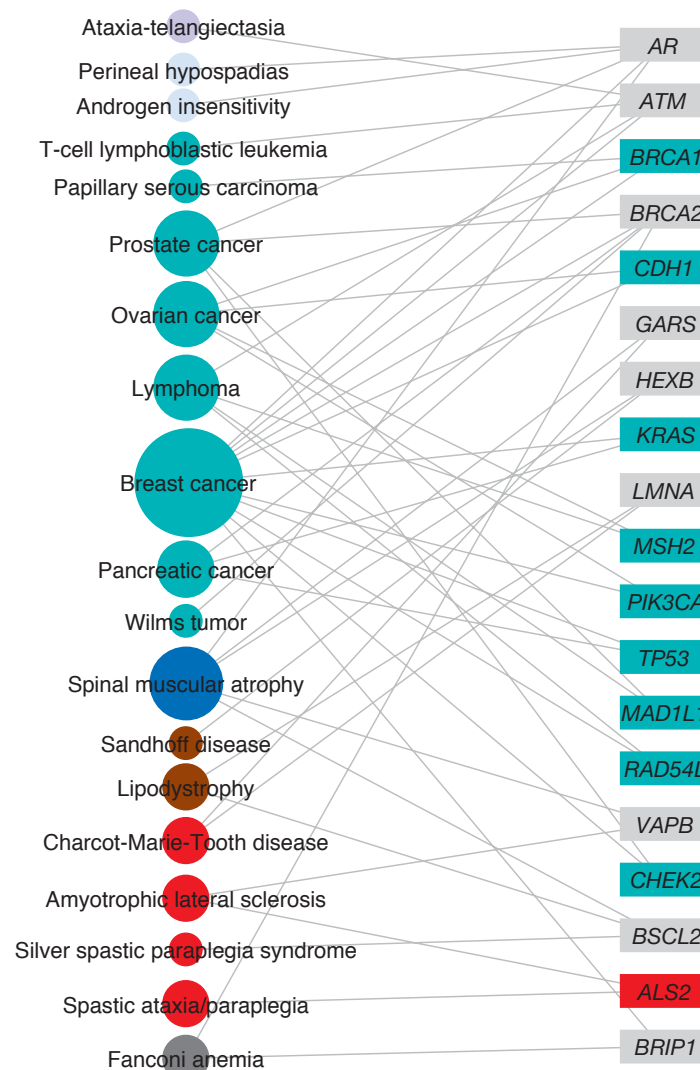


bipartite
OMIM based

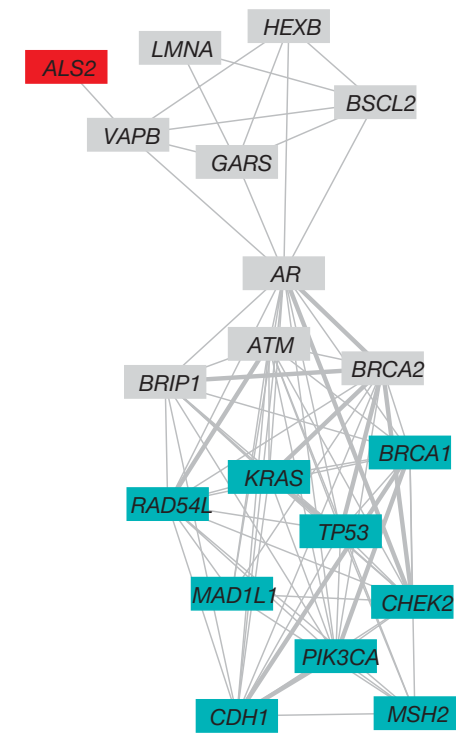
DISEASOME

disease phenotype

disease genome

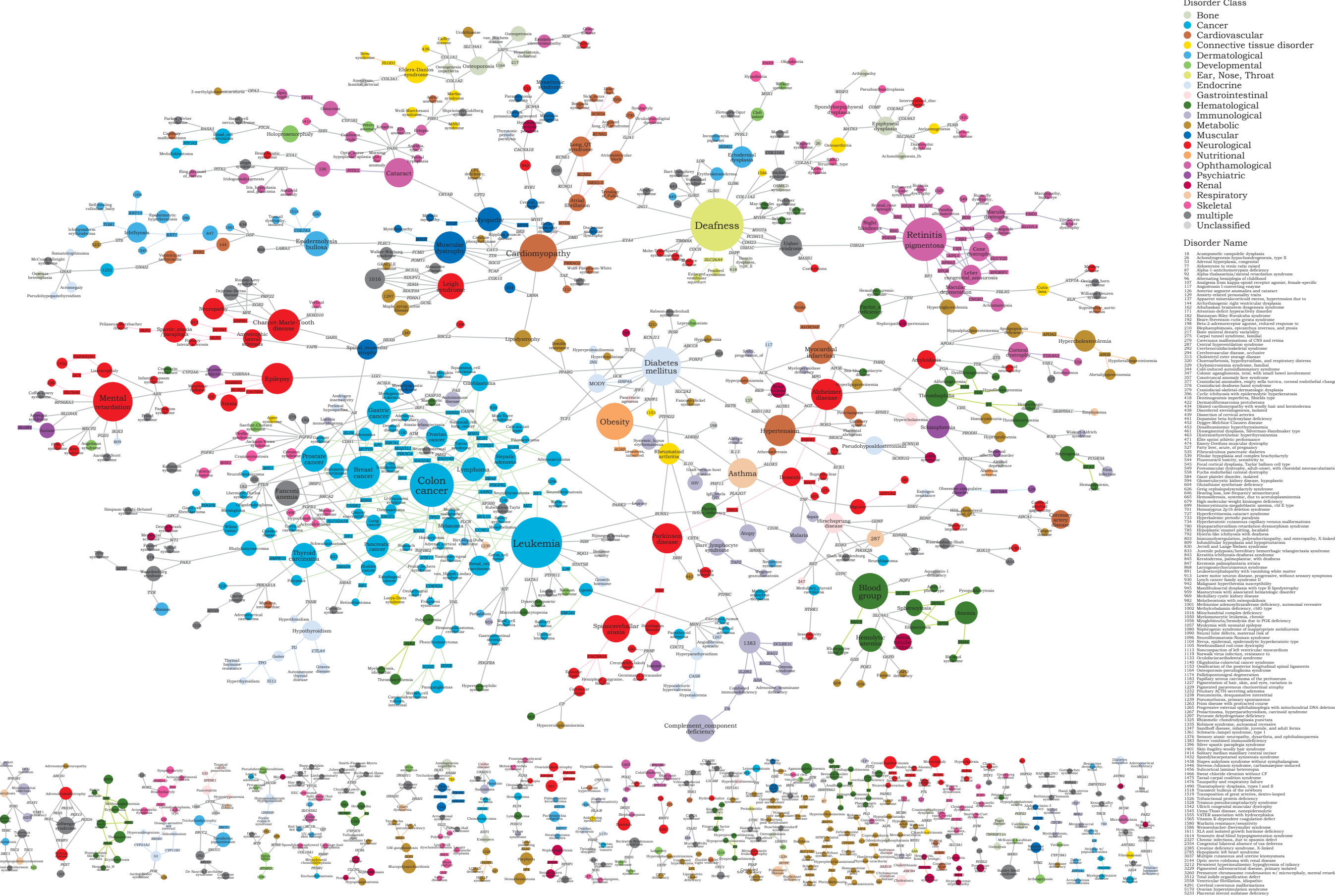


*Disease Gene Network
(DGN)*



Goh et al., PNAS 104(21) p.8685 (2007)

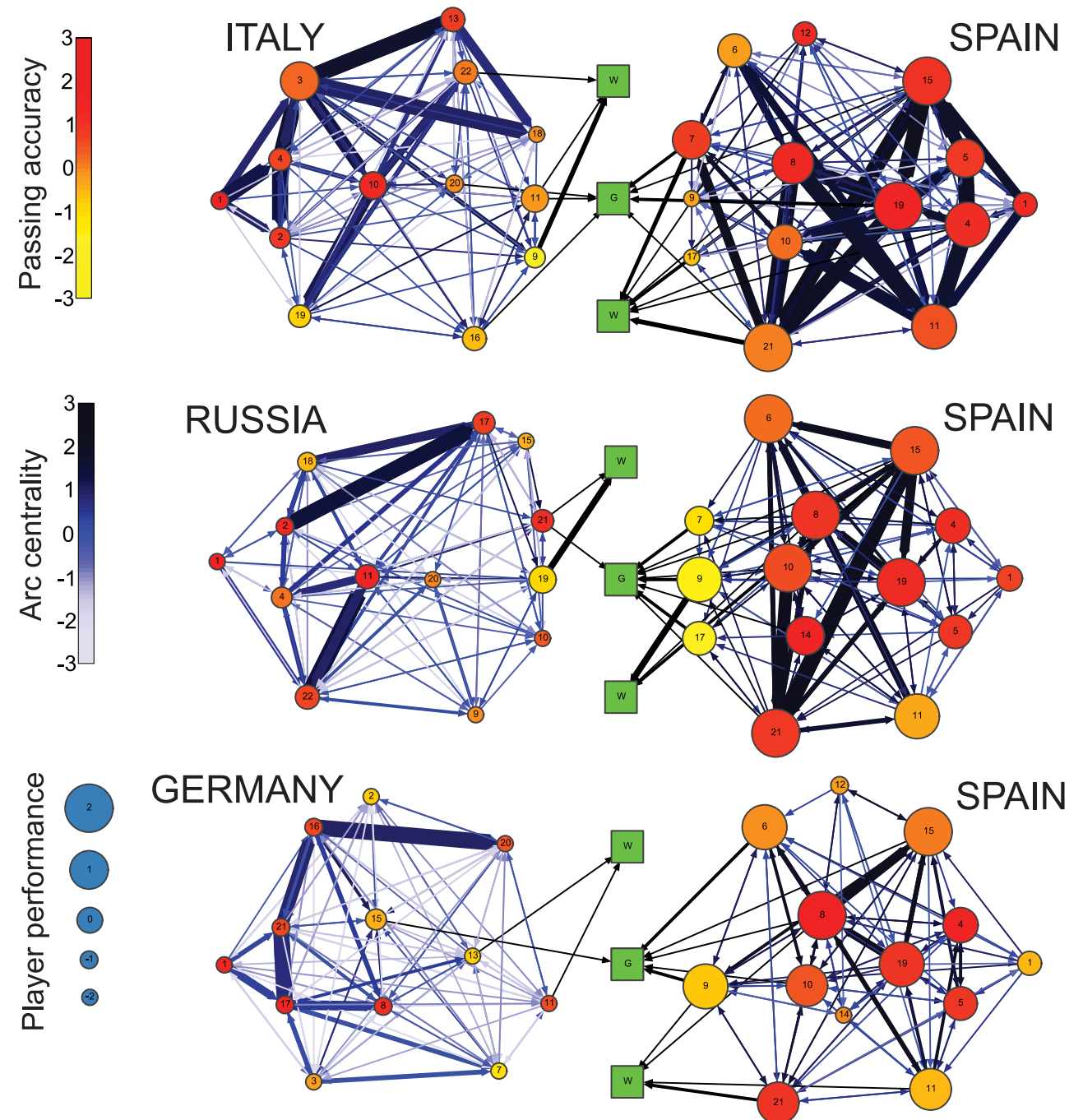
Goh K-I, Cusick ME, Valle D, Childs B, Vidal M, Barabási A-L (2007) *Proc Natl Acad Sci USA* 104:8685-8690



Supporting Information Figure 13 | Bipartite-graph representation of the diseasome. A disorder (circle) and a gene (rectangle) are connected if the gene is implicated in the disorder. The size of the circle represents the number of distinct genes associated with the disorder. Isolated disorders (disorders having no links to other disorders) are not shown. Also, only genes connecting disorders are shown.

Other Applications

Quantifying the
Performance of
Individual Players
in a Team Activity
(Euro 2008)



Gene Ontology

Ontology

Definition

- “A set of concepts and categories in a subject area or domain that shows their properties and the relations between them.” *New Oxford American Dictionary, Oxford University Press 2013*

Gene Ontology

Gene Ontology (GO)

“a computational representation of our evolving knowledge of how genes encode biological functions at the molecular, cellular and tissue system levels”

- [Controlled vocabulary of terms](#)
 - Describe gene product characteristics
 - [Gene product annotation data](#)
- [Tools for GO](#)

Gene Ontology

Controlled vocabularies

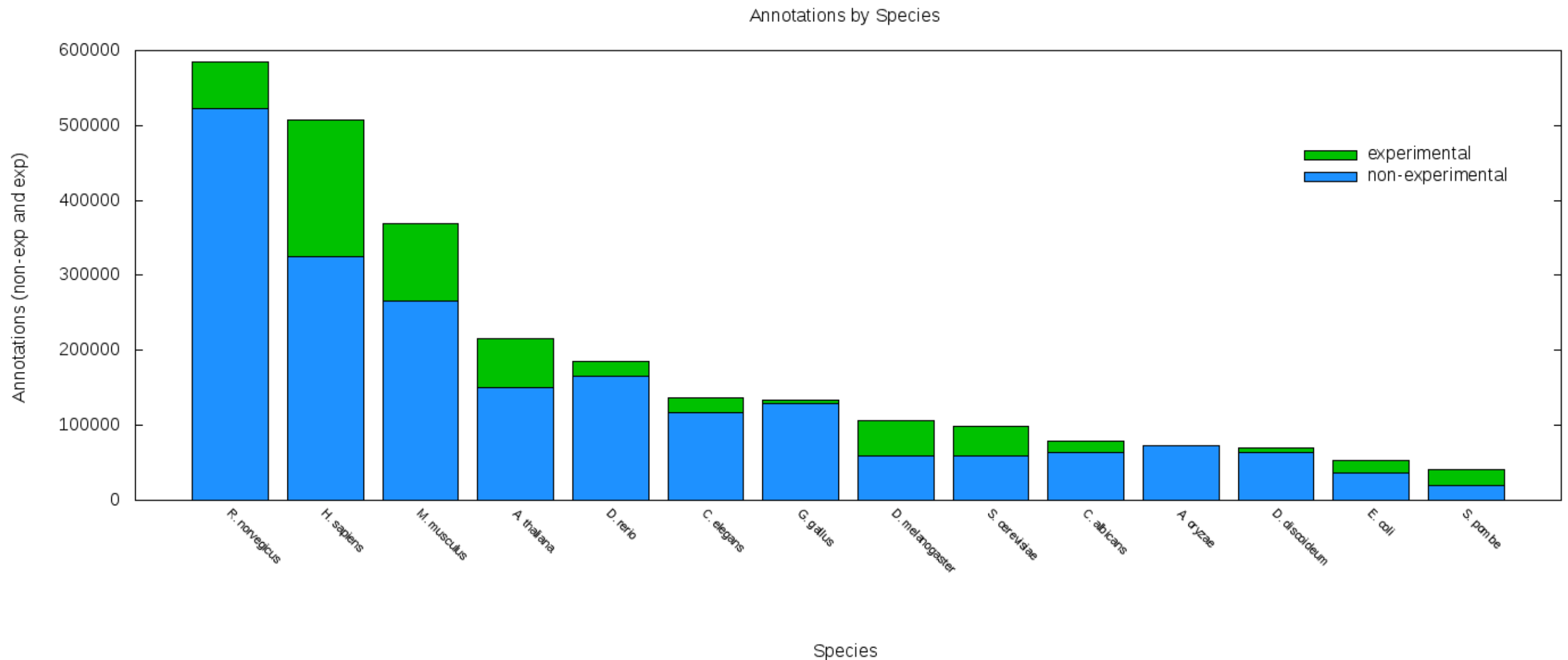
- **Cellular Component (CC)**, the parts of a cell or its extracellular environment
- **Molecular Function (MF)**, the elemental activities of a gene product at the molecular level, such as binding or catalysis
- **Biological Process** operations or sets of molecular events with a defined beginning and end, pertinent to the functioning of integrated living units: cells, tissues, organs, and organisms.

Gene Ontology

Example

- gene product "cytochrome c"
 - ▶ **Molecular Function**
 - "oxidoreductase activity"
 - ▶ **Biological Process**
 - "oxidative phosphorylation"
 - "induction of cell death"
 - ▶ **Cellular Component**
 - "mitochondrial matrix"
 - "mitochondrial inner membrane".

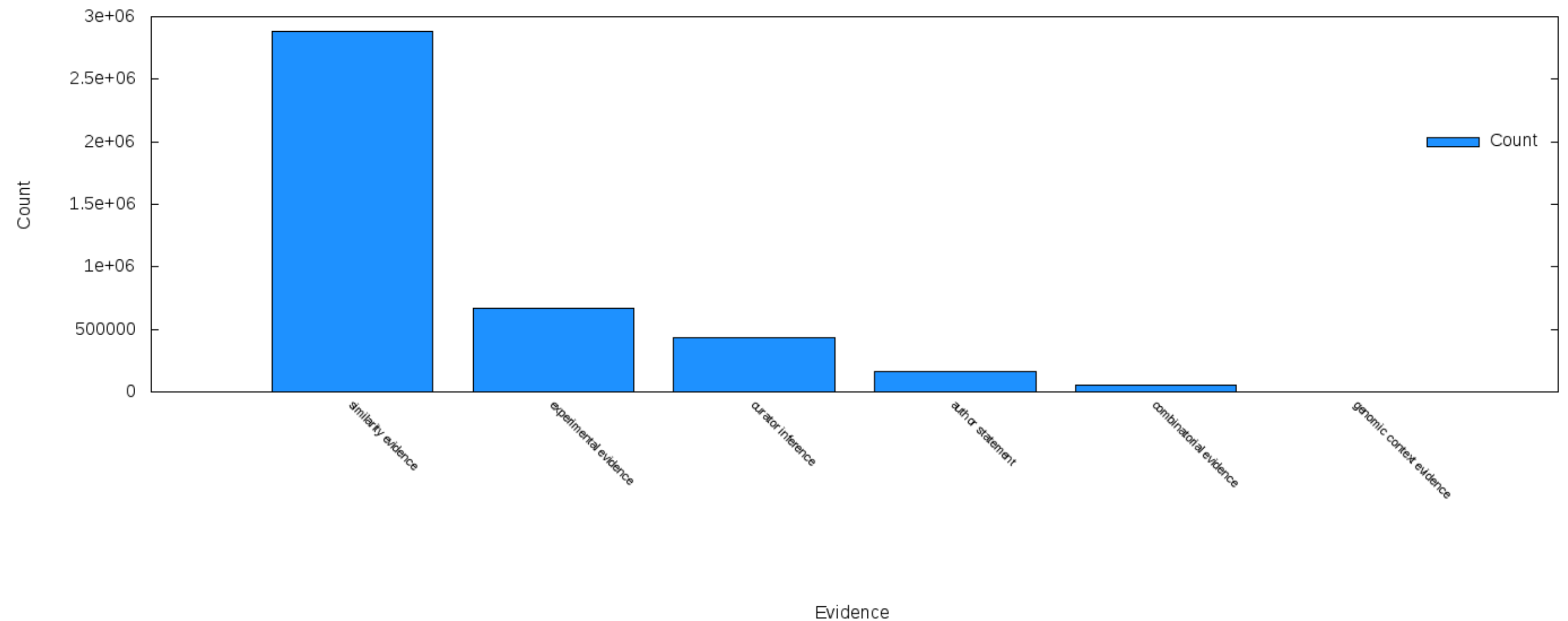
Gene Ontology



Note: GO vocabulary is designed to be species-agnostic, and includes terms applicable to prokaryotes and eukaryotes, and single and multicellular organisms.

Gene Ontology

Evidence Overview

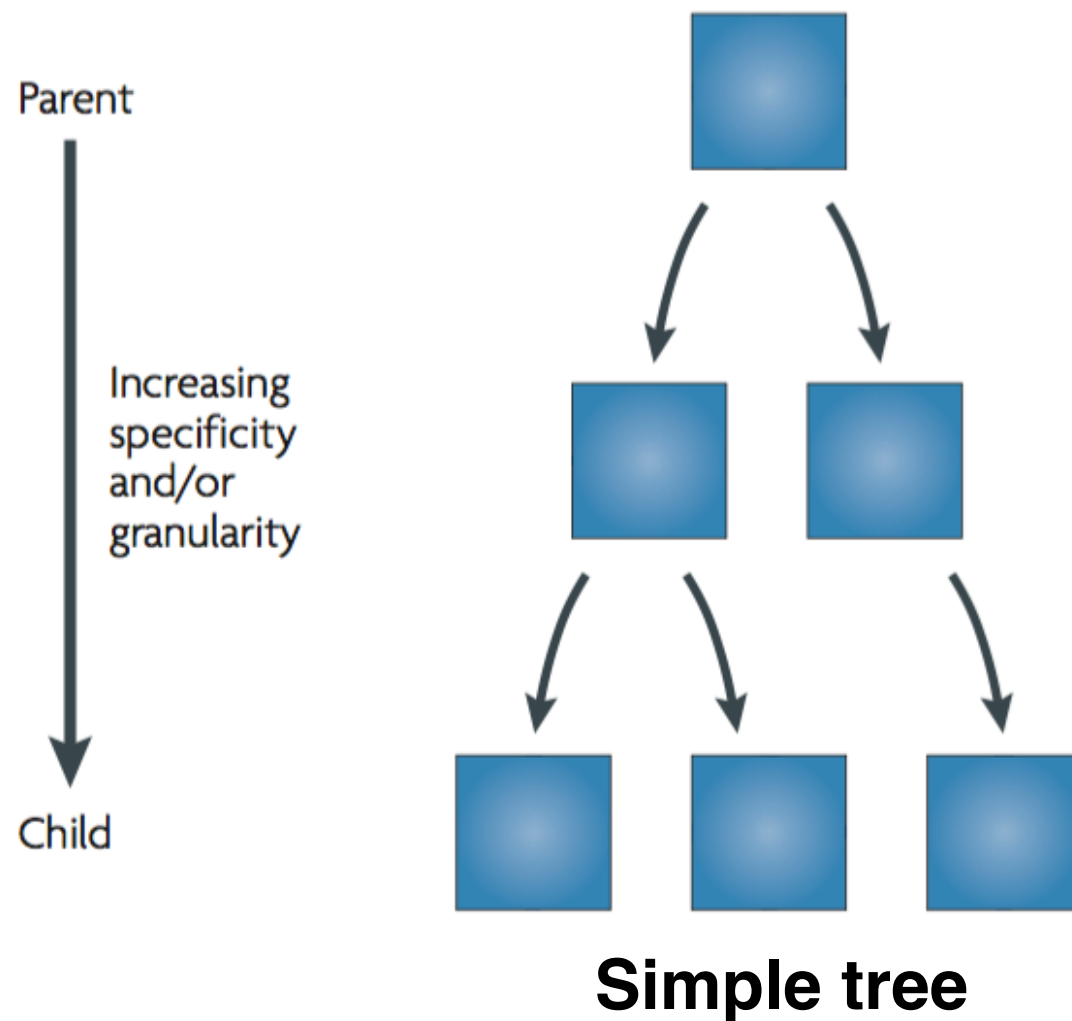


Gene Ontology

evidence code	evidence code description	source of evidence	Manually checked
IDA	Inferred from direct assay	Experimental	Yes
IEP	Inferred from expression pattern	Experimental	Yes
IGI	Inferred from genetic interaction	Experimental	Yes
IMP	Inferred from mutant phenotype	Experimental	Yes
IPI	Inferred from physical interaction	Experimental	Yes
ISS	Inferred from sequence or structural similarity	Computational	Yes
RCA	Inferred from reviewed computational analysis	Computational	Yes
IGC	Inferred from genomic context	Computational	Yes
IEA	Inferred from electronic annotation	Computational	No
IC	Inferred by curator	Indirectly derived from experimental or computational evidence made by a curator	Yes
TAS	Traceable author statement	Indirectly derived from experimental or computational evidence made by the author of the published article	Yes
NAS	Non-traceable author statement	No 'source of evidence' statement given	Yes
ND	No biological data available	No information available	Yes
NR	Not recorded	Unknown	Yes

Gene Ontology

GO ontology structured as directed acyclic graph

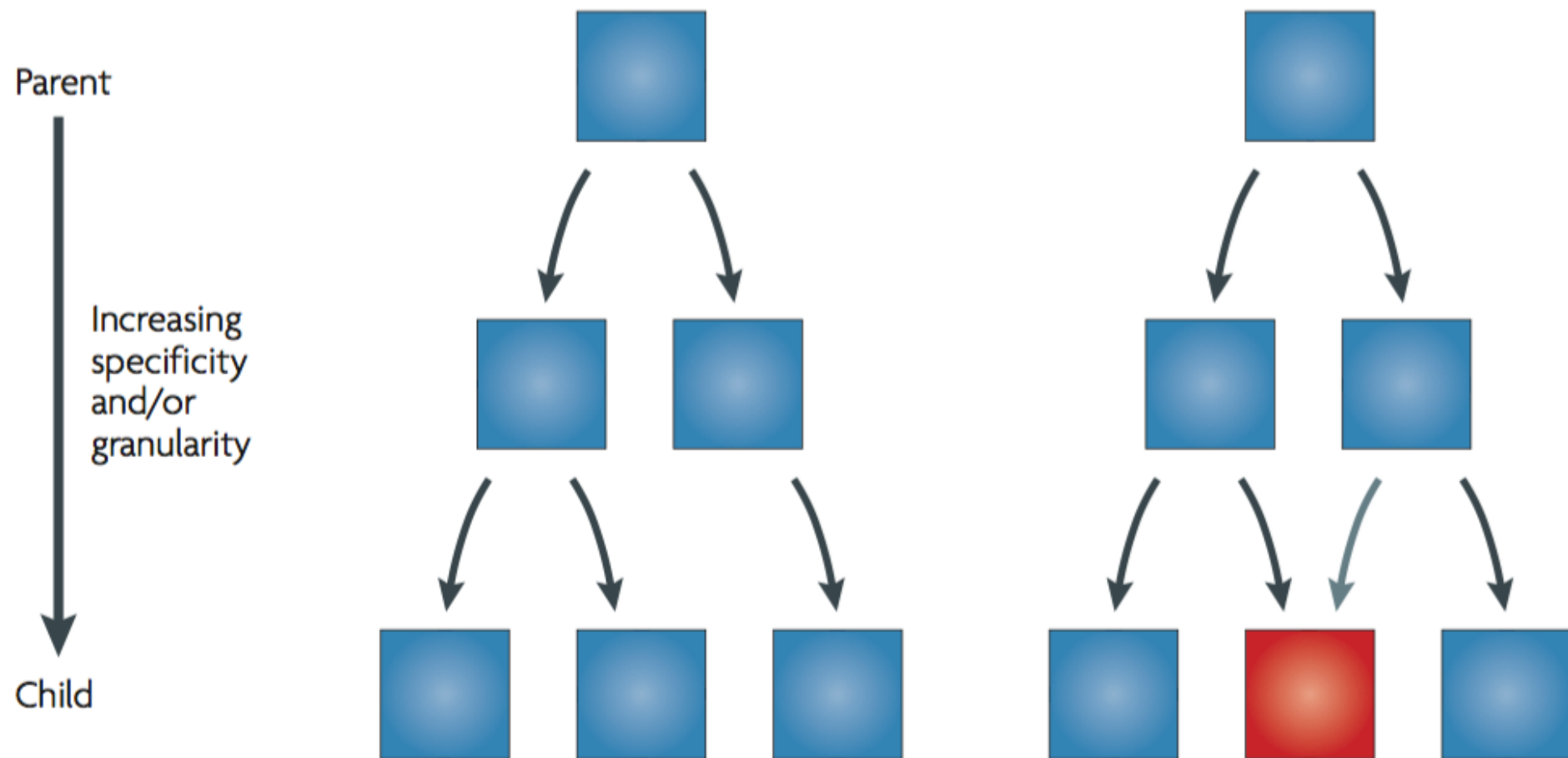


Simple tree

- each child has only one parent
- the edges are directed

Gene Ontology

GO ontology structured as **directed acyclic graph**.

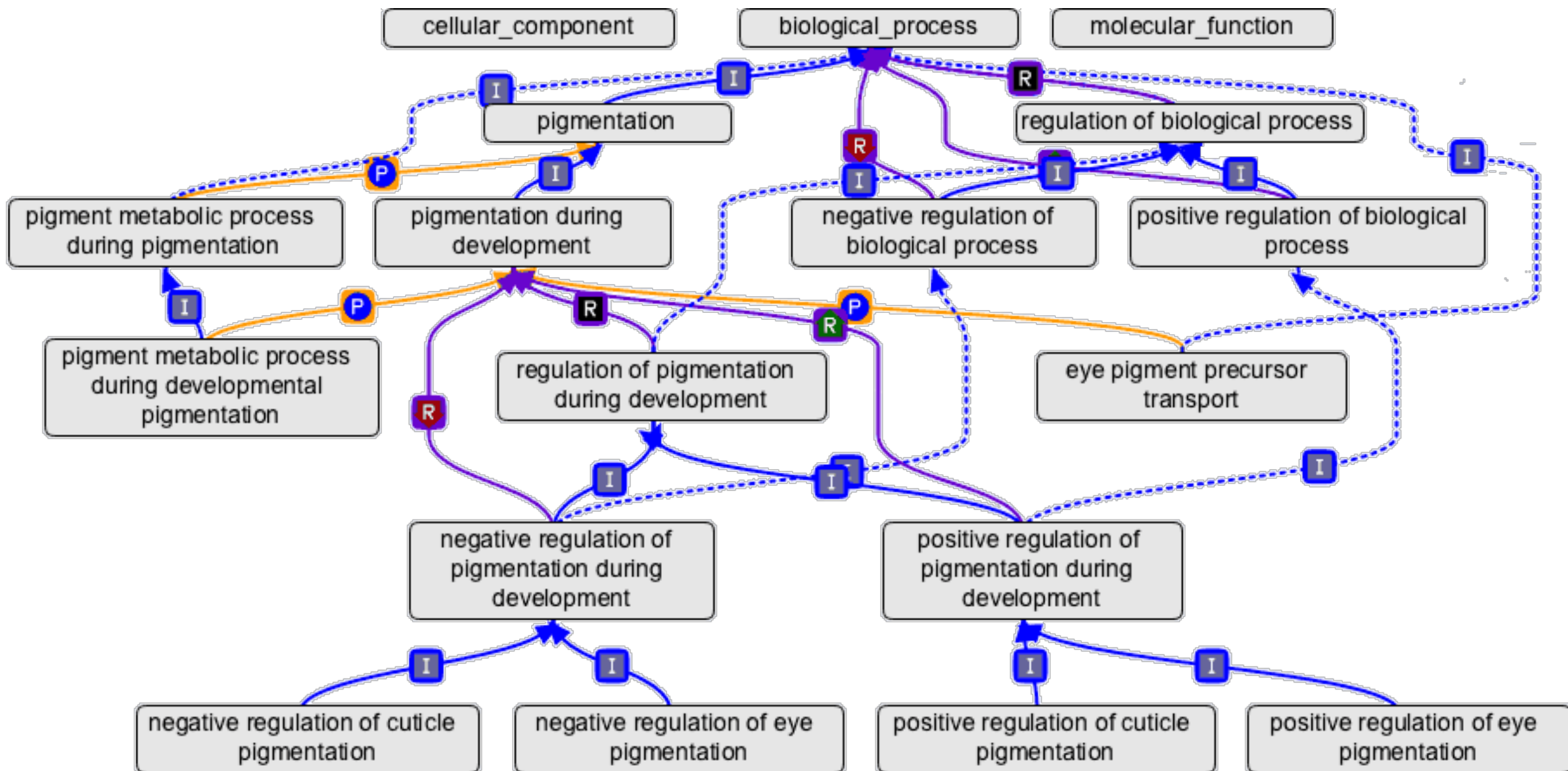


Simple tree

A directed acyclic graph (DAG)

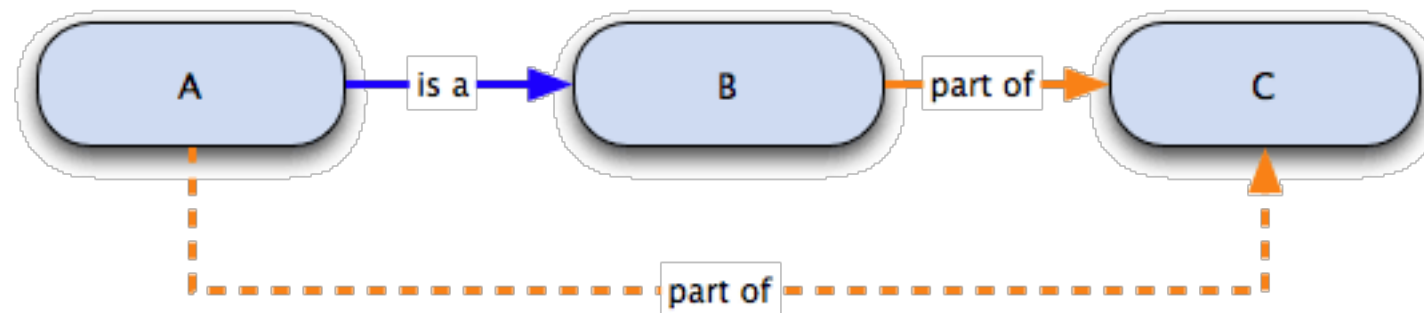
each child can have one or more parents.

Gene Ontology



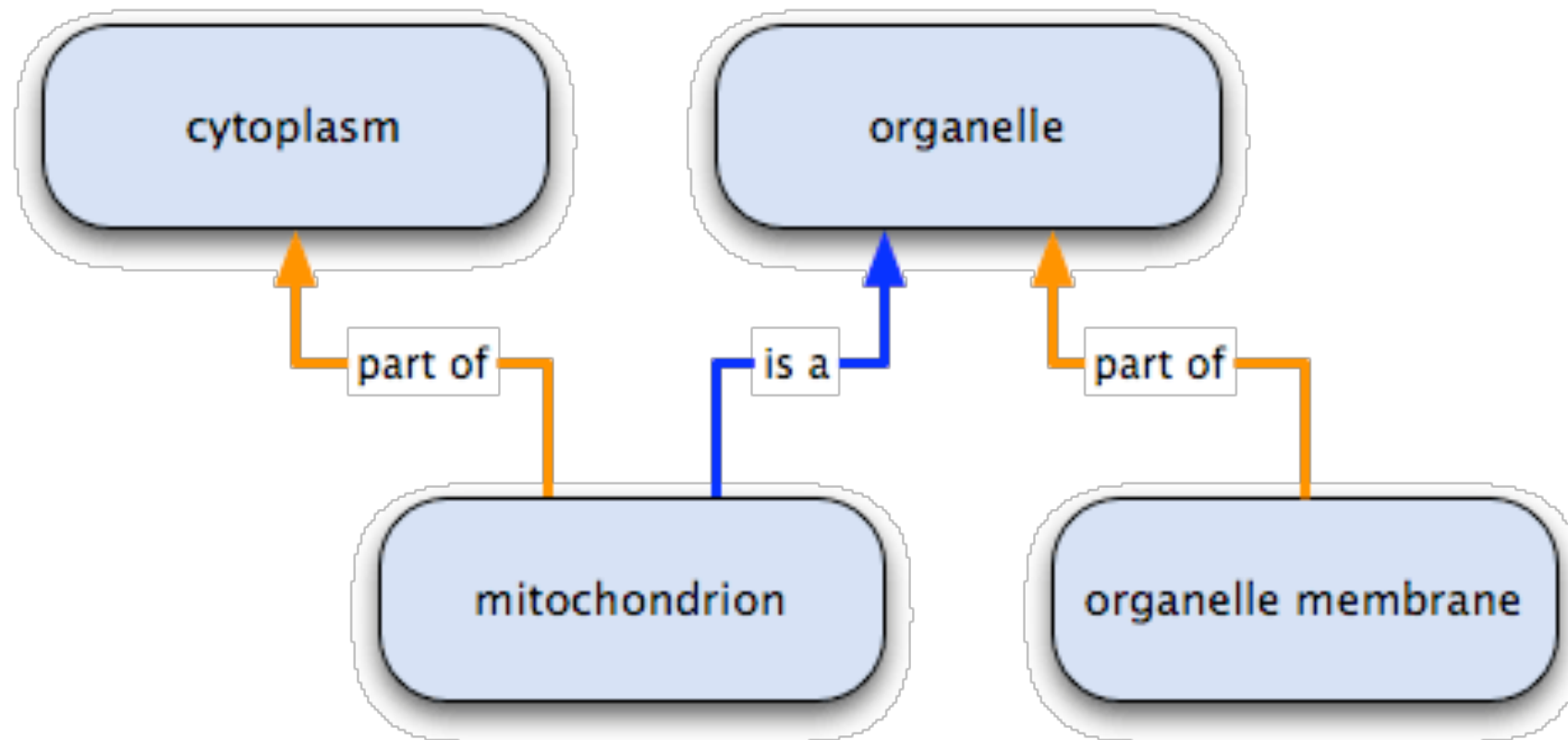
Each term can have relationships to one or more other terms in the same or other domains

Gene Ontology

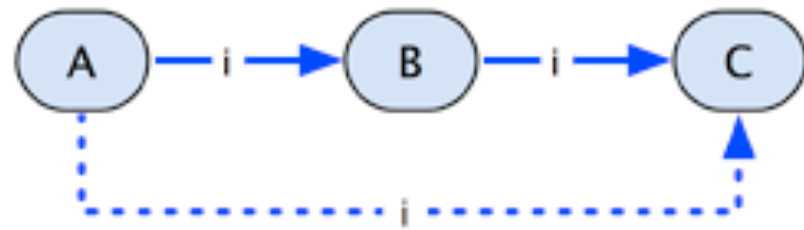


- *A is a B*
- *B is part of C*
- we can infer that *A is part of C*

Gene Ontology



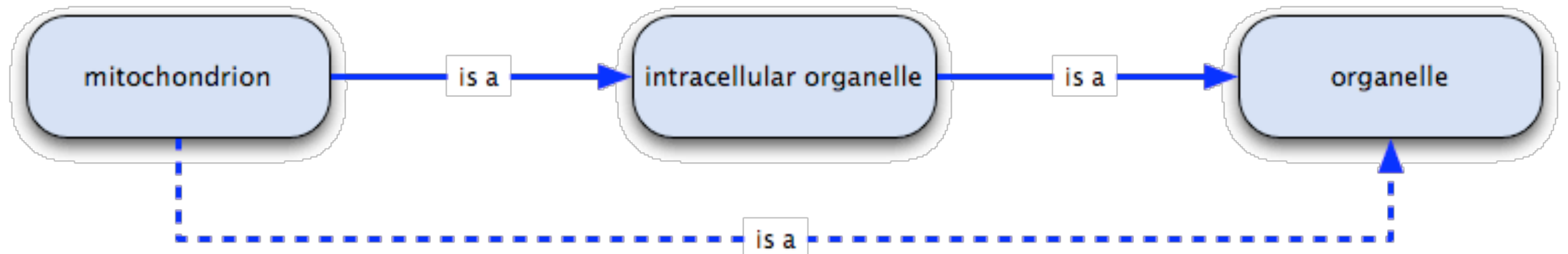
Gene Ontology



The *is a* relation is **transitive**:

If *A is a B* & *B is a C*

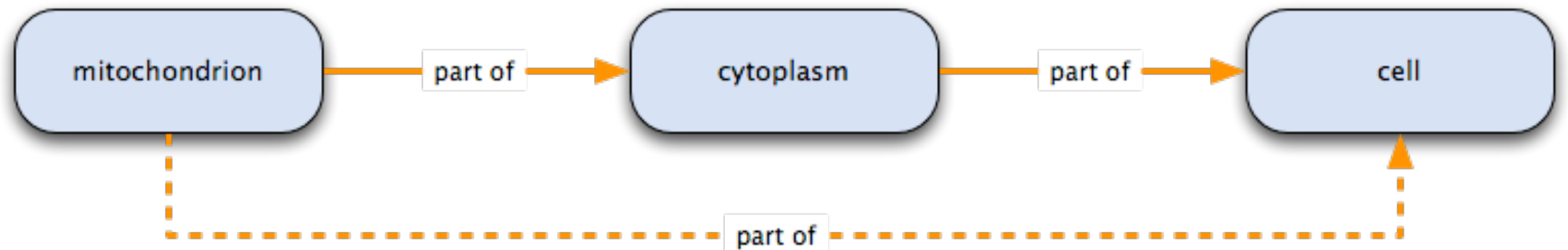
We can infer that *A is a C*



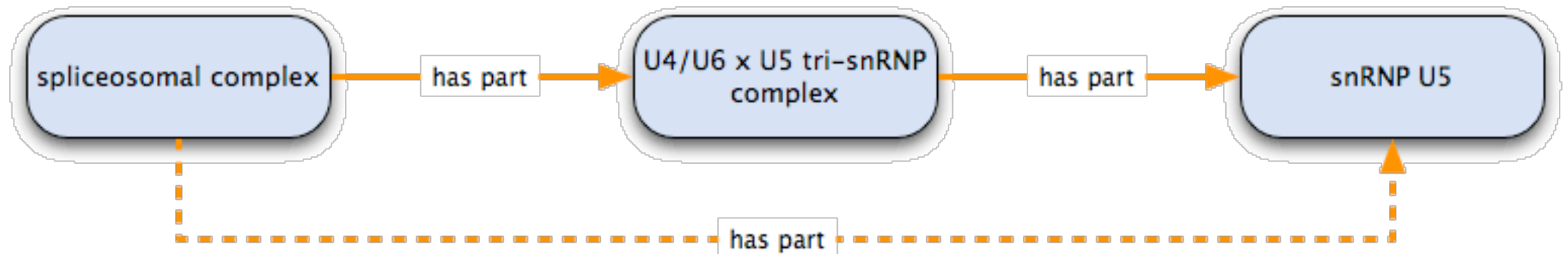
mitochondrion *is an* intracellular organelle and intracellular organelle *is an* organelle
therefore mitochondrion *is an* organelle.

Gene Ontology

part of



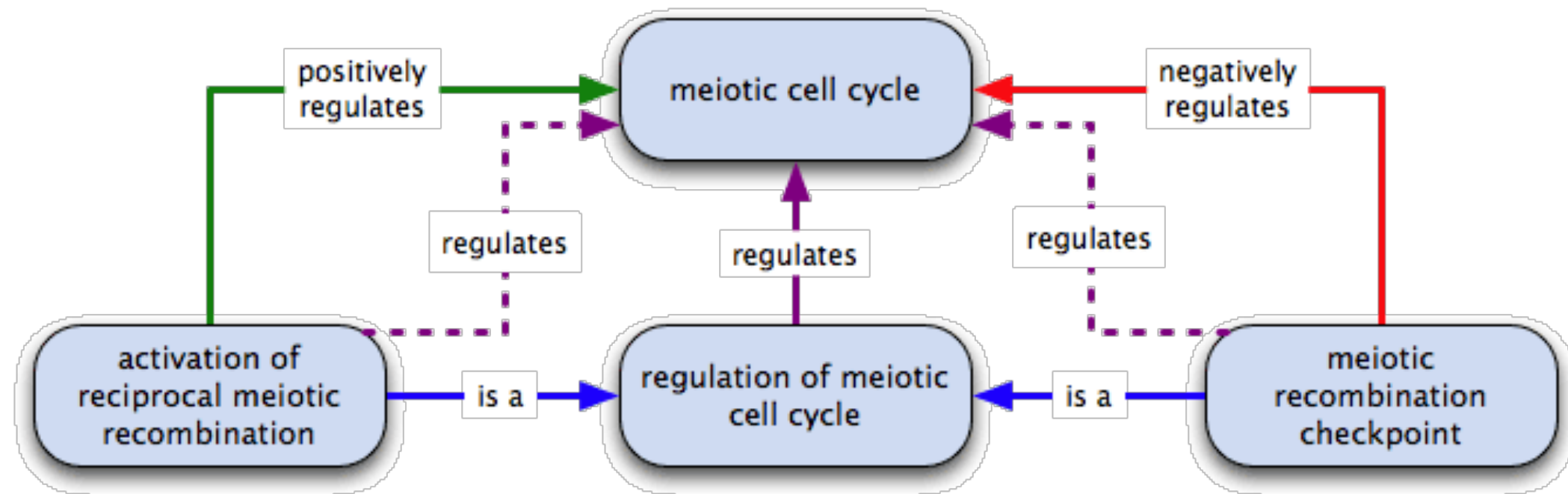
has part



- spliceosomal complex has part U4/U6 x U5 tri-snRNP complex
- U4/U6 x U5 tri-snRNP complex has part snRNP U5
- therefore spliceosomal complex has part snRNP U5

Gene Ontology

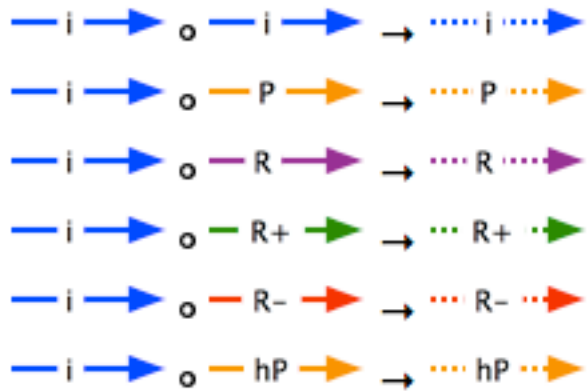
regulates



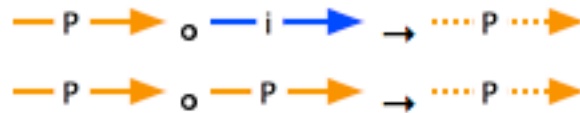
Gene Ontology

Inferences

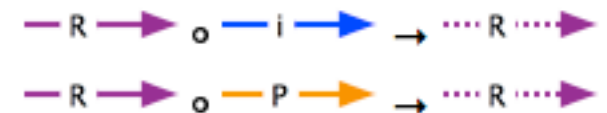
is a



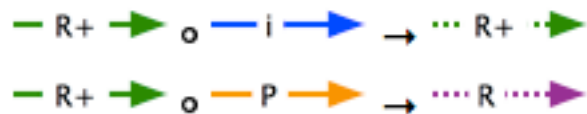
part of



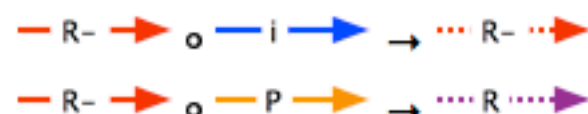
regulates



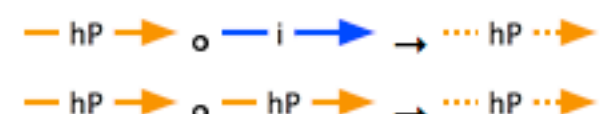
positively regulates



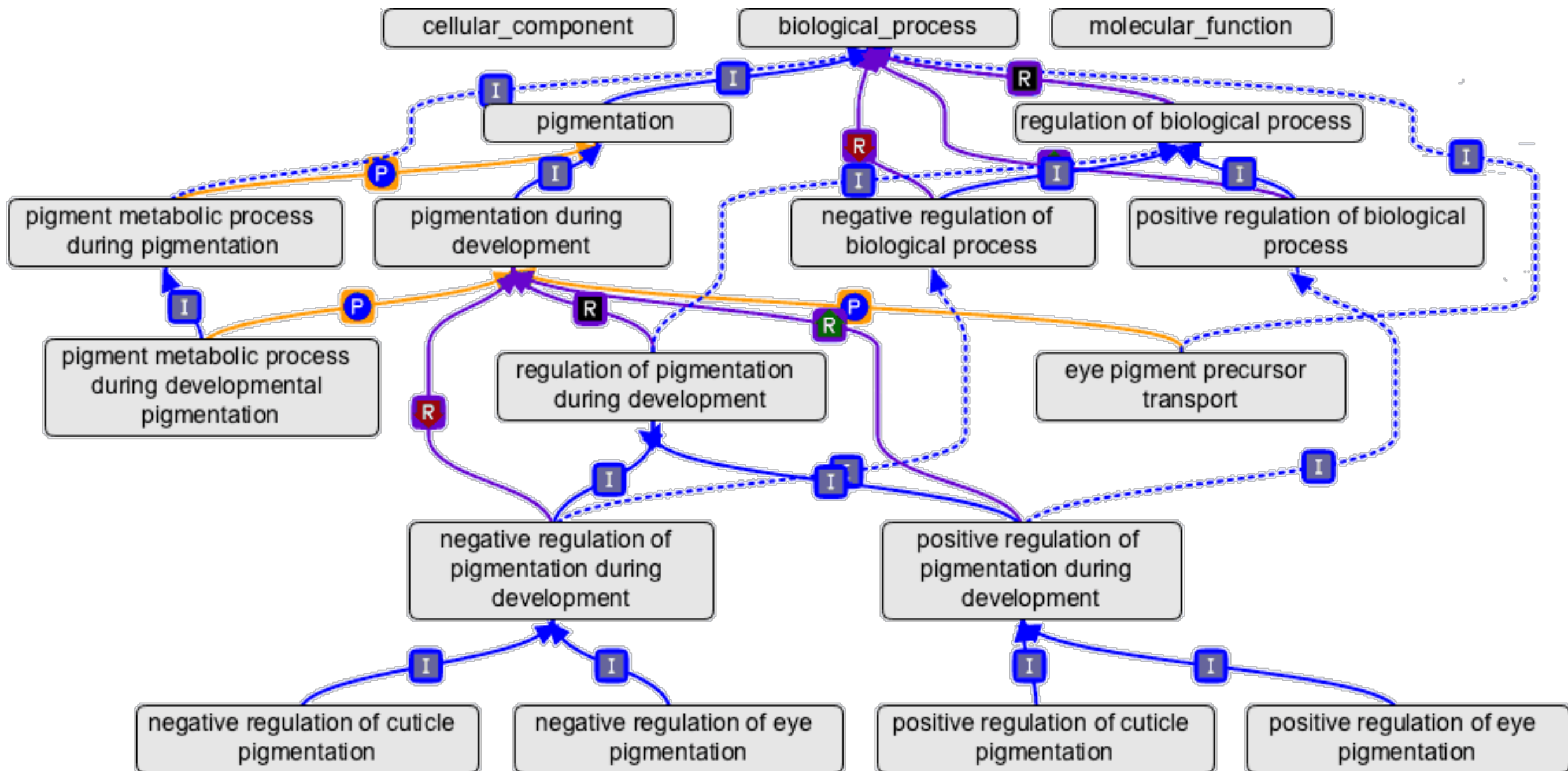
negatively regulates



has part



Gene Ontology



Each term can have relationships to one or more other terms in the same or other domains

Gene Ontology

Ten Quick Tips for Using the Gene Ontology

1. Know the Source of the GO Annotations You Use
2. Understand the Scope of GO Annotations
3. Consider Differences in Evidence Codes
4. Probe Completeness of GO Annotations
5. Understand the Complexity of the GO Structure
6. Choose Analysis Tools Carefully
7. Provide the Version of the Data/Tools Used
8. Seek Input from the GOC Community and Make Use of GOC Resources
9. Contribute to the GO
10. Acknowledge the Work of the GO Consortium

Gene Ontology

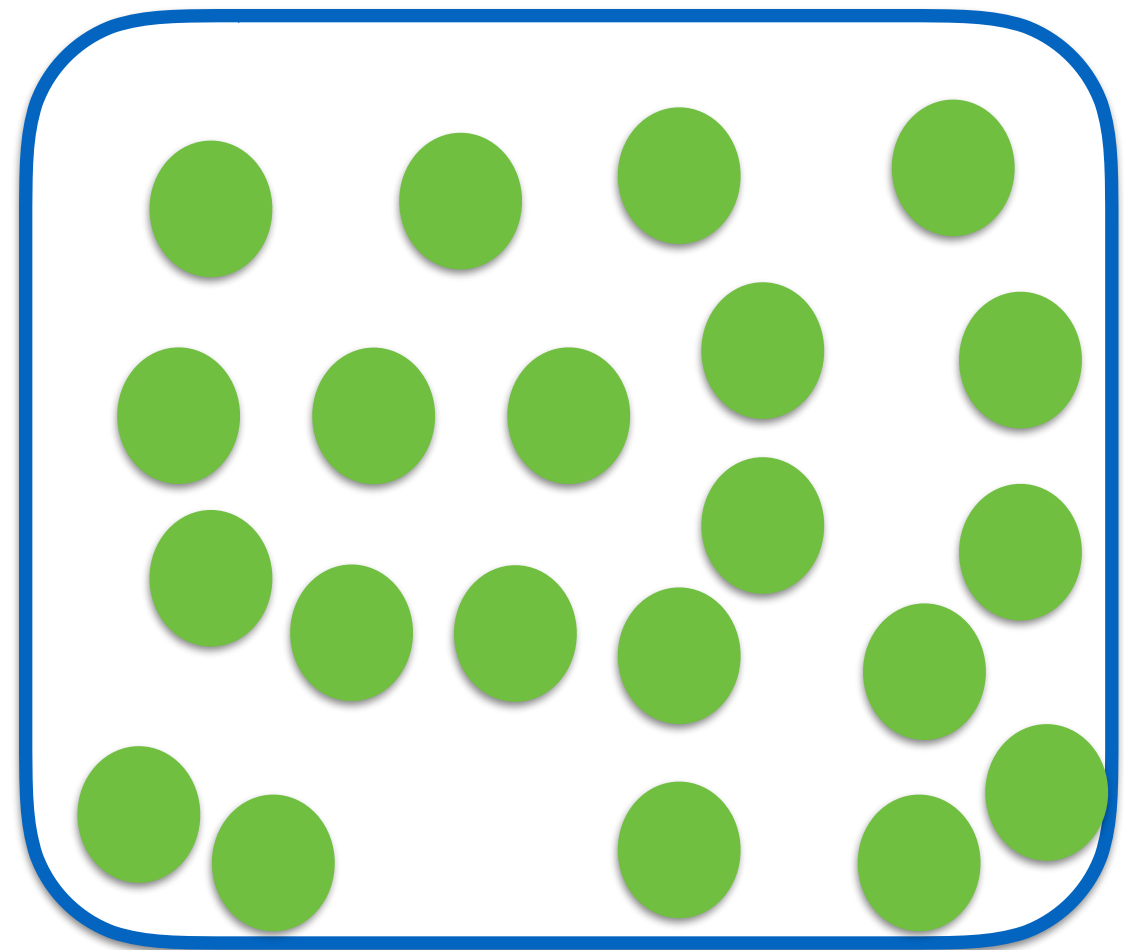
GO Enrichment Analysis

For a set of genes up/down-regulated find which GO terms are over-represented (or under-represented) using annotations for that gene set

Gene Ontology

Basic Enrichment Analysis

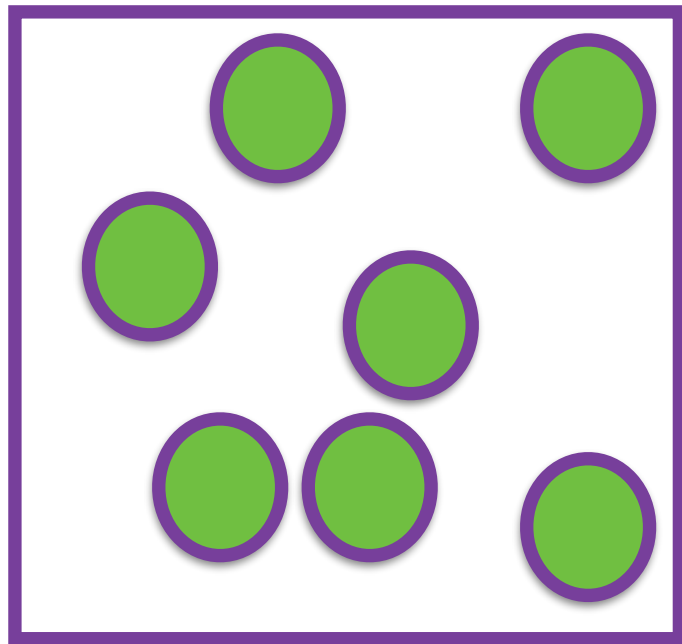
Global Gene Set



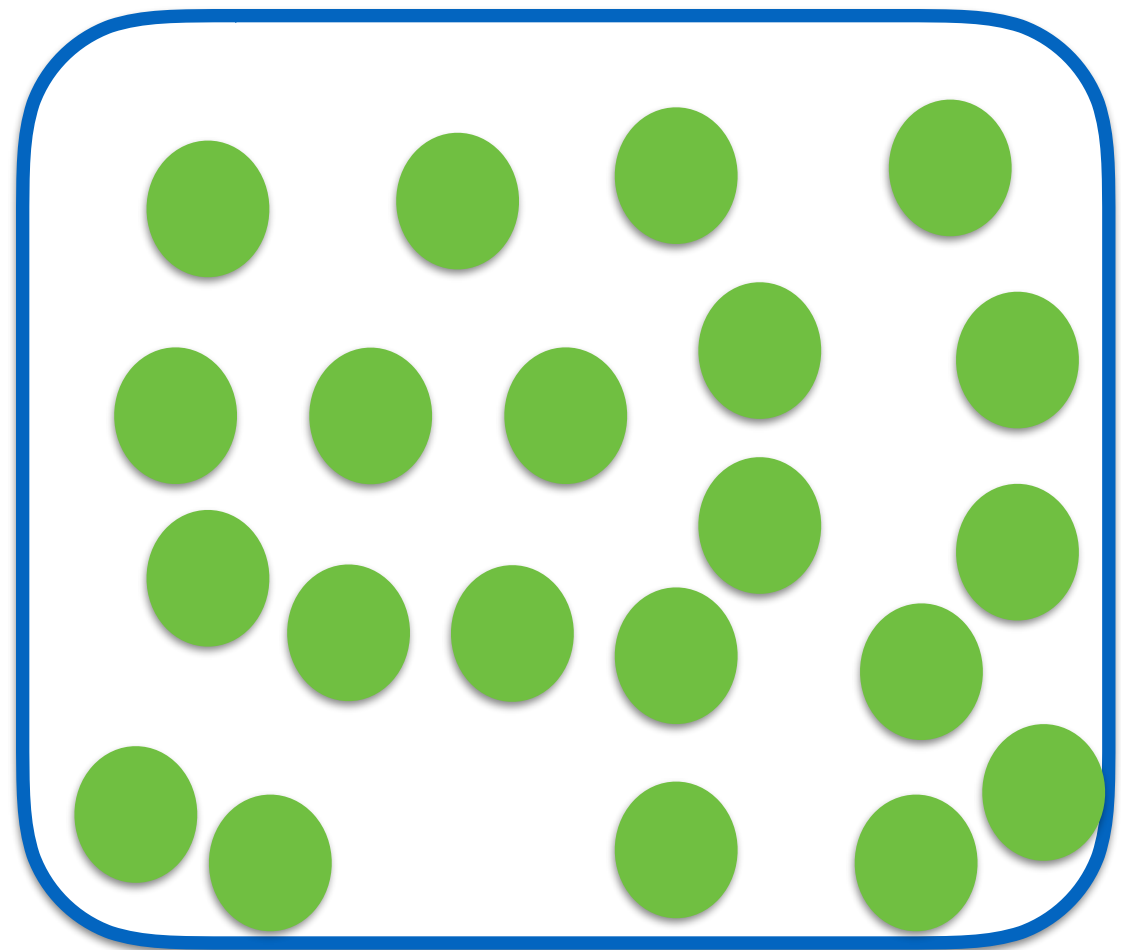
Gene Ontology

Basic Enrichment Analysis

GO Category or Pathway of interest



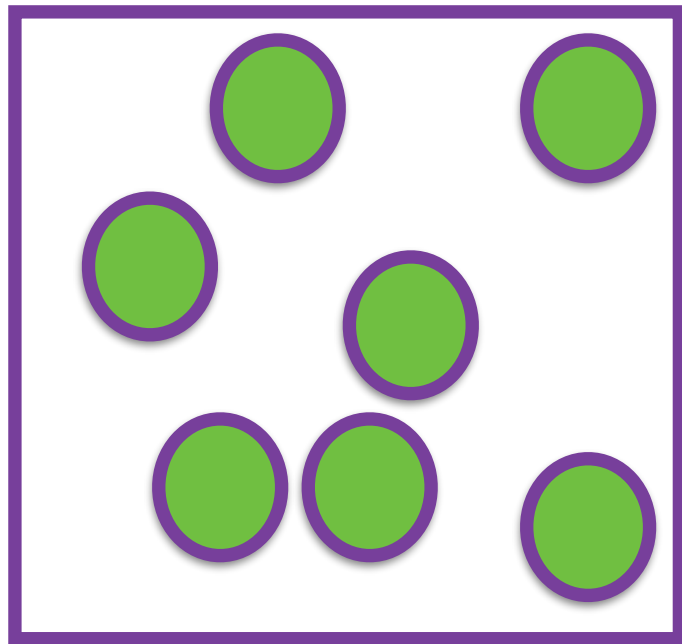
Global Gene Set



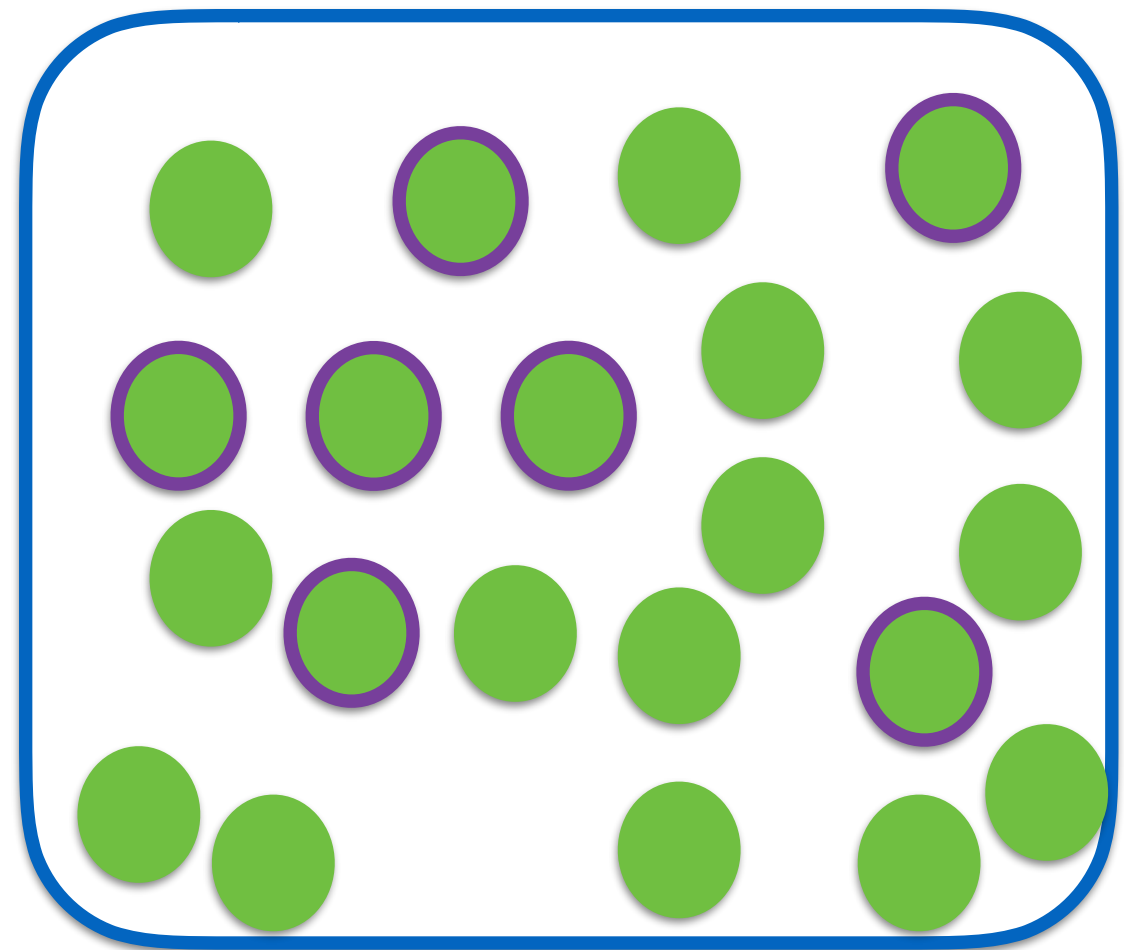
Gene Ontology

Basic Enrichment Analysis

GO Category or Pathway of interest



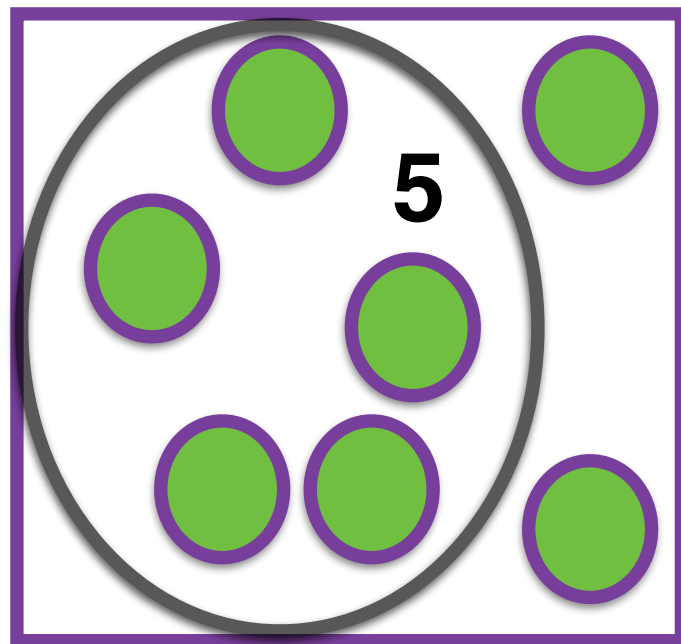
Global Gene Set



Gene Ontology

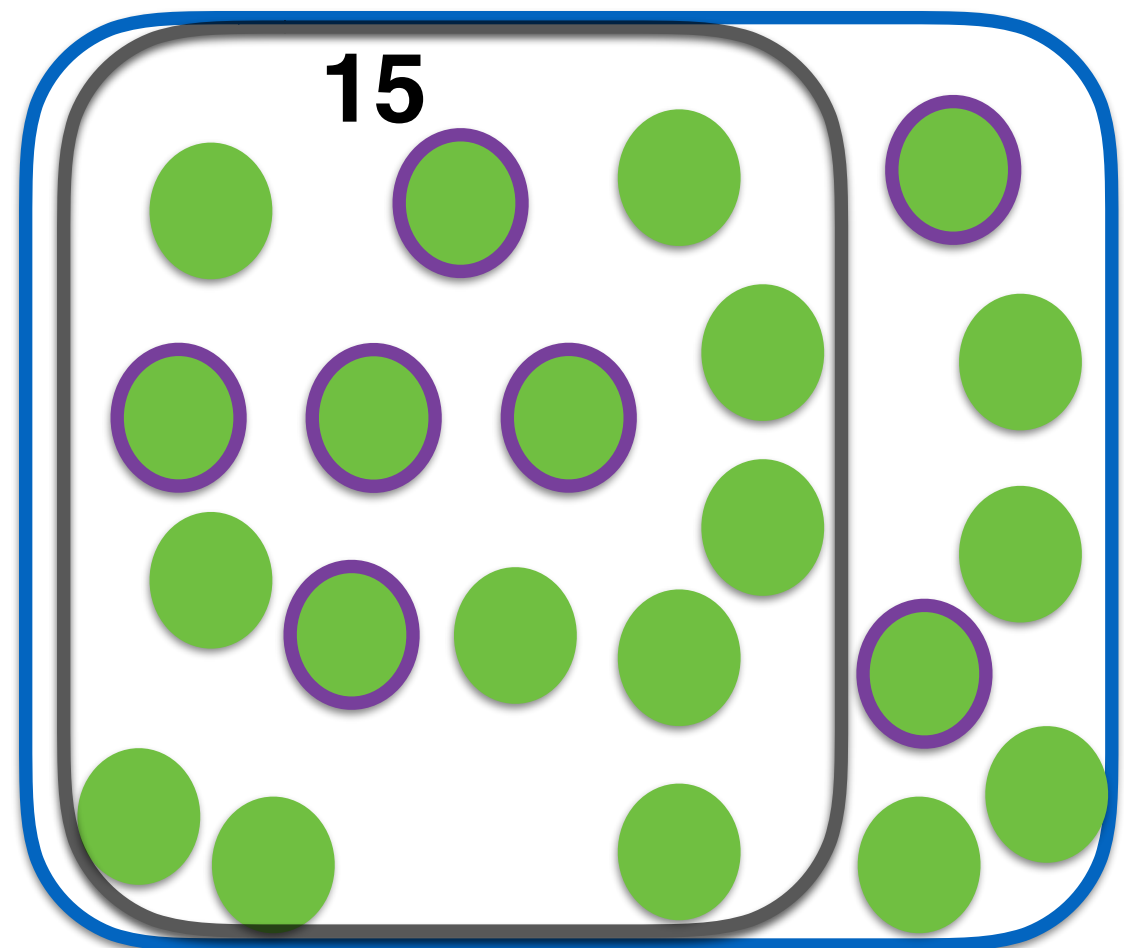
Basic Enrichment Analysis

GO Category or Pathway of interest



query/tested

Global Gene Set

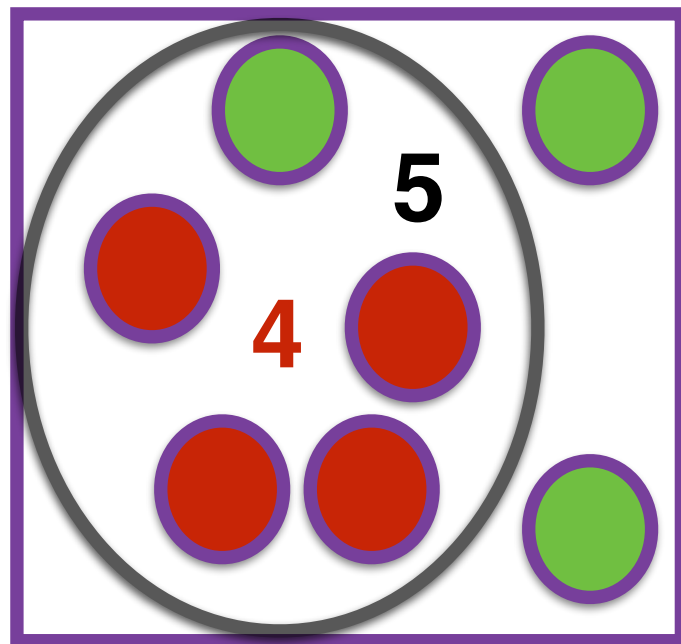


**select the right background set
e.g. right organism**

Gene Ontology

Basic Enrichment Analysis

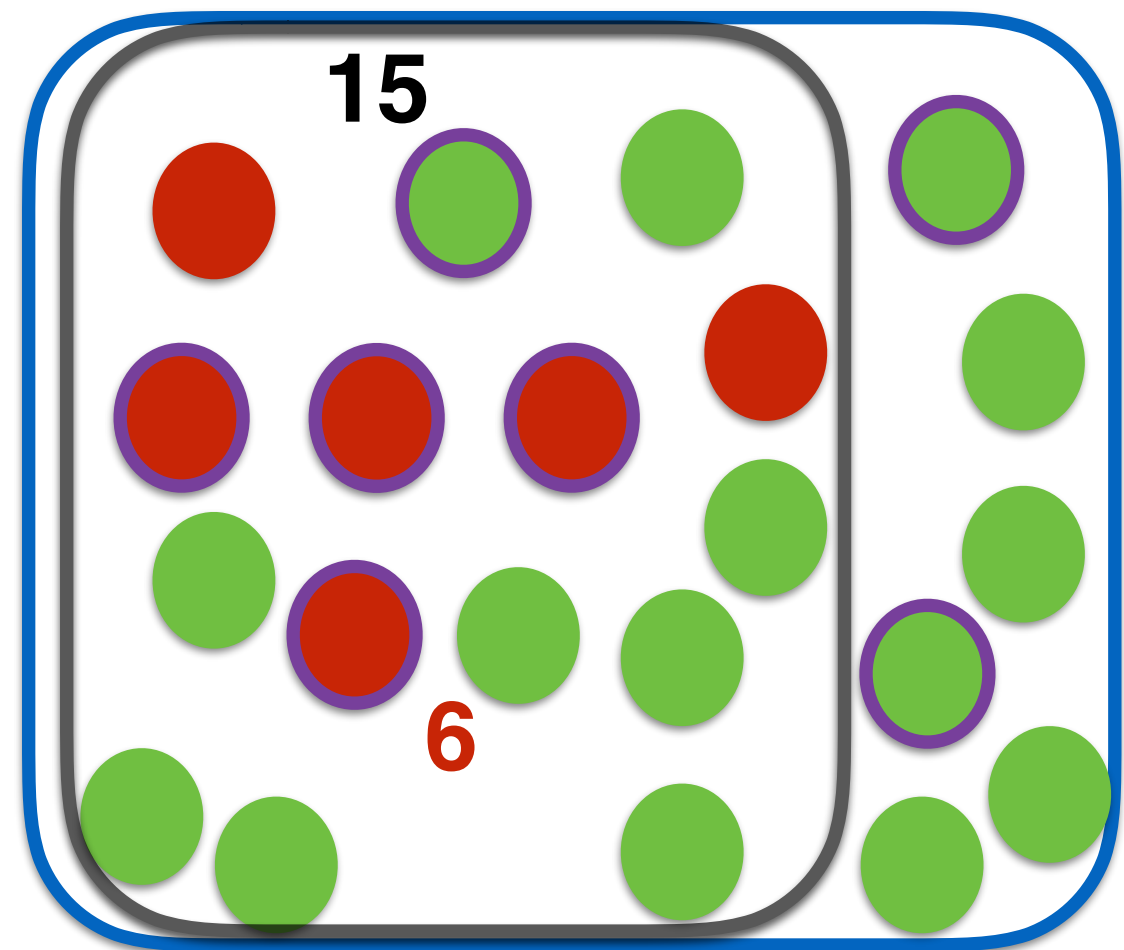
GO Category or Pathway of interest



Experimentally tested

**Interesting behavior
E.g. Unregulated**

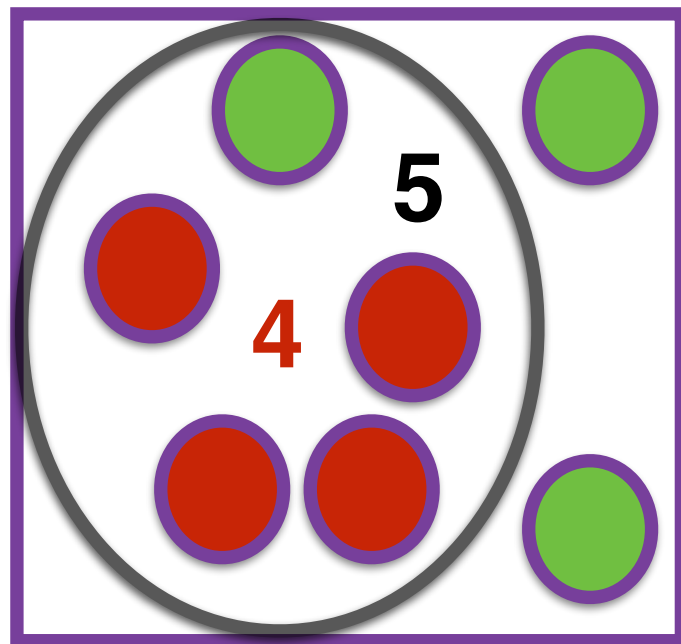
Global Gene Set



Gene Ontology

Basic Enrichment Analysis

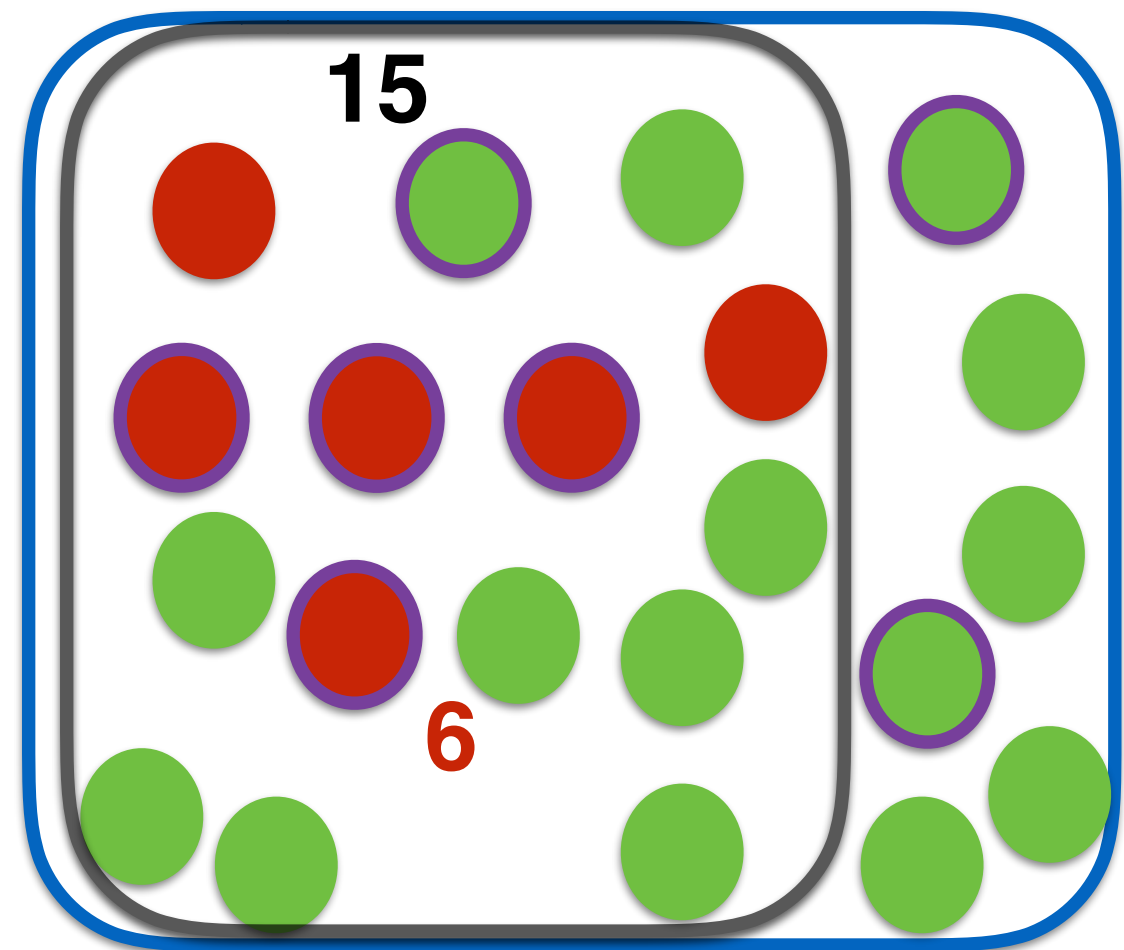
GO Category or Pathway of interest



Experimentally tested

**Interesting behavior
E.g. Unregulated**

Global Gene Set

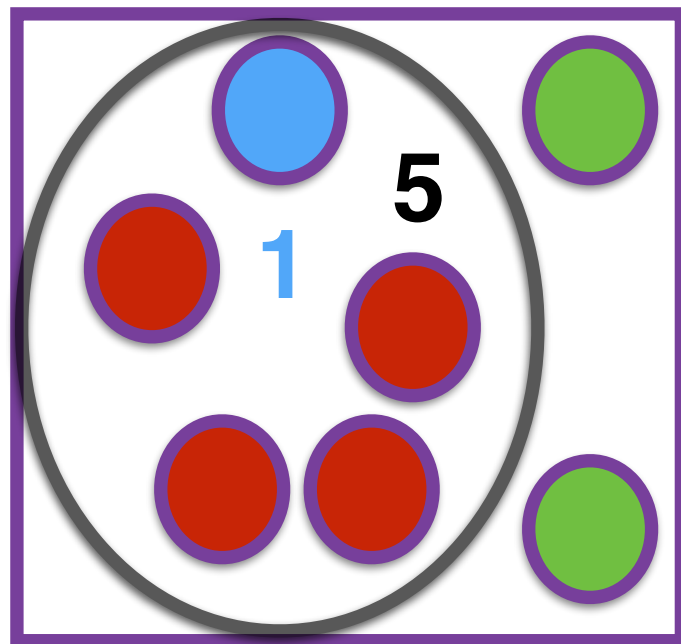


4 out of 6 Vs 5 out of 15

Gene Ontology

Basic Enrichment Analysis

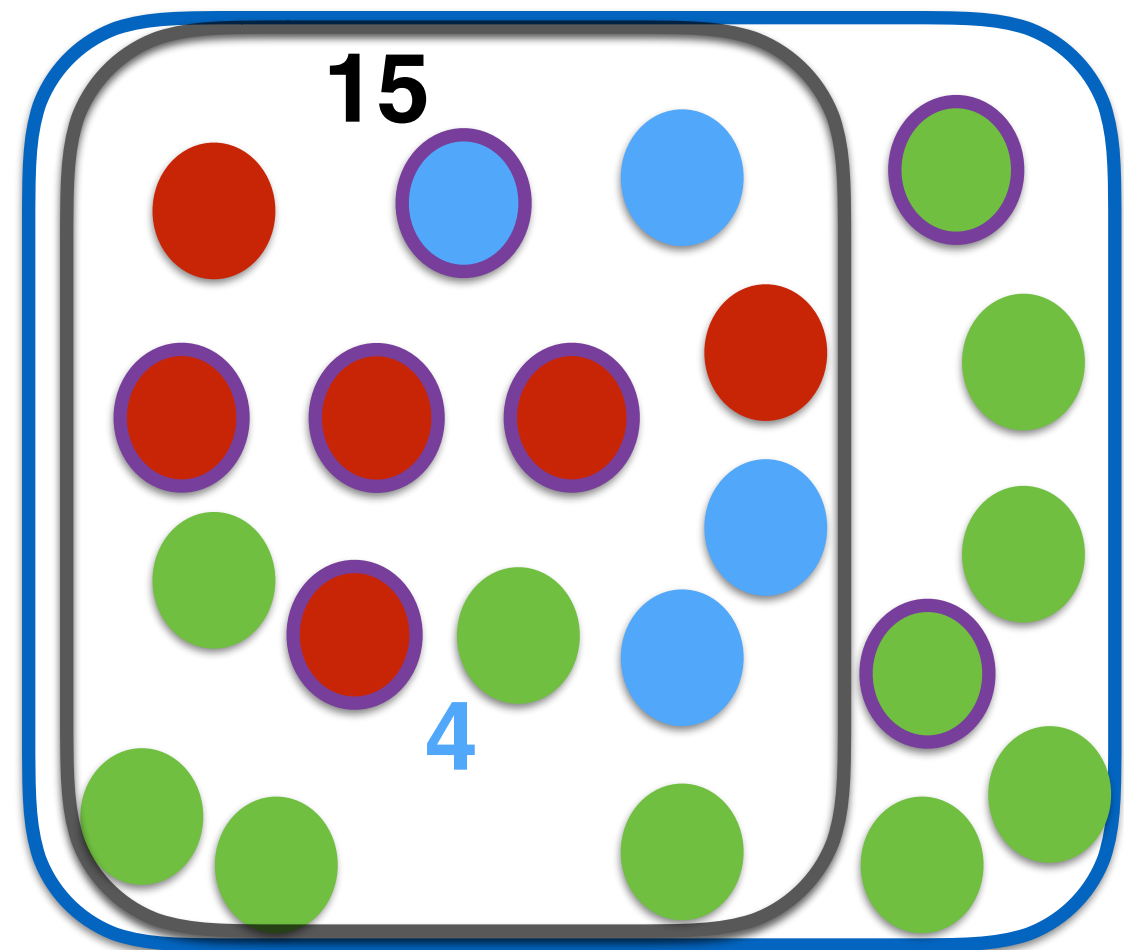
GO Category or Pathway of interest



Experimentally tested

Interesting behavior
E.g. Downregulated

Global Gene Set

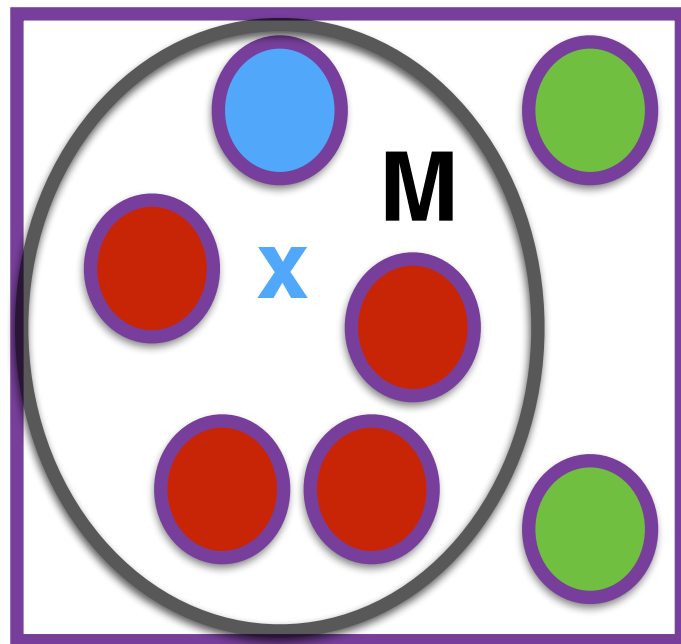


1 out of 4 Vs 5 out of 15

Gene Ontology

Basic Enrichment Analysis

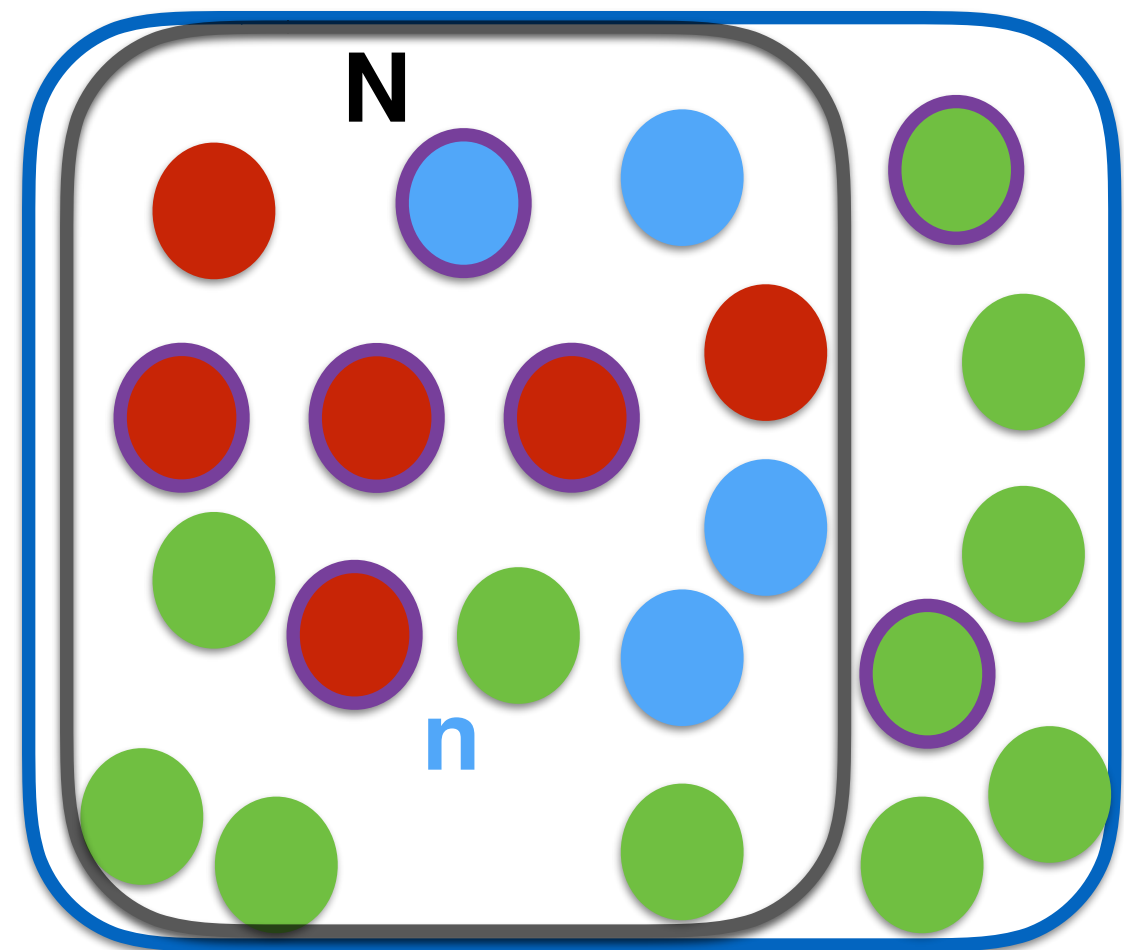
GO Category or Pathway of interest



Experimentally tested

Interesting behavior

Global Gene Set



x out of n Vs M out of N

Gene Ontology

Basic Enrichment Analysis

probability of getting at least x successes, i.e. x or more genes in the GO category (hypergeometric function sum)

$$p = \sum_{i=x}^n \frac{\binom{M}{i} \binom{N-M}{n-i}}{\binom{N}{n}}$$

- N genes in big set
- M genes in category in big set
- n genes of interest
- looking of x or more hits

where

$$\binom{k}{l} = \frac{k!}{l!(k-l)!}$$

Remember to Correct For Multiple Hypothesis Tests

x out of n Vs **M out of N**

Gene Ontology

- Panther (pantherdb.org)
- <http://geneontology.org>
- DAVID (<https://david.ncifcrf.gov>)
- GSEA (<http://software.broadinstitute.org/gsea/index.jsp>)
- many others...

